



## ACCELERATING TRANSIENT DYNAMICS: TARGETED MODAL INTERACTION

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### Abstract

Vibrations occur in many areas ranging from heavy-duty industry over micro sensors to appliances in the private household. A key concept for limiting such vibrations is vibration control that avoids or at least minimize unintentional product behavior or negative effects on the health and safety of humans and animals. A concept for attacking vibrations in mechanical systems is outlined based on time-periodic modulation of a physical parameter in the system. This concept can be applied in parallel to existing controls and allows the artificial increase of damping transient dynamics.

### Keywords

vibration control, parametric anti-resonance

### 1. Introduction

Vibrations occur in many areas ranging from heavy-duty industry over micro sensors and production machines to appliances in the private household. A key concept for limiting such vibrations is vibration control that avoids or at least minimize unintentional product behavior or negative effects on the health and safety of humans and animals, see (ISO 5349-1). For example, the whole-body vibrations in agricultural track-laying tractors may affect the operator's health and work efficiency [1-2]. Another example is the generation of electrical energy in heavy-duty power plants [3]. The efficiency with which such power plants translate gas/oil to electrical energy depends strongly on the gap between blades and casing. This

gap needs to be large enough for allowing transient operation of the power plant due to steadily changing power needs but small enough for ensuring a cost-effective and efficient operation. A further example are wind turbine blades in the so-called green industry [3-4]. The trend towards longer blades makes wind turbines prone to wind-induced vibrations that may limit the turning speed or reduce the lifetime of the blade material. A modern concept for attacking vibrations in mechanical systems is outlined that can be used in parallel to existing controls and allows the artificial increase of damping transient dynamics [4].

Introducing a time-periodic modulation of a system parameter may trigger an energy transfer between vibration modes [5]. If this energy transfer induces a vibration reduction the associated modulation frequency is called parametric anti-resonance frequency. For a system with multiple natural frequencies, the simplest parametric anti-resonance may occur at the sum or difference between two of the many natural frequencies

$$\nu = \frac{|\omega_i \mp \omega_j|}{n} \quad i, j, n = 1, 2, \dots \quad (1)$$

The main benefit is outlined in Fig. 1 for the example of a linear, unstable system. The original system possess some unstable and stable poles. Additional poles may be located on the left half-plane. Introducing a time-periodic modulation of a physical parameter in the system, for example modulating the original stiffness  $k$ , leads to the time-periodic stiffness  $k(t)$ . Tuning the modulation close to a parametric anti-resonance frequency induces a modal interaction between the original system modes and allows for an energy transfer between these two

vibration states of the system. This is a selective, externally triggered energy transfer. Translated to the complex plane in Fig. 1, the original system poles move with respect to the real parts towards a fix point, which eventually results in a stable system. The

concept goes back to the pioneering idea of Tondl (1978) [6] and was verified theoretically and experimentally for different test rigs with flexible structures [7].

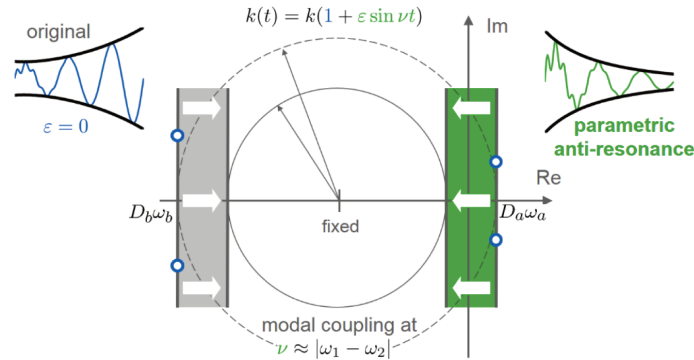


Figure 1. Movement of the system poles at induced modal interaction: The original system poles of the unstable system with constant stiffness  $k$  (left) move with respect to the real parts towards a fix point if an intentional modal interaction is triggered by  $k(t)$  which results in a stable system at parametric anti-resonance (right).

### Potential applications

The strength of this concept is that it is applicable in parallel to already existing control concept. Some potential areas for different mechanical systems are outlined in the following. The first experimental verification was performed by Tondl using an analog electronic circuit. This work motivated analytical, numerical and experimental work on systems utilizing a parametric anti-resonance [7-8]. A test rigs of flexible structure is shown exemplary in Fig. 2: an uniaxial electromagnetic actuator used as a time-modulated support of a flexible cantilever. The effective damping observed during transient

dynamics of the cantilever are collected at different modulation frequencies  $\nu$ . It is clearly shown that if the modulation frequency hits a parametric resonance frequency, the effective damping is decreased and the system response may become unstable. However, tuning the modulation frequency  $\nu$  close to a parametric anti-resonance frequency as defined in eq. (1), triggers a significant increase of the effective damping. A comparison between the transient vibrations for the nominal system and at activated time-periodic modulation of the additional support shows the increase in effective damping.

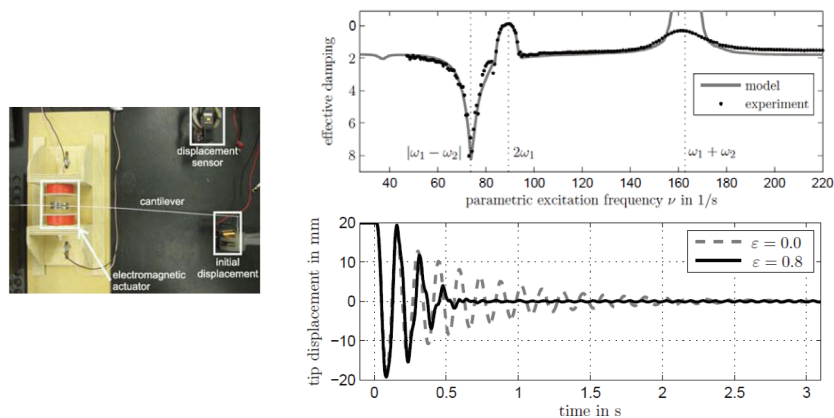


Figure 2. Uniaxial electromagnetic actuator [7]: (left) Cantilever with additional electromagnetic mount, (right, top) Effective damping at a parametric excitation amplitude of  $\epsilon = 0.8$ , (right, bottom) Comparison of transient vibrations for the nominal system and at activated parametric anti-resonance.

Since then, the concept was tested for different applications in structural dynamics at macroscale, e.g. rotordynamics and micro scale, e.g. micro-electromechanical systems (MEMS). A milling machine may experience vibrations, a kind of self-excited vibration mechanism, that occur above a certain cutting depth. A typical stability map is shown

in Fig. 3. Employing a magnetically supported spindle for the milling operation [1] [8] allows for an additional time-periodic modulation of the bearing stiffness. Tuning the frequency of this modulation properly generates a dense region of stable milling operation even for large values of the cutting depth.

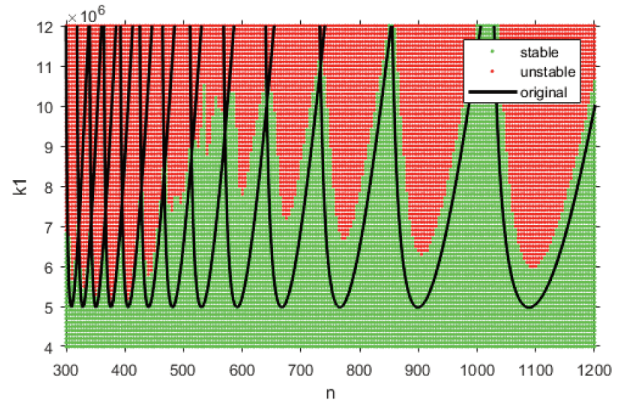
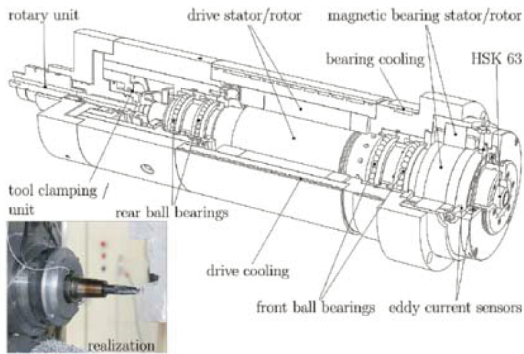


Figure 3. Chatter suppression by parametric anti-resonance: (left) Spindle with active bearings [1]; (right) Stability map of spindle speed over cutting depth for a tool holder at original support stiffness and a time-periodically modulated support showing enlarged stability region at 550 rpm [7]

An efficient implementation of time-periodic modulation in MEMS is shown in Fig. 5. A sensor beam driven at a forced excitation during the time interval  $t_d$  allows for a desired measurement. After the successful measurement, the sensor beam vibrations need to be mitigated quickly for getting ready for the next measurement cycle. A parametric

anti-resonance triggers an energy transfer between the first mode of the sensor beam and the first mode of the auxiliary beam [9-10]. The transient time histories are depicted in Fig. 4 on the top right. The energy transferred to the auxiliary beam is eventually dissipated by structural damping.

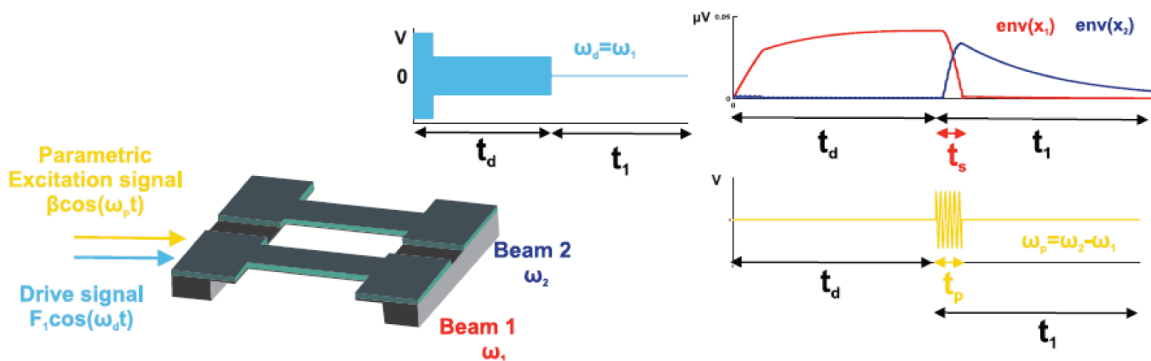


Figure 4. MEMS with multiple degrees of freedom: a modulation at parametric anti-resonance triggers a targeted energy transfer between sensor beam 1 (red) and auxiliary beam 2 (blue) and allows for a significant reduction of the ring-down time of the sensor at repeated measurement operation [11]

Vibrations play also an important role in the power conversion industry. Rotors in this industry are typically supported by fluid-film bearings that may

show instability (whirl) above a critical speed, see Fig. 5 [12]. Introducing an adjustable bearing enables the implementation of a time-periodic modulation and

the chance of mitigating vibrations by a parametric anti-resonance. The vibration mitigation was confirmed theoretically in [13-14] and experimentally in [14]. A real rotor was analyzed [14-15] and shows

a significant increase of the onset speed of rotor whirl. It is also possible to perform high speed balancing of a rotor without turning the rotor at high speed [15].

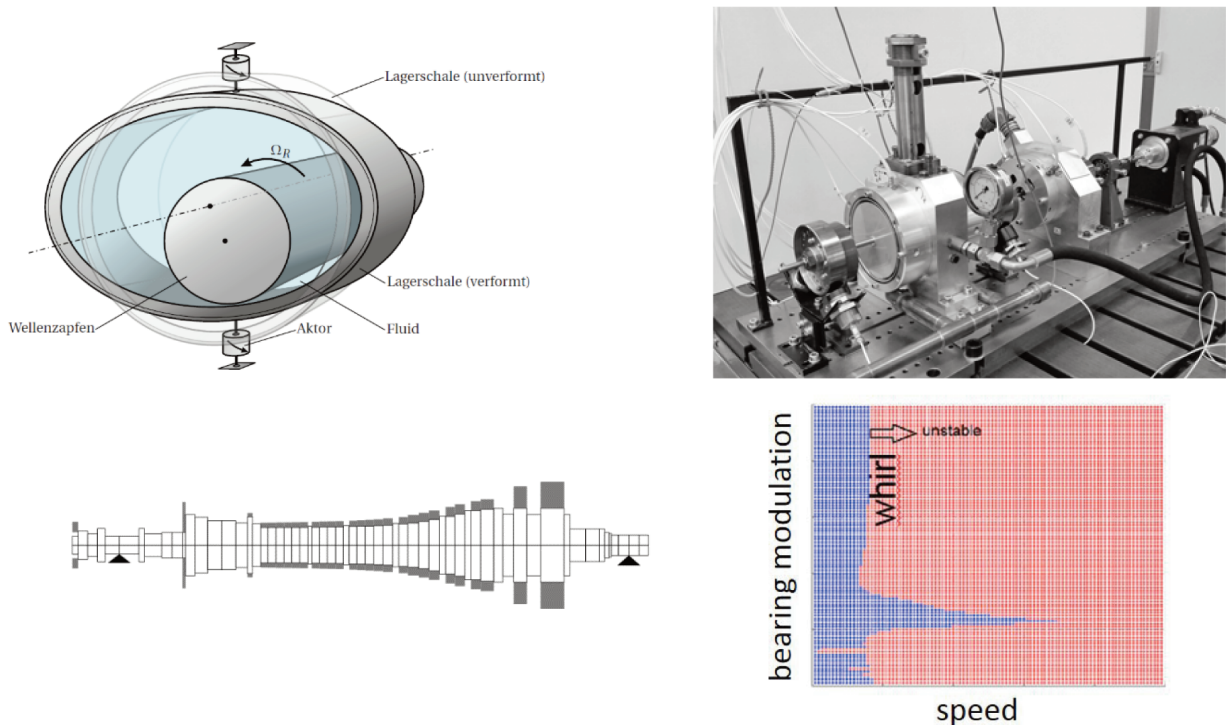


Figure 5. Rotordynamic systems at parametric anti-resonance: (left, top) active deformation of the bearing shell [13], (right, top) experimental test rig of a fluid-film bearing with moveable bearing half shell [14], (bottom) typical rotor for power generation up to 12 MW and the corresponding stability map showing a significant increase of the whirl speed [15]

The concept of parametric anti-resonance is most beneficial for systems with low structural damping. A minimum requirement is that the system possesses at least two vibration modes. If the original system has only one vibration mode, an additional subsystem must be attached. It should be noted that the concept allows for the reduction, and sometimes even

suppression of transient vibrations. Other potential applications that should be investigated in future are the transient vibration of long wind turbines blades [16-17], the drivetrain of cars and wind turbines in Fig. 6 [18] or the seat dynamics of a farming vehicle [19-20].

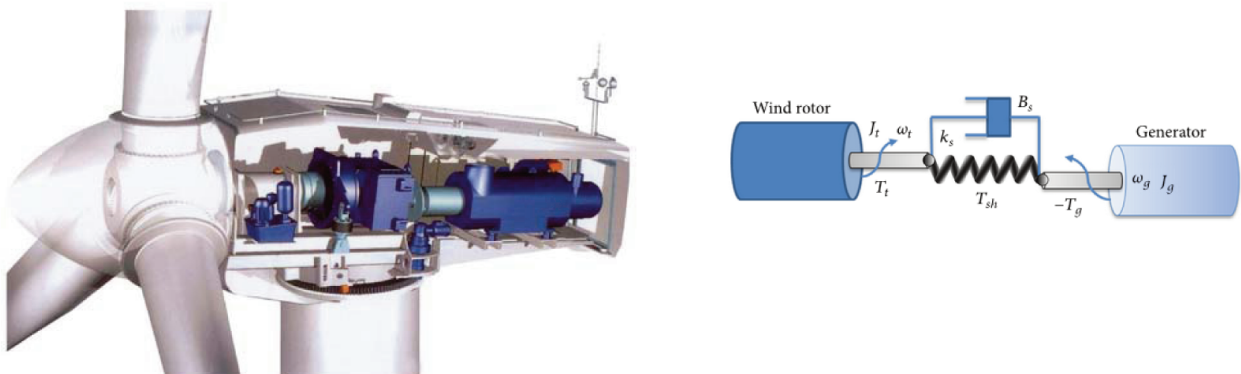


Figure 6. Drivetrain of a wind turbine: (left) assembly, (right) simplified mechanical model [18]

## Conclusions

The concept of parametric anti-resonance is applicable in parallel to existing control strategies and allows for suppressing or at least damping of transient vibrations. Several proven examples and future directions are outlined briefly. Time-periodic systems have been analyzed since decades due to their severe vibration response at parametric excitation. On the contrary, the concept of parametric anti-resonance at macroscale systems was understood recently and enable a structured and efficient implementation in real engineering applications.

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