

Electron-Induced Excitation, Recombination, and Dissociation of Molecular Ions Initiating the Formation of Complex Organic Molecules

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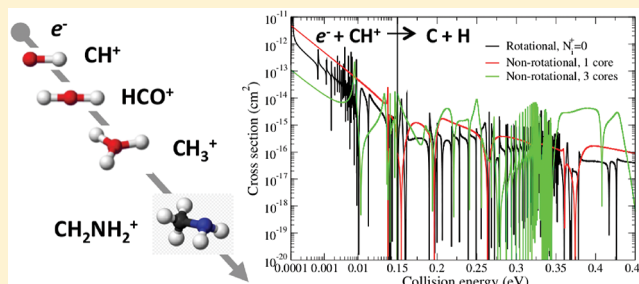
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ABSTRACT: We review the study of dissociative recombination and rovibrational excitation of diatomic and small polyatomic molecular ions initiating complex organic molecules formation. In particular, we show how multichannel quantum defect theory (MQDT) and R-matrix methods are used to compute cross-sections and rate coefficients for cations in well-defined rovibrational levels of the ground electronic state, from sub-meV up to a few eV collision energies. The most recent MQDT results are compared either with other theoretical data or with measured data obtained in storage-ring experiments.

KEYWORDS: Superexcited molecular states, Multichannel quantum defect theory, R-matrix method, Low energy electron collision, Carbon-based molecular cations



1. INTRODUCTION

The cold ionized media of astrophysical interest, namely, the interstellar molecular clouds, the supernovae, and the planetary atmospheres, etc., are the seat of an extremely rich chemical physics, due to the presence of numerous atomic and molecular species—neutral or ionized—photons, low-energy electrons, and cosmic rays.

There is a variety of processes that can lead to the formation/destruction of molecules in the interstellar medium (ISM), but these can be separated into two broad classes: reactions that occur in the gas phase and reactions that occur on the surfaces of small grains prevalent throughout the interstellar medium.

The reactions taking place in the gas phase can be further divided¹ into *bond-forming* processes, including radiative association, which link atoms and molecules into more complex species, i.e., complex organic molecules (COMs) or

polycyclic aromatic hydrocarbons (PAHs), and *bond-destruction* processes, such as photo-ionization, photodissociation, atomic- and molecular-induced collisional dissociation, and electron-impact dissociative recombination, which result into stable and metastable smaller species and/or radicals.

Finally, the *bond-rearrangement* reactions—ion–molecule charge-transfer reactions and neutral–neutral reactions—transfer parts of one co-reactant to another one.

An important case is the carbon chemistry of the diffuse² and/or dense³ ISM, which starts from the carbon atom and

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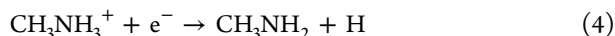
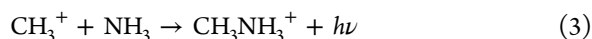
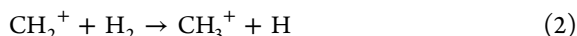
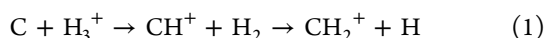
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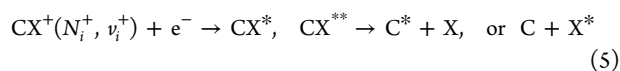
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results through the bond-forming/rearrangement processes to complex molecules such as HCO, HOC, HCN, CH₃OH, HCOOCH₃, and CH₃NH₂, as, e.g., in the following chain of reactions:⁴



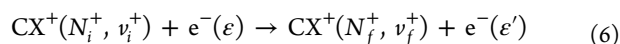
More examples can be found in Figures 15, 16, 19, 20, and 22 of ref 5 where many other pathways for COMs formations are proposed.

In essentially all of these formation pathways relevant for the ISM environments, where the temperature and pressure are very low, carbon-containing diatomic or polyatomic molecular cations, CX⁺, are involved. The abundance of carbon-containing molecules is partly driven by the electron-induced dissociative recombination (DR):



where X stands for atomic or molecular species containing hydrogen, oxygen, and fluorine, etc., N_i^+ and ν_i^+ denote respectively the initial rovibrational levels of the molecular ion in its electronic ground state, and CX^{**} stands for dissociative autoionizing—often doubly excited—states and CX^{*} for bound excited states belonging to Rydberg series of the neutral.

Meanwhile, within the same reactive collision, this ion-destruction process competes with transitions between the rovibrational states of the target:



where N_f^+ and ν_f^+ are its final rotational and vibrational quantum numbers, and ε/ε' the initial/final energy of the incident electron.

In the often non-equilibrium and cold environments of astrochemical interest, the qualitative and quantitative understanding of the formation of COMs are critically based on the precise knowledge of state-to-state cross-sections and/or rate coefficients of the electron-induced dissociation and/or excitation of molecular cations.

The present paper is divided into two parts.

The first one deals with the diatomic systems. The multichannel quantum defect theory (MQDT) is used to calculate state-to-state DR cross-sections and rate coefficients for molecular cations such as CH⁺, CO⁺, and CF⁺. The detailed presentation of the method is followed by the results with special focus on the driving mechanisms.

The second part presents our results obtained for polyatomic systems. The MQDT and the normal-mode approach combined with the R-matrix theory is applied for calculating DR cross-sections for H₃O⁺, HCO⁺, CH₃⁺, and CH₂NH₂⁺.

This work ends with conclusions and future plans.

2. MULTICHANNEL QUANTUM DEFECT THEORY OF ELECTRON/DIATOMIC MOLECULAR CATION COLLISIONS

We currently use an MQDT-type method to study the electron-impact collision processes given by eqs 5 and 6. These processes involve *ionization* channels, describing the scattering of an electron on the molecular ion, and *dissociation* channels, accounting for atom–atom scattering. The mixing of these channels results in quantum interference of the *direct* mechanism—in which the capture takes place into a dissociative state of the neutral system (CX^{**})—and the *indirect* one—in which the capture occurs via a Rydberg state of the molecule CX^{*}, predissociated by the CX^{**} state. The direct mechanism dominates the reactive collisions in the cases of favorable crossings (in the sense of the Franck–Condon principle) between the potential energy curves of the dissociative states and that of the target ion—CO⁺ and CF⁺—and is exceeded by the indirect one otherwise—CH⁺—as shown below. In both mechanisms the auto-ionization is in competition with the predissociation, and leads, through reaction 6, to *superelastic collision* (SEC; $\varepsilon' > \varepsilon$), *elastic collision* (EC; $\varepsilon' = \varepsilon$), and *inelastic collision* (IC; $\varepsilon' < \varepsilon$).

A detailed description of our theoretical approach has been given in previous studies on different diatomic systems, including the carbon-containing ones.^{6–14} The main ideas and steps are recalled below for the three standard situations (a, b, and c) encountered. This is performed in the order of the accuracy in predicting the cross-section, from the very fine modeling of the rotational (a) and/or vibrational (a, b) resonances associated with the temporary capture into singly excited Rydberg states, to that of the broad resonances associated with the capture into doubly excited states (c). Whereas the major relevant details are provided for the a case taken as reference, we outline either the simplifications or the extensions in the situations b and c with respect to the former.

(a) *Accounting of rotational and vibrational structures and interactions for the target ion's ground electronic state and for the neutral's relevant electronic states.*¹⁰

The major steps in this case are the following.

(1) *Building the interaction matrix \mathcal{V}* : Within a quasi-adiabatic representation of the CX states, and for a given set of conserved quantum numbers of the neutral system, Λ (projection of the electronic angular momentum on the internuclear axis), S (total electronic spin), and N (total rotational quantum number), the interaction matrix is based on the couplings between *ionization* channels—associated with the rovibrational levels N^+, ν^+ of the cation and to the orbital quantum number l of the incident/Rydberg electron—and *dissociation* channels, d_j . The structure of the interaction matrix \mathcal{V} introduced in step 1 is in block form,

$$\mathcal{V} = \begin{pmatrix} 0 & \mathcal{V}_{\bar{d} \overline{\text{N}_c \nu_c}} \\ \mathcal{V}_{\overline{\text{N}_c \nu_c} \bar{d}} & 0 \end{pmatrix} \quad (7)$$

where the collective indices \bar{d} and $\overline{\text{N}_c \nu_c}$ span the ensembles of all individual indices d_j and N^+, ν^+ , which respectively label dissociation channels and ionization channels, the latter ones built on the ground electronic state of the ion—also called ground core, and labeled c. The only nonvanishing matrix elements organized in the nondiagonal blocks express the *Rydberg–valence* interaction.

(2) *Computation of the reaction matrix \mathcal{K}* : Given H_0 the Hamiltonian of the molecular system under study in which the Rydberg–valence interaction is neglected, we adopt the second-order perturbative solution for the Lippman–Schwinger integral equation,¹⁵ written in operator form as

$$\mathcal{K} = \mathcal{V} + \mathcal{V} \frac{1}{E - H_0} \mathcal{V} \quad (8)$$

(3) *Diagonalization of the reaction matrix*, yielding the eigenvectors and eigenvalues used to build the eigenchannel wave functions.

(4) *Frame transformation* from the Born–Oppenheimer (short-range) representation, characterized by N , v , and Λ quantum numbers, valid for small electron–ion and nucleus–nucleus distances, to the close-coupling (long-range) representation, characterized by N^+ , v^+ , Λ^+ (for the ion), and l (orbital quantum number of the incident/Rydberg electron), valid for both large distances. This frame transformation relies on the quantum defects, $\mu_l^\Lambda(R)$, describing the relevant Rydberg series built on the ionic core, and on the eigenvectors and eigenvalues of the \mathbf{K} -matrix.

(5) *Building of the generalized scattering matrix \mathbf{X}* : On the basis of the frame-transformation coefficients, this matrix being organized in blocks associated with energetically open and/or closed (O and/or C, respectively) channels (“C” for “closed” to be distinguished from “c” for “core”).

$$\mathbf{X} = \begin{pmatrix} \mathbf{X}_{\text{OO}} & \mathbf{X}_{\text{OC}} \\ \mathbf{X}_{\text{CO}} & \mathbf{X}_{\text{CC}} \end{pmatrix} \quad (9)$$

(6) *Building of the physical scattering matrix \mathbf{S}* :

$$\mathbf{S} = \mathbf{X}_{\text{OO}} - \mathbf{X}_{\text{OC}} \frac{1}{\mathbf{X}_{\text{CC}} - \exp(-i(2\pi)\nu)} \mathbf{X}_{\text{CO}} \quad (10)$$

The first term in eq 10 is restricted to the open channels, resulting in the *direct* mechanism, and the second takes into account their mixing with the closed ones, resulting in the *total*, i.e., direct and indirect mechanism, the denominator being responsible for the resonant patterns in the shape of the cross-section.¹⁶ Here the matrix $\exp(-i(2\pi)\nu)$ is diagonal and relies on the effective quantum numbers ν_{N^+,v^+} associated with the vibrational thresholds of the closed ionization channels.

(7) *Computation of the cross-sections*: For a given target cation on the rovibrational level N_i^+, v_i^+ and for a given energy of the incident electron, ϵ , the dissociative recombination and the rovibrational transition—elastic scattering, excitation, and de-excitation—the cross-sections are computed using, respectively,

$$\sigma_{\text{diss} \leftarrow N_i^+, v_i^+}^N = \frac{\pi}{4\epsilon} \frac{2N+1}{2N_i^++1} \rho \sum_{l, \Lambda, d_j} |S_{d_j, l N_i^+, v_i^+}^{N\Lambda}|^2 \quad (11)$$

$$\begin{aligned} \sigma_{N_f^+, v_f^+ \leftarrow N_i^+, v_i^+}^N &= \frac{\pi}{4\epsilon} \frac{2N+1}{2N_i^++1} \rho \\ &\times \sum_{l, l', \Lambda} |S_{N_f^+, v_f^+, l', N_i^+, v_i^+, l}^{N\Lambda} - \delta_{N_f^+, N_i^+} \delta_{v_f^+, v_i^+} \delta_{l', l}|^2 \end{aligned} \quad (12)$$

where ρ stands for the ratio between the spin multiplicities of the involved electronic states of CX and that of the target, CX^+ .

(b) *Accounting of vibrational structures and interactions, neglecting the rotational ones, for the target ion's ground electronic state and for the neutral's relevant electronic states* ref. 11. The

target and the neutral systems are considered rotationally relaxed, and N^+ is not a parameter in steps 1–6 of case a. In particular, the structure of the interaction matrix \mathcal{V} introduced in step 1 is, in block form,

$$\mathcal{V} = \begin{pmatrix} 0 & \mathcal{V}_{\bar{d}\bar{v}} \\ \mathcal{V}_{\bar{v}\bar{d}} & 0 \end{pmatrix} \quad (13)$$

With respect to step 7, formulas 11 and 12 become

$$\sigma_{\text{diss} \leftarrow v_i^+} = \frac{\pi}{4\epsilon} \sum_{l, \Lambda} \rho^\Lambda \sum_j |S_{d_j, l v_i^+}^\Lambda|^2 \quad (14)$$

$$\sigma_{v_f^+ \leftarrow v_i^+} = \frac{\pi}{4\epsilon} \sum_{l, l', \Lambda} \rho^\Lambda |S_{l', v_f^+, l v_i^+}^\Lambda - \delta_{l', l} \delta_{v_f^+, v_i^+}|^2 \quad (15)$$

Here ρ^Λ is the ratio between the spin and angular momentum multiplicities of the neutral and the target ion.

(c) *Accounting for vibrational structures and interactions, neglecting the rotational ones, for the target ion's ground and excited bound electronic states, and for the neutral's relevant electronic states*.¹⁴ The structure of the interaction matrix \mathcal{V} in block form, more complex than that in case b. Equation 13, is, e.g., for the case of one ground bound electronic core and two excited bound electronic cores the following:

$$\mathcal{V} = \begin{pmatrix} 0 & \mathcal{V}_{\bar{d}\bar{v}_1} & \mathcal{V}_{\bar{d}\bar{v}_2} & \mathcal{V}_{\bar{d}\bar{v}_3} \\ \mathcal{V}_{\bar{v}_1\bar{d}} & 0 & \mathcal{V}_{\bar{v}_1\bar{v}_2} & \mathcal{V}_{\bar{v}_1\bar{v}_3} \\ \mathcal{V}_{\bar{v}_2\bar{d}} & \mathcal{V}_{\bar{v}_2\bar{v}_1} & 0 & \mathcal{V}_{\bar{v}_2\bar{v}_3} \\ \mathcal{V}_{\bar{v}_3\bar{d}} & \mathcal{V}_{\bar{v}_3\bar{v}_1} & \mathcal{V}_{\bar{v}_3\bar{v}_2} & 0 \end{pmatrix} \quad (16)$$

where the collective indices \bar{d} , \bar{v}_{ci} , $i = 1, 2, 3$, span the ensembles of all individual indices connected to the dissociation channels and ionization channels built on c_1 (ground), c_2 , and c_3 (excited) ion cores.^{6–14}

Here, besides the *Rydberg–valence* interactions, represented by $\mathcal{V}_{\bar{d}\bar{v}_1}$, $\mathcal{V}_{\bar{d}\bar{v}_2}$, and $\mathcal{V}_{\bar{d}\bar{v}_3}$, like in eqs 7 and 13, one may notice the appearance of the *Rydberg–Rydberg* ones, represented by $\mathcal{V}_{\bar{v}_1\bar{v}_2}$, $\mathcal{V}_{\bar{v}_1\bar{v}_3}$, and $\mathcal{V}_{\bar{v}_2\bar{v}_3}$.

3. APPLICATION TO CARBON-BASED DIATOMIC MOLECULAR SYSTEMS

The molecular data necessary to model the dissociative recombination and the rovibrational (de)excitation given in the diabatic representation are as follows:

- the potential energy curve (PEC) of the ground state of the ion, CX^+ ;
- the PECs of the excited attractive states energetically close to the ion's ground-state one, CX^{+*} ;
- the PECs of the valence dissociative states of the neutral CX^{**} interacting with the ionization continua;
- the PECs of the Rydberg bound states CX^* associated with the ionization continua and situated below the ion states CX^+ or/and CX^{+*} , which can be conveniently described by smooth R -dependent quantum defects, predissociated by the CX^{**} states and being furthermore subject to interseries Rydberg–Rydberg interactions;
- the electronic couplings between the valence dissociative states and the Rydberg manifolds, as well as the

Rydberg–Rydberg electronic couplings whenever multiple Rydberg manifolds are present.

A representative example of molecular data needed for the MQDT calculations—relevant for the DR of CH^+ —is shown in Figure 1.

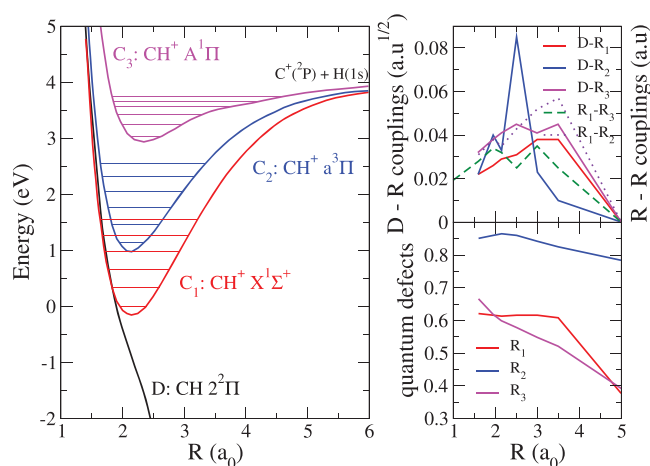


Figure 1. Molecular data sets relevant for the dissociative recombination of CH^+ compiled from Figures 2–5 of ref 7. Left panel: red, blue, and magenta continuous lines, the ground (C_1 , $X^1\Sigma^+$) and the lowest two excited (C_2 , $a^3\Pi$; C_3 , $A^1\Pi$) electronic states of the ion, having the $\text{C}^+(^2\text{P}) + \text{H}(1\text{s})$ dissociation limit, whereas the black continuous (D) line gives the dissociative auto-ionizing state ($2^2\Pi$) of the neutral. Upper right panel: electronic couplings; red, blue, and magenta lines between the valence state (D) and the states belonging to the Rydberg series R_1 , R_2 , and R_3 built on the C_1 , C_2 , and C_3 ion cores, respectively. The violet dotted and the green dashed lines stand for the couplings of the R_1 Rydberg series to the R_2 one and that of the R_1 Rydberg series to the R_3 one, respectively. The coupling between R_2 and R_3 was considered zero. Lower right panel: quantum defects for the Rydberg series based on the ground and excited ion cores.

The DR cross-section is extremely sensitive to the position of the neutral dissociative states with respect to that of the target ion.

Several methods are available to provide all of the necessary molecular data with the desired accuracy. Among these are R-matrix theory,¹⁷ the complex Kohn variational method,¹⁸ the quantum defect methods,¹⁹ the interpretation of spectroscopic data,²⁰ and the block diagonalization method.^{21,22}

3.1. MQDT Calculations. Following the molecular data preparations as described above we have performed a series of MQDT calculations of cross-sections for DR and its competitive processes involving relevant cations, as follows.

3.1.1. CH^+ . CH^+ was first found in the interstellar molecular clouds in 1941 by Douglas and Herzberg.²³ Since then, its absorption lines have been observed toward many background stars, demonstrating the omnipresence of this simple carbon hydride in the diffuse interstellar medium (ISM). This outstanding abundance is so far unexplained.

The most probable formation channel of the CH^+ cation is the hydrogen abstraction reaction $\text{C}^+ + \text{H}_2 \rightarrow \text{CH}^+ + \text{H}$, which is endothermic. In order to be formed in a sufficient abundance for observation, alternative energy sources were suggested such as turbulent dissipation, shocks, or shears (see e.g., Valdivia et al.,²⁴ and references therein). Furthermore, it was found that, in photon-dominated regions, the rovibrationally excited H_2

reservoir can provide an alternative route to overcome the endothermicity of the formation reaction,²⁵ since the rotational and vibrational energies are as effective as the translational energy in promoting this type of reaction.²⁶

This reaction is in competition with the low-density process known as radiative association,⁴ $\text{C}^+ + \text{H} \rightarrow \text{CH}^* \rightarrow \text{CH}^+ + h\nu$ in which the collision complex is stabilized by emission of a photon.

Yet another ion–molecule reaction able to fix atomic carbon into a molecular form and thus start the buildup of organic molecules, according to refs 4 and 27, is the proton-exchange reaction: $\text{H}_3^+ + \text{C} \rightarrow \text{CH}^+ + \text{H}_2$.

It is obvious from the previous examples that the detailed knowledge of the CH^+ molecular cation chemistry can provide unique physical insights into the modeling of the different ISM environments. CH^+ is one of the major building block of the hydrocarbon chemistry,²⁸ that leads through radiative association to more complex radicals such as CH_3^+ or CH_5^+ , key pieces of the carbon chemistry of ISM that leads to COMs (for a representative sample see eqs 1–4). Thus, the full understanding of both production and loss mechanisms, as well as the competition between the radiative processes, the destruction of the ion, and the collisional excitation processes is needed to be known in detail.

CH^+ is easily destroyed by reactions with electrons and hydrogen atoms and also by reactions with H_2 molecules. Here we show and discuss cross-sections on the electron-induced destruction pathways and competitive processes such as rovibrational excitations.

The first complete potential energy curves of CH^+ and CH relevant for DR of CH^+ were produced by Giusti-Suzor and Lefebvre-Brion,²⁹ where the authors did not find a favorable crossing of the ion curve with a neutral one. This finding led to a slow DR rate coefficient. Similar results were obtained by the earlier theoretical calculations of Bardsley and Junker.³⁰ The most complete calculation was performed by Takagi et al.,³¹ who obtained the relevant molecular structure data using configuration mixing methods and provided reliable DR cross-sections and low-temperature rate coefficients using a different version of MQDT in reasonable agreement with that predicted by ref 30 and the experimental values given by Mitchell and McGowan.³²

On the experimental side, this first merged-beam measurement of DR for CH^+ ³² was followed by a new revised one of the same team,³³ resulting in slightly larger values. All of these results were later recompiled in ref 34. The most detailed experimental study of CH^+ DR performed on a heavy-ion storage-ring equipment, resulting in cross-sections, product branching ratios, and angular distributions, was given by Amitay et al.³⁵ Their measurements showed several broad and prominent resonances that were tentatively attributed to the capture of the incident electron into core-excited Rydberg states. In order to understand and characterize the broad resonances, Carata et al.⁷ performed, on a set of new molecular structure data of CH^+ and CH, new calculation by including in the available MQDT-DR approach the effect of these core-excited states in a first-order perturbative approximation.

Here we discuss two different sets of MQDT calculations,^{12,14,36} which have been performed for this molecular cation making use of the same molecular data sets, shown in Figure 1 and presented originally in ref 7.

In a first step, relying on the ground electronic state of the ion only, and valid for very low energy, the dissociation state of

the neutral, and the interaction between the ionization and the dissociation continua, we have computed the interaction, reaction, and scattering matrices and produced the DR cross-sections for the 11 lowest rotational levels of CH^+ in its ground electronic and vibrational states, using version a of our MQDT method.³⁶

In the second step of our MQDT calculations, devoted to higher incident electron energy, we focused on the importance of the excited bound ionic cores, using approach c, adopting a second-order perturbative solution for eq 8 in contrast to the first-order treatment employed in ref 7. Indeed, CH^+ has several bound excited states whose ionization continua are coupled to the ionization continuum of the ground core and to the neutral dissociative states. For the energy range characterizing the incident electron in the present work, two such excited states are relevant, i.e., those of a $^3\Pi$ and A $^1\Pi$ symmetry, which we respectively call core 2 and core 3. The neutral $2^2\Pi$ dissociative state is coupled to the ionization channels of the three ion cores and is mainly responsible for driving the low-energy DR mechanism.

We have used in total 42 ionization channels associated with 19 vibrational levels of the CH^+ ($X^1\Sigma^+$) ground state (c_1) and 14 and 9 vibrational levels of CH^+ (A $^3\Pi$) (c_2), and CH^+ (a $^1\Pi$) (c_3), respectively. The incident electron energy range is 0.01–0.5 eV, which is typical for the interstellar environments. The $l = 1$ (p) partial wave was considered for the incident/Rydberg electron.

The rate coefficients were determined at kinetic temperatures between 10 and 3000 K.

Figure 2 shows the DR cross-section for 1 core/1 dissociative state including rotation (black curve), 1 core/1

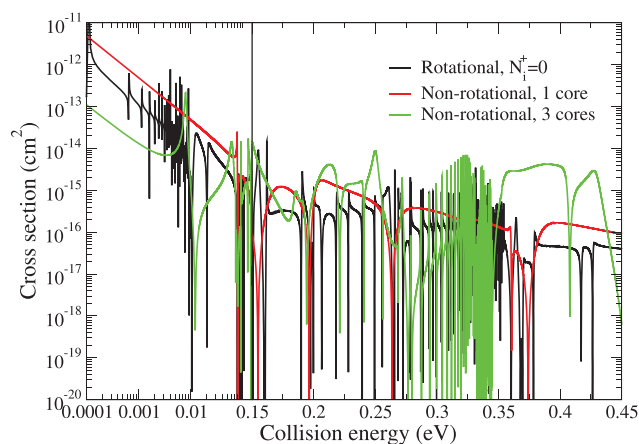


Figure 2. Cross-sections for the dissociative recombination of the vibrationally relaxed CH^+ by electrons as a function of the collision energy. The initial-state-specific ($N_i^+ = 0$) including rotation³⁶ are compared to two non-rotational calculations using the ground (red curve) and all three ionic cores (green curve).¹⁴ In the left panel the results are shown in log–log scale, while in the right one in log–linear scale.

dissociative state excluding rotation (MQDT approach b, red curve), and 3 cores/1 dissociative state excluding rotation (MQDT approach c, green curve) respectively.

The effects of inclusion of rotation (black vs red curves) and of the excited cores (red vs green curves) is striking. New Fano-type resonances appear in the cross-section due to the rovibrational levels of the superexcited Rydberg states of the neutral, correlating to the ground and excited ion states

(indirect mechanism). The quantum interference between the *direct* and *indirect* mechanisms lead to shifted mean cross-section values.

The best comparisons between the MQDT calculations and the storage-ring experiments can be made starting from the convoluted cross-sections shown in Figure 3. Here we have

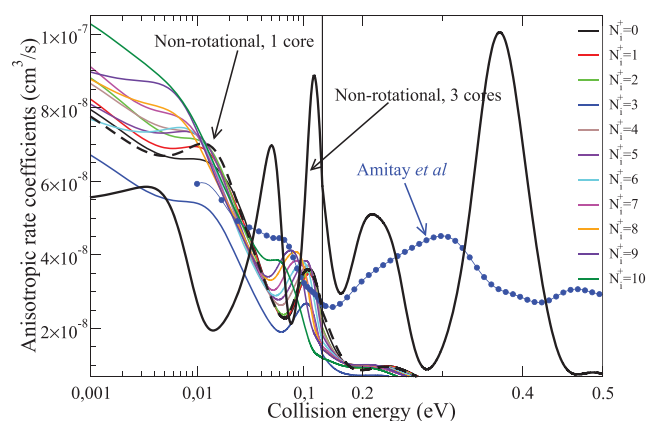


Figure 3. Anisotropic rate coefficients for the dissociative recombination of the vibrationally relaxed $\text{CH}^+(N_i^+)$ as a function of the kinetic energy of the electrons. The initial-state-specific rate coefficients (colored continuous lines)³⁶ are compared to two non-rotational calculations using the ground (black dashed line) and all three ionic cores (thick black line)¹⁴ and to the experimental results of Amitay et al.³⁵ (blue line with circles). The anisotropic Maxwell averaging was done according eq 1 of ref 37 using $T_{\perp} = 17$ meV and $T_{\parallel} = 0.5$ meV electron temperatures. In the left panel the results are shown in log–log scale, while in the right one in log–linear scale.

used anisotropic Maxwellian distribution taking into account the experimental conditions of Amitay et al.³⁵ Whereas the rotational effects are relevant for low collision energies, the excited core effects become important for higher energy, where the strong resonances revealed by the experiment are qualitatively well reproduced by our calculations. Meanwhile, the positions and the intensities of the experimentally observed resonance profiles are not yet quantitatively well reproduced. We hope to remove this disagreement by using in the near future more accurate molecular structure data on the superexcited electronic states of CH and by taking into account simultaneously the effects of core-excited resonances and of the rotational effects.

And finally in Figure 4 (using the same color code as that of Figure 3), the initial-state-specific (colored lines) DR rate coefficients are plotted as functions of the kinetic temperature. These rate coefficients were obtained by averaging the cross-sections over isotropic Maxwell–Boltzmann velocity distributions. The thermal average at a rotational temperature of 300 K is also shown (red dashed line), and it is compared to two sets of non-rotational MQDT calculations using the ground (black dashed line) and all three excited cores (thick black line) and to two sets of experimental rate coefficients. The first was obtained from a thermal average of the DR cross-sections measured by Amitay et al.³⁵ (blue line with circles), where the ions were assumed to be thermalized at the ambient temperature of the storage ring (300 K). In order to be able to compare the calculated rate coefficients with the measured ones at low electron temperatures, we have extrapolated the experimental cross-sections toward low collision energies assuming a Wigner-type behavior: $\sigma(\epsilon) = a_0/\epsilon$, where the

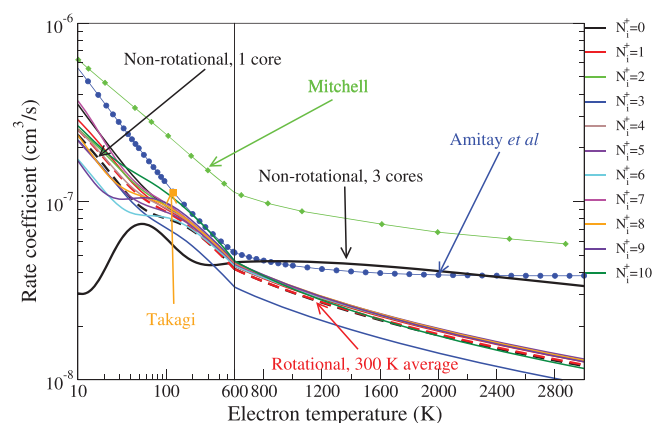


Figure 4. Maxwellian rate coefficients for the dissociative recombination of the vibrationally relaxed $\text{CH}^+(N_i^+)$ by electrons as a function of the kinetic temperature. The initial-state-specific (colored continuous lines) and 300 K thermal rate coefficients (red dashed line)^{12,36} are compared to two nonrotational calculations using the ground (black dashed line) and all three ionic cores (thick black line)¹⁴ and to the experimental results of Amitay et al.³⁵ (blue line with circles) and Mitchell³⁴ (green line with diamonds). The rate constant calculated at $T = 120$ K electron temperature by Takagi et al.³¹ with a different MQDT approach is given in the orange square.

fitting parameter $a_0 = 1.559 \times 10^{-16} \text{ cm}^2 \cdot \text{eV}$. The second is the experimental recommendation of Mitchell³⁴ (green line with diamonds).

The theoretical thermal average at 300 K is significantly lower, but the agreement with Amitay et al.³⁵ is within a factor of 2 up to ~ 1000 K. One should notice that the variation of the DR rate coefficients is not monotonic with N_i^+ ; i.e., there is no particular trend with increasing N_i^+ . Their dependence on the rotational excitation of the target ion is weak, and all the initial-state-specific rates agree to within a factor of 2. Here, the DR Maxwell rate coefficients computed for the lowest 11 rotational levels of the ground vibrational level are compared with two non-rotational cases and the averaged rate 300 K. Figure 4 shows stronger dependence on the initial rotational levels of the molecular cation for temperatures up to 200 K. In this region one can observe the largest differences between the averaged and non-rotational with ground core only rates. The second set of non-rotational rates (three ionic cores) are very convincing on the minor importance on the rotational effects for this particular molecular cation. Above this temperature, the rotational effect is even less pronounced; the non-rotational rate coefficient (one core only) and that one averaged at 300 K are on top of each other. This is partially due to the peculiar behavior of the rate coefficient belonging to the $N_i^+ = 3$ rotational state.

The best agreement between the non-rotational MQDT calculations for three cores and the thermally convoluted experimental results of Amitay et al.³⁵ is achieved for temperatures higher than 600 K, although the comparison with the anisotropic Maxwell rate coefficients shows only qualitative agreement. This very good agreement lasts up to 2800 K and frames the region where the excited core effects are really important.

3.1.2. CO^+ . The carbon monoxide ion CO^+ is one of the most abundant ions detected in the interstellar medium,³⁸ in the coma, and in the tail region of comets and is of key relevance for the Martian atmosphere.³⁹ It has been detected by several spacecraft missions to different comets and is

thought to be formed by photo-ionization and electron-impact ionization of CO and CO_2 molecules.⁴⁰

The high density of electrons and molecular ions in the cometary coma and some parts of ISM facilitates dissociative recombination. Moreover, this process plays an important role in producing numerous carbon and oxygen atoms in metastable states.

The first experimental results on the dissociative recombination of carbon monoxide was obtained in the late 1960s by Mentzoni and Donohoe⁴¹ in a dc discharge afterglow measurement. This was followed by the merged-beam experiment of Mitchell and Hus⁴² in 1985 and by the flowing afterglow experiment of Geoghegan et al.⁴³ in 1991. The most recent and complete experimental results were obtained by Rosen et al.⁴⁴ on the CRYRING storage-ring equipment. The first and pioneering theoretical study providing rate coefficients was done by Guberman⁴⁵ in 2007 that was followed in 2013 by an updated quantum chemistry calculation⁴⁶ providing the most relevant molecular states for DR of CO^+ .

By using the R-matrix-based calculations of Chakrabarti and Tennyson^{47,48} completed by other ab initio quantum chemistry calculations,^{49,50} we have managed to set up a molecular data set containing the three most important symmetries contributing to DR and its competitive processes, namely, the $^1\Sigma^+$, $^1\Pi$, and $^3\Pi$ ones, and considering four dissociative states for each symmetry. The calculations were performed using MQDT version b. For each available dissociative channel, we have considered its interaction with the most relevant series of Rydberg states, that is, s, p, d, and f, for the $^1\Sigma^+$ symmetry and s, p, and d for the $^1\Pi$ and $^3\Pi$ symmetries.

The DR cross-sections are displayed in Figure 5.^{11,13} They are characterized by resonance structures due to the temporary captures into vibrational levels of Rydberg states embedded in the ionization continuum (closed channels and indirect process), superimposed on a smooth background originating in the direct process.

The ionization thresholds (vibrational levels of the molecular ion) shown as dotted vertical lines in Figure 5 act as accumulation points for these Rydberg resonances. Moreover, the asymptotic limits of the dissociation channels opening progressively are shown with shorter dark-green vertical lines, corresponding to the atomic pairs of states $\text{C}(^1\text{D}) + \text{O}(^1\text{D})$, $\text{C}(^3\text{P}) + \text{O}(^1\text{S})$, $\text{C}(^1\text{S}) + \text{O}(^1\text{D})$, and $\text{C}(^1\text{D}) + \text{O}(^1\text{S})$. We notice that the $\text{C}(^3\text{P}) + \text{O}(^3\text{P})$ and $\text{C}(^1\text{D}) + \text{O}(^3\text{P})$ limits are open at zero collision energy.

The DR of CO^+ vibrationally relaxed (top panel of Figure 5) is by far dominant: it is about four times larger below 700 meV and above 2 eV, while in-between, the maximum deviation among all of the cross-sections is smaller than a factor of 2. At low energy, one can observe a systematic decrease of the total cross-section, except for $v_i^+ = 5$ (bottom panel of the same figure). In this latter case, the PECs of the two open valence states of $^1\Sigma^+$ symmetry have favorable crossings with the ion PEC—symmetry with the largest valence—Rydberg electronic couplings (see Figure 2 from¹¹)—leading to an increase of the cross-section.

Another interesting feature is the revival of the cross-section at high energy, due to the opening of dissociation states.

In spite of the overall factor 2 between our MQDT calculated rate coefficients and all experimental results (except the higher placed rates of Mentzoni and Donohoe due to the presence of CO clusters), the *shape* agreement achieved over a

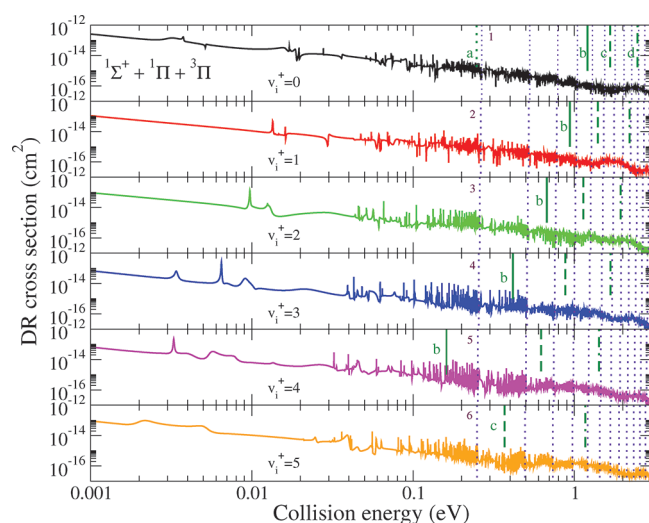


Figure 5. Dissociative recombination of CO^+ on its lowest six vibrational levels ($v_i^+ = 0, 1, 2, 3, 4$, and 5): cross-sections summed-up over all of the relevant symmetries (see ref 11). The dotted vertical indigo lines are the different ionization thresholds, given by the vibrational levels of the molecular ion. The first ionization thresholds are indicated on the figure. The dark-green shorter vertical lines stand for the different dissociation limits measured from the initial vibrational levels of the ion, as follows: the dotted line (a) stands for the $\text{C}(^1\text{D}) + \text{O}(^1\text{D})$ limit, the solid lines (b) for the $\text{C}(^3\text{P}) + \text{O}(^1\text{S})$ one, the dashed lines (c) for $\text{C}(^1\text{S}) + \text{O}(^1\text{D})$, and the dashed-dotted lines (d) for $\text{C}(^1\text{D}) + \text{O}(^1\text{S})$. Reproduced with permission from ref 13. Copyright 2018 ESO Sciences.

significant range of energies and temperatures, illustrated in Figure 6, but also, in more detail, in Figures 4–6 from ref 11, is satisfactory for this diatomic system with many electrons.

3.1.3. CF^+ . Whereas the DR of fluorine-containing molecular cations controls the ionization state and the chemical composition of many plasmas used in electronic process-

ing,^{51–55} it also does, especially in the case of CF^+ , for the fluorine chemistry in the cold interstellar medium.^{56,57}

Very little has been done regarding the quantum chemistry of the superexcited states of CF and the DR CF^+ . The relevant molecular PECs and electronic couplings, shown in Figures 4 and 5 in ref 8, have been calculated by the complex Kohn variational method.¹⁸ The molecular data set contained one ion core and one dissociative molecular state for each of the three $^2\Sigma$, $^2\Pi$, and $^2\Delta$ symmetries. The MQDT calculations—using approach b⁸—were performed without including the Rydberg bound states responsible for the indirect process. The results were compared with measurements performed on the Test Storage Ring (TSR), Heidelberg.

The anisotropic Maxwell rate coefficients for both experiments and theory are reported on Figure 7. The agreement is

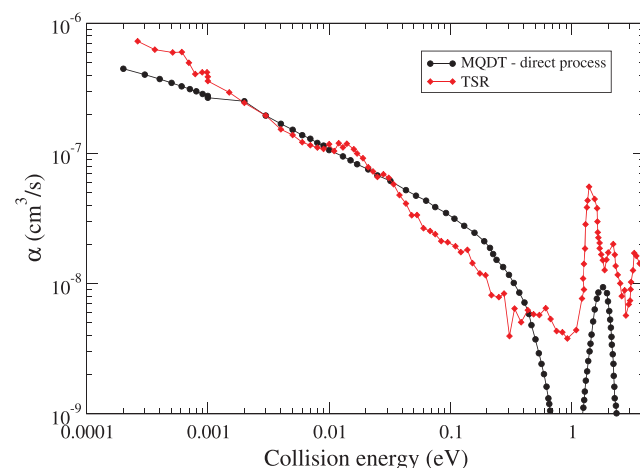


Figure 7. DR anisotropic rate coefficients for the vibrationally relaxed ($v_i^+ = 0$) CF^+ molecular ion compared to TSR experiment.⁸ Reproduced with permission from ref 8. Copyright 2009 IOP Science.

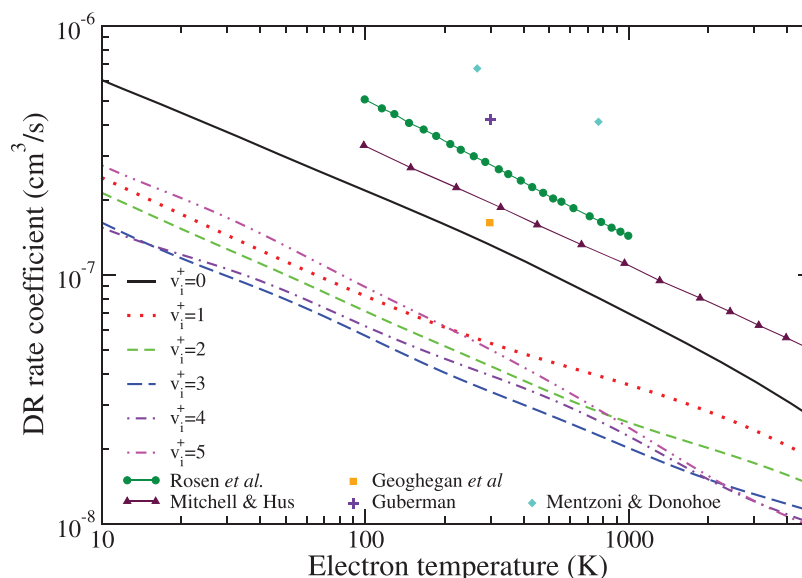


Figure 6. Dissociative recombination of CO^+ on its lowest six vibrational levels ($v_i^+ = 0, 1, 2, 3, 4$, and 5): Maxwell rate coefficients summed-up over all of the relevant symmetries, colored lines with different line styles (see refs 11 and 13). The green line and full circles are the experimental data measured on CRYRING, Stockholm,⁴⁴ the maroon line and triangles are the estimates provided by Mitchell and Hus,⁴² the turquoise diamonds are the measurements of Mentzoni and Donohoe,⁴¹ the orange square is the experimental rate of Geoghegan et al.,⁴³ and finally the indigo cross is the theoretical estimate of Guberman.⁴⁵

very good up to an electron energy close to 1 eV. At higher energies the discrepancies observed can be accounted for the indirect mechanism, for the higher dissociative and/or excited ion curves that have not been considered in the present treatment. The very good agreement is even more visible for the isotropic rate coefficients presented in Figure 8.

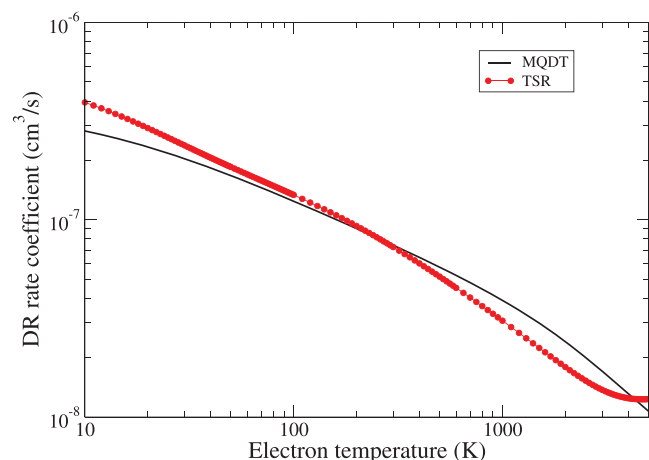


Figure 8. DR Maxwell isotropic rate coefficients for the vibrationally relaxed ($v_i^+ = 0$) CF^+ molecular ion compared to TSR experiment.⁸

3.2. Numerical Details. The key numerical parameter determining the memory used and the running time is the dimension of the matrices involved in computation: the interaction matrix \mathbf{V} , (eqs 7, 13, and 16), the reaction matrix \mathbf{K} (eq 8), the generalized scattering matrix \mathbf{X} (eq 9), and the physical scattering matrix \mathbf{S} (eq 10). The dimensions of the matrices are given by the number of reaction channels—dissociation channels and ionization ones. For example, for the DR of CO^+ (see above), for a given electronic symmetry (from the three relevant ones) of the CO system, we considered 212 ionization channels, associated, each of them, to one of the 53 vibrational levels of the ion and to one of the 4 partial waves of the incident electron.

Another key parameter is the dimension of the grid of energies of the incident electrons. Using the same example of the DR of CO^+ , in order to take into account the indirect process characterized by fine Rydberg resonances, we had to use a step of 10^{-2} meV, which, for an incident electron energy up to 0.5 eV, implies 50,000 energy points.

These features correspond in average to runs on a “standard” desktop computer (Xeon CPU with 6 cores) taking between 1 and 2 weeks for each initial vibrational level of the target ion. We expect improvement in the overall running time following parallelization of the numerical routines/methods over the energy-grid points.

4. POLYATOMIC MOLECULES

4.1. Vibrational Dynamics in DR of Polyatomic Molecules. The multidimensional nature of vibrational motion of polyatomic ions makes the theoretical study of the dissociative recombination and rovibrational excitation of such ions much more difficult^{58–61} compared to the case of diatomic ions discussed above. Once the electron is captured, the complexity of the dissociation processes increases not only with the multidimensional vibrational and dissociative dynamics but also with the symmetry of the neutral

system.^{58,59,62,63} In particular, this complexity applies to the spectacular role of the indirect process, already discussed and illustrated in the diatomic case, especially for the CH^+ DR. For polyatomic ions with high symmetry, such as linear ions^{64,65} or ions having three or more identical nuclei,^{62,63} the non-Born–Oppenheimer coupling between the incident electron and the rovibrational degrees of freedom could be nontrivial^{58,59,64–66} and special attention should be given to the construction of the reaction and scattering matrices. However, the main ideas of the MQDT approach described above for the diatomic ions can be applied to polyatomic ions as long as the symmetry of the total system is accounted for in modeling the non-Born–Oppenheimer coupling, which is responsible for VE and DR processes.

Over the recent years, three major approaches were developed to account for vibrational dynamics of the target polyatomic ion and the neutral molecule formed after the recombination step in the DR process.

The simplest approach is based on the idea that, for certain ions, only one vibrational degree of freedom is responsible for the dynamics.^{67,68} Whenever this approximation is reasonable, one can apply almost all techniques developed for diatomic ions.

The second approach was initially developed for the DR and VE treatment of the H_3^+ ion, and it uses the properties of the hyperspherical coordinates.^{58,59,66,69,70} This approach is very useful for systems with only a few (2–3) vibrational degrees of freedom that should be taken into account explicitly. The idea of the approach can be summarized as follows. The coordinate system is made out of all vibrational degrees of freedom and consists of a hyperradius, ρ , and a set of hyperangles, Ω . By the construction, the hyper-radius describes uniformly all dissociation channels and, therefore, can be viewed as a generalized dissociation coordinate. One can think of the hyper-radius as being related to the size of the molecular system, whereas the hyperangles, related to its shape. Once the coordinate system is set, the ionic target vibrational Hamiltonian is diagonalized in the hyperangles space for several values of ρ yielding eigenvalues that represent the hyperspherical adiabatic potential energies, $U_a(\rho)$, of the ion with $a = 1, 2, \dots$ labeling the different eigenvalues. With the potential energies in hand, the DR and VE of the polyatomic ion can be considered using all of the techniques developed for diatomic ions by replacing the interatomic distance, R , with the hyper-radius. The main difference is a much larger number of (hyperspherical adiabatic) channels compared to a typical situation of diatomic ions where only one or a few electronic channels of the target are taken into account as, for example, demonstrated above for the CH^+ ion.

The third approach is based on the normal-mode approximation for the vibrational manifold,^{71–74} which usually provides a good description of the vibrational dynamics of molecular systems near the equilibrium geometry. Because, in general, normal coordinates are easy to determine for small polyatomic ions, they are perfectly suitable for determination of rovibrational excitation cross-sections. However, due to their lack of dissociation limit, they cannot represent the dissociative dynamics that are needed to treat the DR process. Thus, additional steps are needed if one wants to use normal modes to treat the vibrational dynamics of DR, and they are described below.

4.1.1. Normal-Mode Approach for DR and VE. If one is interested in thermal rate coefficients or cross-sections with a

relatively low energy resolution, one important observation is that resonances associated with closed rotational or vibrational channels are smeared out. In fact, at present, the highest resolution achieved in storage-ring experiments measuring DR cross-sections is a few cm^{-1} . Then, one has to add to this uncertainty a different one associated with the toroidal sections of the storage-ring or merged-beam setups, where relative velocities of ions and electrons are not perfectly matched. In this situation, the energy splitting between two Rydberg resonances, which represent closed vibrational channels for autoionization and increase the probability for dissociation in the DR process, is smaller than the experimental resolution. It is therefore reasonable to evaluate the DR cross-sections averaged over the energy splitting as it is made by Mikhailov et al.⁶⁴ Such a DR cross-section averaged over the energy interval between three consecutive auto-ionizing vibrational resonances, having energies ϵ_{n-1} , ϵ_n , and ϵ_{n+1} and responsible for a temporary capture of the electron by the target ion, is

$$\langle \sigma(E_{\text{el}}) \rangle = \frac{1}{\Delta_n + \Delta_{n+1}} \int_{\epsilon_n - \Delta_n}^{\epsilon_n + \Delta_{n+1}} \sigma(E') dE',$$

$$\Delta_{n+1} = \frac{\epsilon_{n+1} - \epsilon_n}{2} \quad (17)$$

As shown in ref 64, if auto-ionization lifetimes of the resonances are large compared to their predissociation lifetimes, the averaging procedure gives the following expression for the DR cross-section

$$\sigma(E_{\text{el}}) = \frac{2a_0\pi^2}{e^2k^2} \Gamma_\nu \nu^3 \quad (18)$$

where $E_{\text{el}} = (\hbar k)^2/(2m_e)$, k , e , and m_e are the kinetic energy, wavenumber, charge, and mass of the incident electron, respectively, a_0 is the Bohr radius, Γ_ν is the width of the resonance produced by the closed vibrational channel ν of the ion, and ν is the effective quantum number of the resonance with respect to the closed channel.

Provided that one neglects the presence of perturbing resonances associated with other vibrational or electronic channels, the widths Γ_ν scale with the effective quantum number of the Rydberg electron, ν , as $1/\nu^3$, and therefore the product $\Gamma_\nu \nu^3$ is energy-independent. As shown in refs 64, 70, and 75, the product $\Gamma_\nu \nu^3$ is related to nondiagonal matrix elements of the reactance $\langle \nu, \Lambda | \hat{K} | \nu', \Lambda' \rangle$ or scattering $\langle \nu, \Lambda | \hat{S} | \nu', \Lambda' \rangle$ matrices, where the indices ν', Λ' refer to the initial vibrational and electronic states of the target ion and the indices ν, Λ correspond to the vibrational and electronic states producing the Rydberg series of resonances Γ_ν . Expressed in terms of the scattering-matrix element, the averaged cross-section can be written as^{70,75}

$$\sigma = \frac{\pi}{k^2} |\langle \nu, \Lambda | \hat{S} | \nu', \Lambda' \rangle|^2 \quad (19)$$

The scattering-matrix element is computed as the integral⁷⁶

$$\langle \nu, \Lambda | \hat{S} | \nu', \Lambda' \rangle = \int dQ \langle \nu | Q \rangle S_{\Lambda, \Lambda'}(Q) \langle Q | \nu' \rangle \quad (20)$$

in which the symbol Q refers collectively to all normal coordinates labeled as q_i ($Q = \{q_1, q_2, \dots\}$), describing the vibration of the ion. Using the relationship between the scattering matrix \hat{S} and the quantum defect matrix $\hat{\mu}$, $\hat{S} =$

$\exp(2\pi i \hat{\mu})$, and expanding $\mu_{\Lambda, \Lambda'}(Q)$ in a Taylor series around the equilibrium configuration Q_0 of the ion

$$\mu_{\Lambda, \Lambda'}(Q) = \mu_{\Lambda, \Lambda'}(Q_0) + \sum_i \frac{\partial \mu_{\Lambda, \Lambda'}}{\partial q_i} q_i + \dots \quad (21)$$

allows one to express analytically the matrix element of the quantum defect as long as the derivatives in eq 21 are known.

It is convenient to use dimensionless coordinates q_1, q_2, \dots , which are related to the length-unit normal coordinates S_1, S_2, \dots , as $q_i = S_i \sqrt{\mu_{\text{red}} \omega / \hbar}$, where μ_{red} and ω are the reduced mass and the frequency of the normal mode.⁷⁷ Assuming that the ion is initially in its ground vibrational state $|\nu'\rangle = |0\rangle$ and retaining only zero- and first-order terms in the above expansion, eq 19 takes the form⁷⁸

$$\sigma_i(E_{\text{el}}) = \frac{4\pi^3}{k^2} \left(\frac{\partial \mu_{\Lambda, \Lambda'}}{\partial q_i} \right)^2 |\langle \nu_i | \hat{q}_i | 0 \rangle|^2 \quad (22)$$

The index i in ν_i and σ_i is used to stress that the capture occurs into the q_i vibrational mode excited by one vibrational quantum ν_i . It is more convenient to use the effective quantum numbers $\nu(Q) = n - \mu(Q)$, where n is the principal quantum number, rather than quantum defects. In the harmonic oscillator approximation, the matrix element $\langle \nu_i | \hat{q}_i | 0 \rangle = \delta_{\nu_i, 1} / \sqrt{2}$. This gives

$$\sigma_i(E_{\text{el}}) = \frac{2\pi^3}{k^2} \left(\frac{\partial \mu_{\Lambda, \Lambda'}}{\partial q_i} \right)^2 \theta(\hbar \omega_i - E_{\text{el}}) g \delta_{\nu_i, 1} \quad (23)$$

In the above equation the spin degeneracy factor g is explicitly specified.

The equation above describes in fact the process of electron capture into vibrational resonances associated with closed vibrational levels. It gives the DR cross-section only if the auto-ionization lifetime of these resonances is much larger than the dissociation lifetime, which has been verified for the DR process of H_3^+ .⁷⁹ This assumption is believed to be valid also for other polyatomic molecules because the neutral molecule formed after the electron capture goes quickly to geometries in which auto-ionization is forbidden due to the repulsive character of the potential energy surfaces of the neutral molecule near the geometry of equilibrium of the ion.

Due to the procedure of averaging over the interval of electron energies corresponding to the energy splitting between vibrational auto-ionizing resonances, discussed above, the theoretical DR cross-section at low energies is featureless and behaves simply as $1/E_{\text{el}}$. Due to a relatively low resolution in all DR experiments with polyatomic ions, except a few experiments with H_3^+ , the experimental resolution is too low to resolve individual Rydberg resonances in the DR spectra. Therefore, the averaging procedure is justified. The interval of applicability of the procedure is determined by the approximation of the energy independence of the product $\Gamma_\nu \nu^3$ in eq 18. The product varies to the same degree as the strongest couplings between different partial waves in the scattering matrix. In the absence of electronic resonances in the spectra (such resonances can influence the process for closed-shell ions at relatively high energies, above a few eV), such a variation is weak and can be neglected for the interval of electron energies up to 1 eV. The uncertainty introduced by the averaging procedure is significantly smaller than the

uncertainty due to the quantum defect approach discussed in this section.

In order to apply eq 23, one should know the behavior of the coupling elements in the matrix $\hat{\nu}$ of the principal quantum number. In practice, the principal quantum numbers are obtained in bound-state calculations of highly excited electronic Rydberg states. The principal quantum numbers obtained in this way correspond to eigenvalues of the matrix $\hat{\nu}$; i.e., they do not provide the information about the couplings between closed electronic states. In order to obtain the couplings, model Hamiltonians are developed for different types of the molecular ions. The form of a particular model Hamiltonian depends on the symmetry of the ion. On the basis of the model Hamiltonian, a model for the matrix of principal quantum number is obtained and its elements $\nu_{\Lambda,\Lambda'}$ are computed fitting the eigenvalues of the matrix evaluated in bound-state calculations to the model matrix. This approach was used in several studies.^{63–65,75,80} For example, for the H_3O^+ and CH_3^+ ions, the model Hamiltonian is constructed⁶³ taking into account the Jahn–Teller coupling between degenerate electronic states and vibrational modes. On the basis of the model Hamiltonian, the model matrix of principal quantum number for H_3O^+ has the following form

$$\hat{\nu}(\rho, \varphi) = \begin{pmatrix} \nu_e^{(0)} & \kappa_{ea_1} \rho e^{i\varphi} & \kappa_{ee} \rho e^{-i\varphi} \\ \kappa_{ea_1} \rho e^{-i\varphi} & \nu_{a_1}^{(0)} & \kappa_{ea_1} \rho e^{i\varphi} \\ \kappa_{ee} \rho e^{i\varphi} & \kappa_{ea_1} \rho e^{-i\varphi} & \nu_e^{(0)} \end{pmatrix} \quad (24)$$

in the basis of three electronic states taken into account: an a_1 and the doubly degenerate e states. The coordinates ρ and φ are polar versions of the x and y components of the q_2 or q_4 degenerate modes of the ion. The parameters κ_{ee} and κ_{ea_1} are real and ρ - and φ -independent and obtained by a fit to the ab initio results: The eigenvalues of the above matrix should be equal to the values obtained from ab initio bound-state energies. More details about the construction of the matrix (eq 24) can be found in ref 63.

Figures 9 and 10 show the DR cross-sections for the H_3O^+ and CH_3^+ ions obtained using the approach described above. The theoretical cross-sections agree well with the experimental data from the storage-ring experiments. A more detailed discussion of the theoretical approach and the comparison with the experiment can be found in ref 63.

4.2. Beyond Quantum Defect Approach. The theoretical approach described above requires couplings in the matrices of quantum defect or principal quantum number. The couplings are evaluated assuming a model for the Hamiltonian of interaction between electronic and vibrational degrees of freedom of the ion + electron system. The approach was successful for C_{3v} , D_{3h} , and T_d ⁶² molecular ions, where the Jahn–Teller coupling has the largest contribution to the DR and vibrational excitation cross-section. This means that the model Hamiltonian and, correspondingly, the model couplings in the matrix of eq 24 are able to represent entirely the major physics of the DR and of the VE processes.

Trying to apply similar ideas to other types of polyatomic ions, such as linear ions of the $\text{C}_{\infty v}$ symmetry group, was not as successful as it was for the C_{3v} , D_{3h} , and T_d ions. Initially, it was suggested that the Renner–Teller coupling could be the main mechanism for the DR process in the $\text{C}_{\infty v}$ ions. The idea was developed^{64,65,75} on the example of the HCO^+ ion. The model

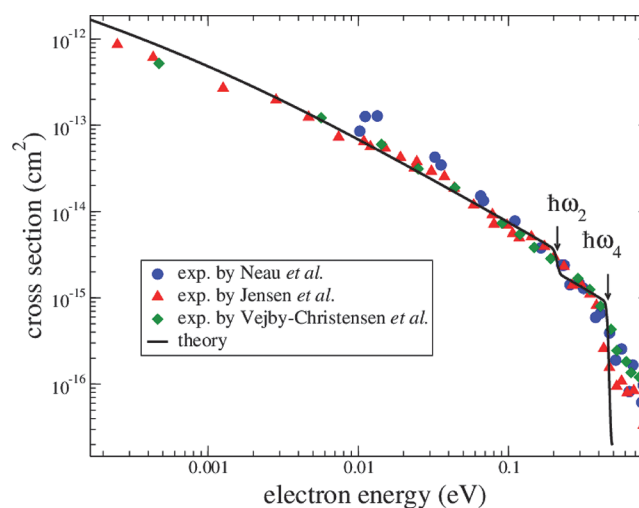


Figure 9. Comparison of theoretical⁶³ and experimental^{81–83} cross-sections for DR of H_3O^+ . The experimental data are obtained in the ASTRID/CRYRING storage rings, the theoretical cross-section is obtained using eqs 23 and 24 and applying a convolution with the experimental distribution over collision energies. The arrows indicate energies of excitation of a quantum of the q_2 and q_4 degenerate modes. Reproduced with permission from ref 63. Copyright 2012 American Physical Society.

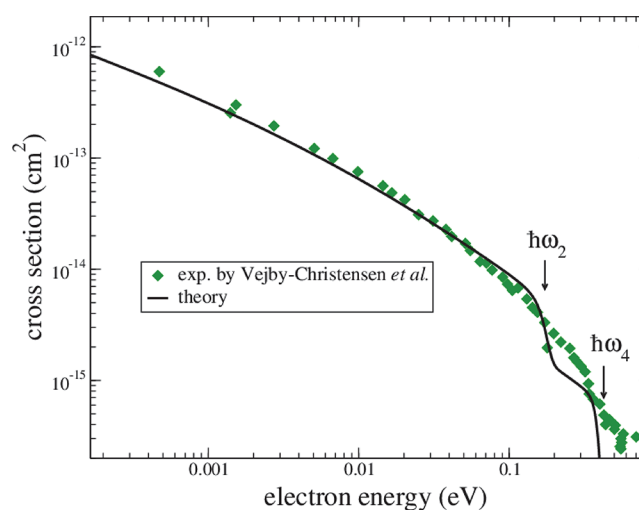


Figure 10. Same as Figure 9, but for the DR in CH_3^+ , theory⁶³ and experiment.⁸¹

Hamiltonian and the couplings in the matrix of principal quantum number were obtained on the basis of the Renner–Teller coupling mechanism. However, the obtained theoretical DR cross-section was significantly smaller, by a factor of 2–10, than all available experimental data. In addition, the fitting procedure of bound-state energies to the model matrix of quantum defects is not unique. After many efforts it was concluded that the Renner–Teller interaction is not the only one that contributes to the DR process. The vibronic coupling between electronic states, other than that involved in the Renner–Teller interaction, should be accounted for to describe the DR process in linear ions.

The difficulties with the above theoretical approach and the availability of electron-scattering codes suggested that one can use the results of electron-scattering calculations directly, without employing model Hamiltonians and quantum defect

coupling models: Instead of computing energies of excited electronic states of the neutral molecule, one can simply use scattering or reaction matrices obtained from electron-scattering codes, such as the UK R-matrix¹⁷ or the complex Kohn method.^{84,85} Therefore, if one expands the scattering matrix in eq 20 in a way similar to eq 21, one obtains for the DR cross-section

$$\sigma^{\text{DR}}(E_{\text{el}}) = \frac{\pi \hbar^2}{4m_e E_{\text{el}}} \sum_i g_i \sum_{l, \lambda, l', \lambda'} \left| \frac{\partial S_{l, l', \lambda, \lambda'}}{\partial q_i} \right|^2 \theta(\hbar \omega_i - E_{\text{el}}) \quad (25)$$

Here i runs over all modes of the target molecules, g_i is the degeneracy factor for the mode i , and l, λ and l', λ' are the indices of the partial waves and their projections on a chosen quantization axis in the molecular reference frame. The above formula gives the DR cross-section assuming that the target ion is on its ground vibrational level.

The cross-section for vibrational excitation of the mode i from $v_i = 0$ to $v_i = 1$ is^{86,87}

$$\sigma_i^{\text{VE}}(E_{\text{el}}) = \frac{\pi \hbar^2}{4m_e E_{\text{el}}} g_i \sum_{l, \lambda, l', \lambda'} \left| \frac{\partial S_{l, l', \lambda, \lambda'}}{\partial q_i} \right|^2 \theta(E_{\text{el}} - \hbar \omega_i) \quad (26)$$

In practice,^{55,86,87} if one uses the UK R-matrices codes,¹⁷ the scattering matrix should be obtained from the reactance matrix \hat{K} as

$$\hat{S} = \frac{\hat{1} + i\hat{K}}{\hat{1} - i\hat{K}} \quad (27)$$

where $\hat{1}$ is the identity matrix, and it has to be computed for two values only of each normal coordinates q_i , such that the derivative $\partial S_{l, l', \lambda, \lambda'} / \partial q_i$ of the scattering matrix with respect to the normal coordinate q_i could be computed by the simple finite-difference formula. When the complex Kohn method is employed,⁷⁰ electron-scattering calculations produce directly the matrix \hat{S} and, therefore, the step of eq 27 is not needed.

Figure 11 compares the available experimental data from two experiments with theoretical results obtained using the quantum defect approach and explicit scattering calculations. The data from the two experiments differ quite significantly at low electron energies. As discussed in ref 70, in the storage-ring experiment, the two stable isomers of HCO^+ (HCO^+ and HOC^+) could be present. The theoretical DR cross-section for HOC^+ is significantly larger than the one for HCO^+ .⁷⁰ Therefore, the differences in the experimental data^{88,89} could be explained by a larger fraction of HOC^+ in the CRYRING storage ring⁸⁹ compared to the merged-beam experiment.⁸⁸ The merged-beam cross-section agrees quite well with the pure- HCO^+ theoretical result, and the storage-ring data⁸⁹ could be reproduced in calculations if one assumes that some fraction of ions in the experiment is the form of the HOC^+ isomer, which might mean that in the CRYRING experiment the two isomers are present. The cross-section obtained using the quantum defect approach, shown with green⁶⁴ and dashed black⁶⁵ curves in the figure, underestimate the DR cross-section. As discussed in ref 70, this is due to the vibronic coupling between symmetric and asymmetric stretching modes neglected in the quantum defect approach used in previous theoretical studies.^{64,65}

The only COM target ever involved in a DR and VE theoretical study published so far is CH_2NH_2^+ .⁸⁷ This cation

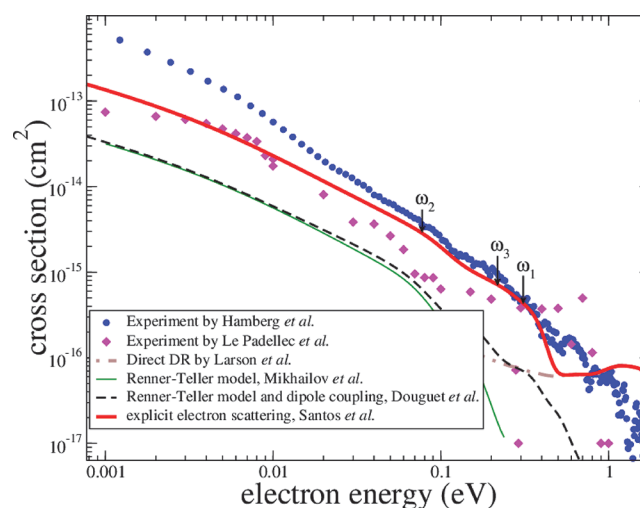


Figure 11. Comparison of different theoretical and experimental DR cross-sections for HCO^+ . The red solid line is the theoretical result⁷⁰ obtained using eq 25. The theoretical results obtained using the model Renner–Teller Hamiltonian and the approach based on quantum defects (discussed above) are shown with green⁶⁴ and dashed black⁶⁵ curves. The experimental results from a merged-beam experiment⁸⁸ and CRYRING storage ring⁸⁹ are shown by purple and blue dots, respectively. The first vibrational thresholds of each normal mode of HCO^+ are indicated by arrows.

can act as a precursor of simple amino acids. We have applied the approach discussed above to this ion. Figure 12 shows the

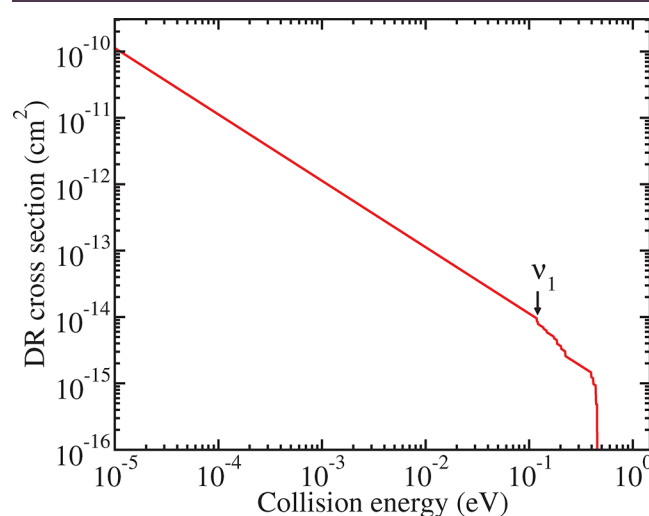


Figure 12. Dissociative recombination of ground-state CH_2NH_2^+ cross-section. Reproduced with permission from ref 87. Copyright 2019 The Author(s) Published by Oxford University Press on behalf of the Royal Astronomical Society.

DR cross-section for the target in its vibrationally ground state as a function of collision energy. For energies higher than 0.1 eV, the cross-section drops in a stepwise manner because the scattering electron excites the vibrational level of the ionic target by one quanta.

Figure 13 displays the thermally averaged VE and DR rate coefficients vs the electron temperature for all of the normal-mode frequencies. For $T < 400$ K, the DR and VE rate coefficient goes as $(k_b T)^{-1/2}$ and $(k_b T)^{-1/2} \exp(-\hbar \omega_i / k_b T)$, respectively. At higher temperature, as vibrational excitation is

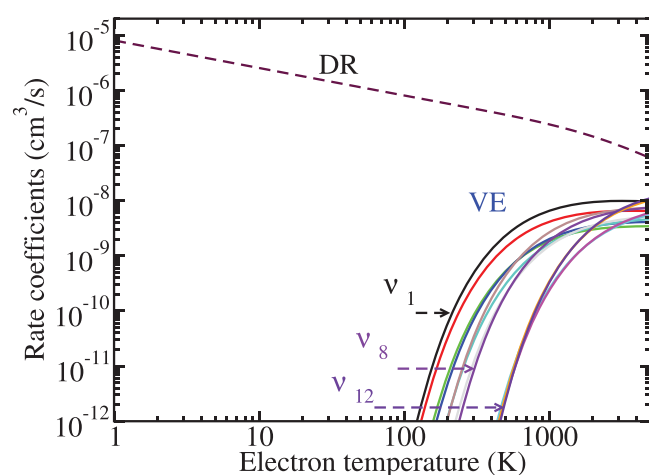


Figure 13. Dissociative recombination (DR, dashed line) and vibrational excitation (VE, solid lines) of CH_2NH_2^+ in its ground state. VE rate coefficients are arranged from low to high frequencies. The vibrational modes 1, 8, and 12 are indicated with arrows for visual guidance. Reproduced with permission from ref 87. Copyright 2019 The Author(s) Published by Oxford University Press on behalf of the Royal Astronomical Society.

more probable, the DR rate coefficient decreases faster than $(k_b T)^{-1/2}$.

To the best of our knowledge, there are no experimental data, cross-sections or rate coefficients, on DR or VE processes in electron– CH_2NH_2^+ collisions. It would be desirable if, for example, DR rate coefficients are measured in storage-ring or merged-beam experiments. Such a measurement would help to validate the applicability of the presented theoretical approach for ions with more than 4 atoms.

5. CONCLUSIONS

The multichannel quantum defect theory allows the realistic modeling of the reactive collisions between electrons and molecular cations, provided that the molecular structure of the target and of the neutral complex has been explored and quantitatively characterized by quantum chemistry and R-matrix methods.

High accuracy has been achieved for some of the diatomic species, and the progressive account of the numerous mechanisms, and interactions—Rydberg–valence and Rydberg–Rydberg couplings and rotational and core-excited effects—results in theoretical cross-sections and rate coefficients in increasing agreement with the measurements in storage rings. However, so far, with the exception of rough estimations for CO^+ ,^{11,13} we did not produce branching ratios for the systems studied in this work. The major reason for this is the lack of data for the interactions at large internuclear distances, which may change the dissociation dynamics with respect to the tendencies induced at small distances. This important issue is the subject of further studies.

As for the polyatomic ions, we stress that after several iterations and several years of development, a reliable and relatively simple theoretical approach was developed to study the dissociative recombination and rovibrational excitation of small molecular ions having a closed electronic shell. The method is based on explicit electron–molecule scattering calculations, which could be performed using different existing codes and methods. The approach was successfully applied for a variety of molecular ions, the largest ones so far being CH_2

NH_2^{+87} and $\text{NH}_2\text{CH}_2\text{O}^+{}^{90}$. The theoretical studies of the DR process in the CH_2NH_2^+ and $\text{NH}_2\text{CH}_2\text{O}^+$ ions and their importance in the chain of prebiotic reactions in the interstellar clouds invite experimentalists to perform measurements of the DR rate coefficients. Such experimental measurement will validate the theoretical approach or will prompt a development of a better theoretical method for middle-size polyatomic ions.

These developments will contribute in the near future to a better understanding of the role of the collisions of electrons with molecular cations in the formation of the complex organic molecules.

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