



Article

Modeling, Control, and Prediction of the Spread of COVID-19 Using Compartmental, Logistic, and Gauss Models: A Case Study in Iraq and Egypt

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Abstract: In this paper, we study and investigate the spread of the coronavirus disease 2019 (COVID-19) in Iraq and Egypt by using compartmental, logistic regression, and Gaussian models. We developed a generalized SEIR model for the spread of COVID-19, taking into account mildly and symptomatically infected individuals. The logistic and Gaussian models were utilized to forecast and predict the numbers of confirmed cases in both countries. We estimated the parameters that best fit the incidence data. The results provide discouraging forecasts for Iraq from 22 February to 8 October 2020 and for Egypt from 15 February to 8 October 2020. To provide a forecast of the spread of COVID-19 in Iraq, we present various simulation scenarios for the expected peak and its timing using Gaussian and logistic regression models, where the predicted cases showed a reasonable agreement with the officially reported cases. We apply our compartmental model with a time-periodic transmission rate to predict the possible start of the second wave of the COVID-19 epidemic in Egypt and the possible control measures. Our sensitivity analyses of the basic reproduction number allow us to conclude that the most effective way to prevent COVID-19 cases is by decreasing the transmission rate. The findings of this study could therefore assist Iraqi and Egyptian officials to intervene with the appropriate safety measures to cope with the increase of COVID-19 cases.

Keywords: COVID-19; compartmental model; logistic growth model; Gaussian model; parameter estimation; second wave; sensitivity analysis; control measures

1. Introduction

1.1. Background

The coronavirus disease 2019 (COVID-19) is an emerging public health problem affecting countries around the world, including Iraq and Egypt, and is caused by the severe acute respiratory syndrome Coronavirus 2 (SARS-CoV-2) [1,2]. The disease spreads from individual to individual, most often when physically nearby, but also over long distances, notably indoors [3,4]. The most common symptoms are fever, fatigue, loss of smell, loss of appetite, muscle pain, dry cough, shortness of breath, and coughing up sputum [5,6]. COVID-19 was discovered in Iraq, and the first coronavirus infection was confirmed in an Iranian student in the city of Najaf on 22 February 2020. A family who had recently returned from Iran tested positive for COVID-19 in the city of Kirkuk near Baghdad on 25 February 2020. The first death of a 70-year-old clergyman was confirmed on 4 March in the city of Sulaimaniyah. The disease spread from 27 March onwards in all 19 Iraqi Governorates. As the infections have been steadily increasing since mid-March 2020, the Iraqi government has taken

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the following measures: a national complete or partial lockdown, curfew, and travel restrictions. Schools, universities, and cinemas in Baghdad were closed, and other large public and religious gatherings were banned in the cities. The Iraqi Ministry of Health announced a nationwide total lockdown, which began on 30 July, except in the region of Kurdistan. The high number of reported cases has led us to study the spread of COVID-19 in Iraq.

Egypt launched its prevention precautions for the fatal virus when it appeared in Wuhan, China. All flights from China to Egypt were suspended on 26 January 2020. The first recorded case was reported on 14 February 2020 in a Chinese man in Egypt. The patient was taken to a quarantine station. The first death of an Egyptian person due to COVID-19 was registered on 20 March 2020, twenty days after the first death was reported in Egypt (for a German man). The Egyptian government has introduced various types of lockdowns to mitigate the effects of the disease. Both schools/universities and places of worship were closed from 7 March and 21 March, respectively. The peak of COVID-19 occurred in Egypt on 19 June 2020, followed by a significant decrease of the number of cases. Egypt reopened its tourism borders for seaside resorts from 1 July. From 1 September, travelers from all countries traveling to any part of Egypt must have confirmation of a negative polymerase chain reaction (PCR) test certificate for COVID-19 completed no more than 72 h before arrival.

1.2. Literature Review

A variety of studies have been published to evaluate the epidemiological features of COVID-19 and to mitigate its effects on public health. Tosepu et al. [7] studied the correlation between weather and the COVID-19 pandemic in Jakarta, Indonesia. Batista [8] utilized the logistic growth model to evaluate the final size and peak of the coronavirus epidemic in China, South Korea, and the rest of the world. In [9], a computational tool was established to assess the risks of novel coronavirus outbreaks outside China. Based on the confirmed data, Abdullah et al. [10] proposed a forecast of the size of the COVID-19 epidemic in Kuwait; deterministic and stochastic modeling approaches were used. A study to forecast the peak of the COVID-19 epidemic in Japan using the traditional SEIR model was conducted by Kuniya [11]. Röst et al. [12] proposed an epidemiological and statistical study of the early phase of the COVID-19 outbreak in Hungary and developed an age-structured compartmental model to investigate alternate post-lockdown scenarios. In [13], the authors developed an exponentiated M family of continuous distributions to provide new statistical models. Several researchers have studied COVID-19 in Iraq (see, e.g., [14–16]). Using several regression models, Amar et al. [17] studied the actual COVID-19 database for Egypt from 15 February to 15 June 2020 to predict the number of COVID-19-infected patients and measured the final epidemic scale. Hasab et al. [18] studied the epidemiological distribution and modeling of the novel coronavirus (COVID-19) epidemic in Egypt using the epidemic SIR model. In [19], the SEIR compartmental model was used to identify the situation of COVID-19 in Egypt and to forecast the expected time of the peak of this epidemic based on the actual reported cases and deaths. The research proposed by El Desouky [20] to predict the time of the possible peak and to model the changes induced by the social behavior of Egyptians during Ramadan (Holy Month) used SIR and SEIR compartment models. Several researchers have studied COVID-19 in Egypt (see, e.g., [21–24]).

1.3. Summary

In this work, we study the prevalence of the COVID-19 outbreak in Iraq and Egypt using a compartmental mathematical model, a logistic regression model, and a simple Gaussian model. To better understand the spread of the virus, we estimate the parameters that provide the best fit to the incidence data from both countries. The parameters with the best fit can be used to calculate the basic reproduction rate. In order to forecast the spread of COVID-19 in Iraq, we show different simulation scenarios for the possible peak and its timing using Gaussian and logistic regression models. Using a generalized SEIR model (our compartmental model) with a time-periodic transmission rate, we predict the possible start of the second wave of COVID-19 in Egypt and the possible control measures.

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We derive a formula for the basic reproduction number, which can be used to obtain the contour plots and sensitivity analysis to show the possible measures for controlling the disease. The article is organized as follows. Section 2 describes the materials and methods. The results are given in Section 3. Section 4 presents the discussion.

2. Materials and Methods

2.1. COVID-19 Data from Iraq and Egypt

The data were collected from Worldometer website [25,26]. We focus on the data from 22 February to 8 October 2020 in Iraq and from 15 February to 8 October 2020 in Egypt.

Figure 1 shows the daily confirmed cases in Iraq and Egypt since the beginning of the pandemic in Iraq and Egypt, respectively, until 8 October 2020. The statistics of the data are shown in Table 1.

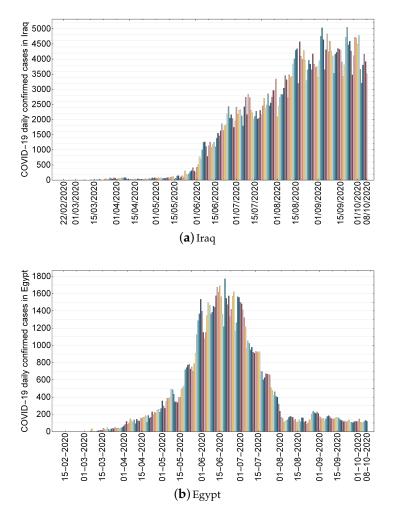


Figure 1. The daily number of confirmed cases in (a) Iraq from 22 February to 8 October 2020 and in (b) Egypt from 15 February to 8 Octobe, r 2020.

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	Iraq Total Sample Size = 231	Egypt Total Sample Size = 238 15 February 2020	
Descriptive Statistics	22 February 2020		
	Cumulative Cases	Cumulative Cases	
Min	1	1	
Max	394,566	104,156	
Median	22,008	41,303	
Mean	92,023	48,004	
Standard error	119,256.6	42,988.4	

Table 1. Statistics for the coronavirus disease 2019 (COVID-19) data from Iraq and Egypt.

2.2. Compartmental Model for COVID-19 Transmission

We spilt the human population into seven compartments: susceptible S(t), exposed E(t), symptomatically infected $I_s(t)$, mildly infected $I_m(t)$, treated H(t), and recovered individuals R(t); and D(t) indicates the individuals who lost their lives due to COVID-19. The total size of the population at any time t is given by

$$N(t) = S(t) + E(t) + I_m(t) + I_s(t) + H(t) + R(t) + D(t).$$

We do not add separate compartments for the quarantined individuals to keep our model simple. Susceptible people (S) are those who can be infected by COVID-19. Once having contracted the disease, an individual progresses to the exposed class (E); these individuals do not yet have symptoms. After the incubation period, exposed individuals move to either the symptomatically infected class (I_s) or the mildly infected class (I_m), depending on whether the individual shows symptoms or not. Mildly infected individuals progress to the recovered class (R) or the symptomatically infected class (I_s). Symptomatically infected individuals move to the treated compartment (H), which includes those who have reported hospitalization. After the infection period, treated persons change to the recovered class (R).

The transmission dynamics are shown in the flow diagram (see Figure 2), and our model takes the form:

$$S'(t) = -\beta \frac{\beta_{e}E(t) + \beta_{m}I_{m}(t) + I_{s}(t) + \beta_{h}H(t)}{N(t) - D(t)}S(t),$$

$$E'(t) = \beta \frac{\beta_{e}E(t) + \beta_{m}I_{m}(t) + I_{s}(t) + \beta_{h}H(t)}{N(t) - D(t)}S(t) - \nu E(t),$$

$$I'_{m}(t) = \theta \nu E(t) - \sigma_{m}I_{m}(t) - \sigma I_{m}(t),$$

$$I'_{s}(t) = (1 - \theta)\nu E(t) + \sigma I_{m}(t) - \sigma_{s}I_{s}(t) - \delta_{s}I_{s}(t),$$

$$H'(t) = \sigma_{s}I_{s}(t) - \sigma_{h}H(t) - \delta_{h}H(t),$$

$$R'(t) = \sigma_{m}I_{m}(t) + \sigma_{h}H(t),$$

$$D'(t) = \delta_{s}I_{s}(t) + \delta_{h}H(t).$$
(1)

The description of the model parameters is summarized in Table 2. Particularly, β stands for the transmission rate from symptomatically infected to susceptible persons, while the transmission rates from exposed, mildly infected, and treated to susceptible are obtained by multiplying β by β_e , β_m , and β_h , respectively. The parameter θ is the fraction of asymptomatically infected persons among all infected people. The length of the latent period for humans is $1/\nu$. $1/\sigma_m$ and $1/\sigma_h$ denote the length of the infection period for mildly and symptomatically infected people, respectively; $1/\sigma$ is the length of the period during which patients progress from mildly to severely infected.

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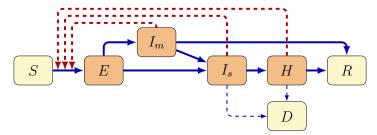


Figure 2. Diagram of COVID-19 transmission. Blue arrows indicate transition from one compartment to another. Light- and dark-colored nodes depict the non-infected and infected compartments, respectively.

Parameters	Description
β	Transmission rate from infectious classes to susceptible
$\beta_e, \beta_m, \beta_h$	The relative transmissibility of E , I_m , and H , respectively
θ	Proportion of asymptomatic infections
σ	Progression rate from I_m to I_s
$\sigma_{\!\scriptscriptstyle S}$	Progression rate from I_s to H
σ_m, σ_h	Recovery rates
δ_s, δ_h	Disease-induced death rates
ν	Incubation rate

Table 2. Description of the parameters of model (1).

2.3. Logistic Growth Model

The logistic growth model in mathematical epidemiology is a regression model frequently used to estimate the growth of a population as exponential, and is then followed by a reduction in growth, with a bound provided by a carrying capacity. Logistic population growth occurs when the rate of population growth decreases as the number of individuals increases. The logistic model introduced in [8,27] takes the form:

$$C' = rC\left(1 - \frac{C}{K}\right),\tag{2}$$

where C denotes the accumulated number of cases, r > 0 is the rate of infection, and K > 0 is the final epidemic size. The number of infected cases is defined as the solution of (2) and is given by

$$C = \frac{K}{1 + be^{-rt}},\tag{3}$$

where $b = \frac{K - C_0}{C_0}$ and C_0 is the initial population. The parameters r and K can be estimated from the data of the epidemic. The maximum growth rate peaks can be estimated at the time $t_p = \frac{\ln(b)}{r}$, and the number of cases at this time is $C_p = \frac{K}{2}$. Thus, the growth rate at the maximum peak is given by

$$\frac{dC}{dt_n} = \frac{rK}{4}.$$

2.4. Gaussian Model

To model the time-dependent daily change of infections, we employ a simple Gaussian model. Let I(t) denote the time-dependent Gaussian function [28,29] and take the following form:

$$I(t) = I_0 e^{-\left(\frac{t-\mu}{\sigma}\right)^2},\tag{4}$$

where I_0 denotes the maximum value at time μ and σ controls the width. The model is characterized by three independent parameters: a variance, a maximum height, and a time of maximum height (peak date). Despite its simplicity, the Gaussian model has significant predictive power. We use it to predict the peak number of infected people and the peak date. In addition, a numerical study

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has explained that the Gaussian model is a special version of the SEIR model. The introduction of gradual social distancing leads to a linear decrease in the infection rate [30]. In the Gaussian model, epidemics are initially exponential; later, as the population approaches carrying capacity, they approach zero, resulting in bell-shaped daily quantities. This starts at zero, approaches a maximum somewhere, and finally drops back to zero.

The assumption behind the logistical growth is that people have an equal chance of infection. Initially, growth is exponential, but the rate of growth decreases and becomes very low with the maximum infectious population. Some may contend that the growth rate should decrease with increasing time; the behavior of Gaussian model and the logistic model have, therefore, very similar results: The Gaussian function converges quickly to zero, like the function e^{-x^2} , while the logistic function is simply the exponential in this aspect e^x , and the logistic growth model is often used to determine the future total epidemic size of the variable.

2.5. Parameter Estimation and Sensitivity

To estimate the parameters of the logistic growth model (2) and the Gaussian model (4), which give the best fit to the epidemic data, we employ the nonlinear least-square curve, which we fit to the incidence curve given by the equations of C'(t) and I(t), respectively. As in the first observation, the initial number of C_0 cases was determined. The parameters of the model (1) that gives the best fit to the data can be estimated by using Latin Hypercube Sampling. This is a sampling method that measures the variation of several parameter values simultaneously (see [31] for details). The core idea of the method is to create a representative sample from the ranges for all parameters listed in Table 3. The solutions of the model (1) are calculated (numerically) for each element of this sample set. Finally, we apply the least-squares method to find the parameters that provide the best fit.

To identify the parameters with respect to their effects on the basic reproduction number, we will apply partial rank correlation coefficient analysis (PRCC; see, e.g., [32]) to perform sensitivity analysis. The PRCC-based sensitivity analysis measures the effects of the parameters on the basic reproduction number while we change the parameters in the given ranges.

2.6. Reproduction Numbers

The basic reproduction number \mathcal{R}_0 is an important threshold parameter for estimating the effort required to eliminate the contagious diseases, and it is perceived as the expected number of secondary infections produced by an infected individual in a population where all individuals are susceptible to infection.

By using the next generation method introduced in [33], we derive a formula for the basic reproduction number of (1). Then, taking into account the infection states E, I_m , I_s , and H in (1) and by substituting the values in the disease-free equilibrium (N,0,0,0,0,0,0), the matrices F and V are calculated for the new infection terms and the remaining transfer terms. The Jacobian F and V are given by

As per [33], the basic reproduction number is the largest absolute eigenvalue of FV^{-1} ; thus, it is given by

$$\mathcal{R}_{0} = \rho(FV^{-1}) = \frac{\beta\beta_{e}}{\nu} + \frac{\theta\beta\beta_{m}}{(\sigma + \sigma_{m})} + \frac{\beta(\sigma + (1 - \theta)\sigma_{m})}{(\sigma + \sigma_{m})(\sigma_{s} + \delta_{s})} + \frac{\beta\beta_{h}\sigma_{s}(\sigma + (1 - \theta)\sigma_{m})}{(\sigma + \sigma_{m})(\sigma_{s} + \delta_{s})(\sigma_{h} + \delta_{h})}.$$
 (5)

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In addition to calculating the basic reproduction number \mathcal{R}_0 of the model (1), the time-dependent reproduction number can be calculated from incidence data (see, e.g., [34] for details).

3. Results

3.1. Parameter Estimation for Iraq and Egypt

Using the method described in Section 2.5, we fitted our model to symptomatically infected cases in Iraq and Egypt.

Figure 3 shows the model (1) fitted to the daily number of confirmed cases in Iraq from 22 February to 8 October 2020 (left panel), and in Egypt, from 5 March to 8 October 2020 (right panel). Our model yields a reasonably good fit for both countries by predicting the peak in Iraq and showing the peak in Egypt. The fitting parameter results are listed in Table 3.

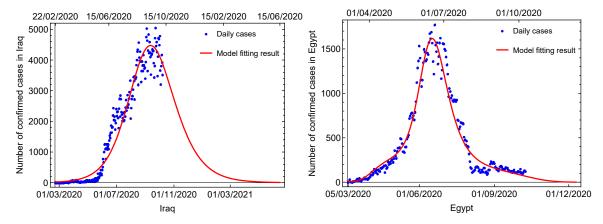


Figure 3. The model (1) fitted to the daily confirmed cases in (**left panel**) Iraq and in (**right panel**) Egypt with the parameters given in Table 3.

Parameters	Value for Iraq	Value for Egypt	Source	
1 arameters	$\mathcal{R}_0 = 1.323$	$\mathcal{R}_0=1.11$	Source	
β	0.753	0.56	Fitted	
eta_e	0.082	0.053	Fitted	
β_m	0.475	0.587	Fitted	
β_h	0.2057	0.443	Fitted	
θ	0.778	0.875	Fitted	
σ	0.307	0.104	Fitted	
$\sigma_{\!\scriptscriptstyle S}$	0.3247	0.213	Fitted	
σ_m	0.239	0.661	Fitted	
σ_h	0.446	0.508	Fitted	
$\delta_{\scriptscriptstyle S}$	0.127	0.131	Fitted	
δ_h	0.298	0.268	Fitted	

Table 3. Parameters and fitted values of model (1) in the cases of Iraq and Egypt.

3.2. Forecast of the Spread of COVID-19 in Iraq and Egypt

To fit the confirmed cumulative cases in both countries from the beginning of the outbreak on 22 February and 15 February, 2020, respectively, until 8 October, 2020, we applied the logistic model (2), which was used to predict the short-term forecast.

0.266

Fitted

0.54

Figure 4 shows the logistic growth model (2) fitted to the cumulative number of infected cases in Iraq (left panel) and the cumulative number of infected cases in Egypt (right panel) with the parameters given in Table 4. We note that the logistic model fit the incidence data with a root mean square error (RMSE) of 5229.7 and R^2 of 0.9981 for the Iraqi data and with an RMSE of 1,924.4 and R^2

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of 0.9980 for the Egyptian data, as shown in Table 4. The logistic model gives a reasonably good fit for both countries.

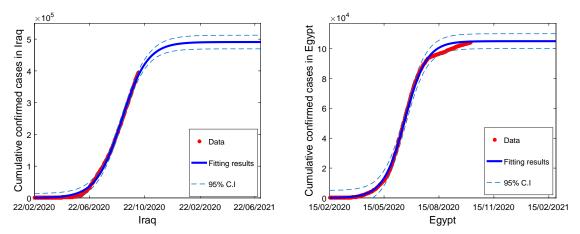


Figure 4. The logistic model (2) fitted to the cumulative number of infected cases in Iraq (**left panel**) and in Egypt (**right panel**).

Parameters	Iraq		Egypt	
rarameters	$\mathcal{R}_0 = 1.0659$	C.I	$R_0 = 1.0318$	C.I
Estimated epidemic size (cumulative cases)	490,900	(478, 300, 503, 500)	105,000	(104, 500, 105, 900)
Estimated start of ending phase date	05/05/2021		04/11/2020	
Goodness of fit (R^2)	0.9981		0.9980	
Root Mean Square Error (RMSE)	5229.7		1924.4	

Table 4. Estimated parameter results of the logistic model (2) for Iraq and Egypt.

The Gaussian model was fitted to data from Iraq and Egypt with reproduction numbers 1.0659 and 1.0318, respectively. Figure 5 shows the Gaussian model fitted to the daily number of confirmed cases from Iraq (left panel) and to the daily number of confirmed cases from Egypt (right panel) with the parameters given in Table 5. The model fits the actual data well with a root mean square error (RMSE) of 335.607 and R^2 of 0.9614 for the Iraqi data and with an RMSE of 110.33 and R^2 of 0.9528 for the Egyptian data, as listed in Table 5.

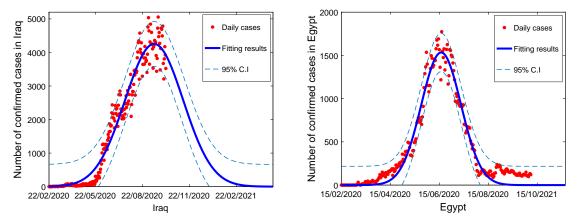


Figure 5. The Gaussian model fitted to the daily confirmed cases in Iraq (**left panel**) and in Egypt (**right panel**).

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Parameters	Ira	ıq	Egypt		
1 diameters	$\mathcal{R}_0=1.0659$	C.I	$\mathcal{R}_0=1.0318$	C.I	
Estimated peak day cases	4254	(4161, 4347)	1534	(1493, 1574)	
Estimated peak date	14/09/2020		16/06/2020		
Goodness of fit (R^2)	0.9614		0.9528		
Root Mean Square Error (RMSE)	335.607		110.33		

Table 5. Estimated parameter results of the Gaussian model for Iraq and Egypt.

The peak of COVID-19 in Egypt occurred on 16 June 2020 with 1534 daily cases. Afterward, the number of daily confirmed cases gradually decreased, and the estimated epidemic size was 105,000 on 4 November 2020. In the coming days in Iraq, the forecast curve shows a significant increase in the estimated size of the epidemic to 490,900. It also shows that the scale of the epidemic is increasing rapidly, indicating that the number of infections continues to rise steadily.

3.3. Prediction of the Spread of the COVID-19 Epidemic in Iraq

It is expected that the daily confirmed cases through Ziarat, the holy shrines in Iraq from different countries, will increase significantly. To predict the spread of COVID-19 in Iraq, we apply the Gaussian model (4) to estimate the value and timing of the expected peak. The logistic model was used to estimate the growth rate at each point in time of the expected peak.

Figure 6 shows the three different scenarios of COVID-19 in Iraq, as well as the daily and commutatively confirmed cases, with three expected maximum values at the peak times. The results illustrate that the highest predicted number cumulative cases is estimated at 650,000 with 6500 daily cases, and this would occur on 17 November 2020, while the peak times of scenario one and scenario two are expected to occur on 10 October 2020 and 5 November 2020, respectively. The parameters used to obtain each scenario are listed in Tables 6 and 7.

A short-term forecast of confirmed cases and cumulative predicted cases from Iraq is presented in Table 8. The errors by day are probably greater than the cumulative errors, as can be seen from Table 8. Minimizing cumulative error is almost certainly the more important goal. This is indeed one of the traditional strengths of the logistic model.

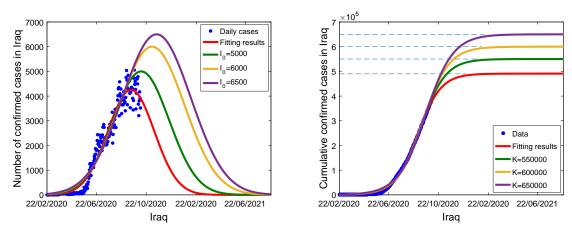


Figure 6. Three different scenarios for the daily confirmed cases (**left panel**) and the cumulative number of infected cases (**right panel**) in Iraq, 2020–2021.

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Logistic Model			
o One Scenario Two	Scenario Three		
,	650,000 05/08/2021		
0.9967	0.9958 7775.5		
	io One Scenario Two 000 600,000 /2021 07/07/2021		

Table 7. Estimated parameter results for the three scenarios of the Gaussian model in Iraq.

	Iraq		
Parameters		Gaussian Mode	el
1 atameters	Scenario One	Scenario Two	Scenario Three
Estimated peak day cases	5000	6000	6500
Estimated peak date	10/10/2020	05/11/2020	17/11/2020
Goodness of fit (R^2)	0.9515	0.9413	0.9378
Root Mean Square Error (RMSE)	360.6507	396.8004	408.4278

Table 8. Prediction and confirmed cases in Iraq.

Daily Cases		Cumulative Cases				
Date	Predicted	Confirmed	Error (%)	Predicted	Confirmed	Error (%)
5-Oct-20	4011.94	3808	5.36	376,351.09	382,949	1.72
6-Oct-20	3987.28	4172	4.43	379,430.15	387,121	1.99
7-Oct-20	3961.56	3923	0.98	382,450.32	391,044	2.20
8-Oct-20	3934.80	3522	11.72	385,411.44	394,566	2.32
9-Oct-20	3907.02	-	-	388,313.42	-	-
10-Oct-20	3878.25	-	-	391,156.25	-	-
11-Oct-20	3848.52	-	-	393,940.00	-	-
12-Oct-20	3817.84	-	-	396,664.80	-	-
13-Oct-20	3786.24	-	-	399,330.85	-	-
14-Oct-20	3753.76	-	-	401,938.42	-	-
15-Oct-20	3720.42	-	-	404,487.83	-	-
16-Oct-20	3686.24	-	-	406,979.47	-	-
17-Oct-20	3651.26	-	-	409,413.76	-	-
18-Oct-20	3615.50	-	-	411,791.19	-	-
19-Oct-20	3579.00	-	-	414,112.30	-	-
20-Oct-20	3541.77	-	-	416,377.66	-	-
21-Oct-20	3503.87	-	-	418,587.89	-	-
22-Oct-20	3465.30	-	-	420,743.64	-	-
23-Oct-20	3426.12	-	-	422,845.60	-	-

3.4. Prediction of the Second Wave of the COVID-19 Epidemic in Egypt

The second wave of the COVID-19 pandemic has been reported in a few countries around the world, such as France, Italy, Spain, Germany, and Hungary. When the second wave will start in Egypt is an interesting question. To predict the second wave of the COVID-19 pandemic in Egypt, we assume that $\beta \equiv \beta(t)$ is a continuous, time-periodic transmission rate with one year as the period and, following, e.g., [35–37], it is assumed to be of the form $\beta(t) = \beta_0 \cdot \left(\sin\left(\frac{2\pi}{366}t + b\right) + a\right)$, where a, b are free adjustment parameters and β_0 is the (constant) baseline value of $\beta(t)$. This function was used to model the periodic recurrence of infectious diseases such as malaria, Zika virus, and Lassa virus. In our simulation, the adjustment parameters a and b were set to 1.15 and 52.5, respectively. To obtain the second peak time, we have performed a simulation with a time-dependent transmission rate to see what kinds of changes in some parameters could increase the number of infected cases. Our simulation started with the fitted parameters given in Table 3. We have increased the transmission rates (β_0 , β_e , β_m , β_h) and the progression rate (σ) from mildly to severely infected; we got a new

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parameter set that can be used to obtain one scenario. By repeating the previous step, we got three different scenarios. We also note that slight changes have been made to the other parameters. We have found that the most effective parameter is the transmission rate.

Figure 7 shows the three different scenarios for the daily confirmed cases in Egypt with their corresponding basic reproduction numbers. The start of the second wave is estimated to occur on 7 November 2020 with $\mathcal{R}_0=2.54$, on 20 November 2020 with $\mathcal{R}_0=2.31$, and on 10 December 2020 with $\mathcal{R}_0=1.92$. Therefore, the expected start time of the second round of COVID-19 in Egypt is estimated to be in the time period between 7 November and 10 December 2020.

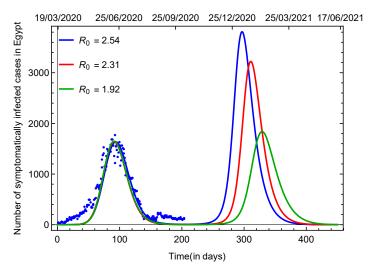


Figure 7. Three different scenarios for the daily confirmed cases in Egypt, 2020–2021.

Based on our simulation, the probability of occurrence of the second wave of COVID-19 in Egypt is high, and it depends on the behavior of individuals and their adherence to the precautionary measures and the government's instructions for reducing the COVID-19 transmission rate.

We have listed the results obtained in Sections 3.1–3.4 in Table 9 to summarize our findings for Iraq and Egypt, which we obtained by using a compartmental mathematical model (1), logistic growth model (2), and Gaussian model (4). Table 9 shows a comparison between the estimated parameters obtained by the three different models, the predicted results of the COVID-19 epidemic in Iraq, and the estimated start dates of the second wave of COVID-19 in Egypt.

3.5. Sensitivity Analysis and Possible Control Measures

To estimate how easily the virus spreads, the reproduction number \mathcal{R}_0 is estimated from the cumulative number of COVID-19 cases using the exponential growth (EG) method and maximum likelihood method (ML; see, e.g., [34] for details). The results are shown in Table 10. The reproduction number is greater than one in both countries and the disease persists.

In addition to calculating the reproduction number from the incidence data, we derive a formula for the reproduction number from our compartmental model (1). Formula (5) provides us with the basic reproduction number at any given time by substituting the parameter values into it. To assess the dependence of the basic reproduction number on the parameters that can be used to control the spread of the virus, the contour plot of the basic reproduction number in terms of the transmission rate (β), progression rate from mildly infected to symptomatically infected individuals (σ), and progression rate from symptomatically infected to hospitalized individuals (σ) for Iraq and Egypt are shown in Figure 8a,b, respectively. Reducing the transmission rate (β) can reduce the number of severely infected persons and, thus, the number of infected individuals who need to be treated and intensively cared for in hospitals.

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Table 9. Summary of the results obtained for Iraq and Egypt in Sections 3.1–3.4.

Madals/Paramatars		Iraq	Egypt
Models/Parameters		Value (C.I)	Value (C.I)
Compartmental model			
\mathcal{R}_0		1.323	1.11
β		0.753	0.56
β_e		0.082	0.053
β_m		0.475	0.587
β_h		0.2057	0.443
θ		0.778	0.875
σ		0.307	0.104
$\sigma_{\scriptscriptstyle extsf{S}}$		0.3247	0.213
σ_m		0.239	0.661
σ_h		0.446	0.508
		0.127	0.131
δ_s			
δ_h		0.298	0.268
ν		0.54	0.266
Logistic Growth Model			
\mathcal{R}_0		1.0659	1.0318
Estimated epidemic size		490,900 (478,300, 503,500)	105,000 (104,500, 105,900
Estimated start of ending phase date		05/05/2021	04/11/2020
Gaussian model		00, 00, 2 021	01, 11, 2020
		1.0659	1.0318
\mathcal{R}_0			
Estimated peak day cases		4254 (4161, 4347)	1534 (1493, 1574)
Estimated peak date		14/09/2020	16/06/2020
Prediction of the spread of COVID-1	9 epidemic in Ir	aq	
-	Scenario one	Scenario two	Scenario three
T			
Estimated peak day cases	5000	6000	6500
Estimated peak date	10/10/2020	05/11/2020	17/11/2020
Estimated epidemic size	550,000	600,000	650,000
Estimated start of ending phase date	17/06/2021	07/07/2021	05/08/2021
Prediction of the second wave of CO	VID-19 epidemi	c in Egypt	
	Scenario one	Scenario two	Scenario three
Estimated start of the second wave	07/11/2020	20/11/2020	10/12/2020
\mathcal{R}_0	2.54	2.31	1.92
σ	3 2 1.0 0	1.0 0.8 0.6 0.4 0.2 0.0 0.0 0.2 0.4 0.6 0.8	0.8 1.0 4 3 2 1 0
a)	(a)	Iraq	
1.0		1.05	· · · · · · · · · · · · · · · · · · ·
0.8	2.5 2.0 1.5 1.0 0.5 8 1.0	0.8 0.6 0.4 0.2 0.0 0.0 0.2 0.4 0.6	2.5 2.0 1.5 1.0 0.5
<i>σ</i> a)	(b) !	σ_{s} b)	

Figure 8. The contour plots of the basic reproduction number for Iraq and Egypt as a function of (β) and for (**a**) progression rate from I_m to I_s (σ) or for (**b**) progression rate from I_s to H (σ_s), respectively.

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Methods	Iraq		Egypt	
Methous	\mathcal{R}_0	C.I	\mathcal{R}_0	C.I
EG	1.1017	(1.10166, 1.101768)	1.0604	(1.060386, 1.060481)
ML	1.0659	(1.065207, 1.066639)	1.0318	(1.030841, 1.032637)

Table 10. Calculation of the reproduction number \mathcal{R}_0 using cumulative cases.

Figure 9 shows a comparison of the PRCC values obtained for the parameters in the basic reproduction number \mathcal{R}_0 for Iraq and Egypt. The results of the sensitivity analysis show that any positive change in the parameters $(\beta, \beta_e, \beta_m, \beta_h, \theta, \nu, \sigma, \sigma_h)$ gives a corresponding ratio for the riskiness of the disease, while \mathcal{R}_0 can be decreased by increasing the values of the parameters (σ_m, σ_s) in both countries. The parameters δ_s and δ_h can not be used as a control measure because they are death rates.

We noticed from the PRCC that the most influential parameter is β , which can be used to control the spread of COVID-19. Decreasing the transmission rate can decrease the number of infected and even turn the disease toward complete extinction. In addition to decreasing the transmission rate from severely infected to susceptible (β), decreasing the parameters β_e , β_m , and β_h would also decrease the basic reproduction number, but this control is not sufficient to drive \mathcal{R}_0 below one. These parameters can be lowered by quarantining any person who tested positive for COVID-19 and has no or mild symptoms for a sufficient period of time (10–14 days). Our model also has its limitations, as we cannot estimate the impact of a quarantine on the spread of the virus. It has also been observed that by reducing the rate of progression from mildly to severely infected (σ), the number of severely infected individuals is also reduced, but just this measure is unable to drive the disease to extinction.

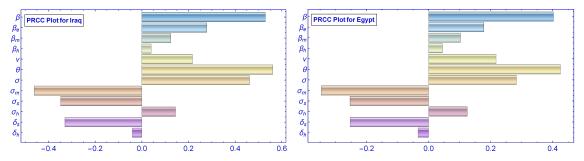


Figure 9. The partial rank correlation coefficient (PRCC) plot of the parameters of \mathcal{R}_0 for Iraq (**left panel**) and for Egypt (**right panel**).

4. Discussion

In this work, we have studied the spread of the COVID-19 pandemic in Iraq and Egypt using a Gaussian model, logistic growth model, and compartmental (generalized SEIR) model. The parameters were estimated using our compartmental model, which was used to understand the spread of COVID-19 in both countries. Our model provides a reasonably good fit to the incidence data. We fitted the logistic model to the cumulative number of confirmed COVID-19 cases in Iraq and Egypt. The simulation results can be used to reduce the at-risk and susceptible population through control measures, such as social distancing and lockdowns, and/or changing the population's behavior. The Gaussian model was used to obtain statistical predictions for the COVID-19 pandemic in Iraq and Egypt; we fitted the Gaussian model to the daily confirmed COVID-19 cases in both countries. A large rise in the predicted epidemic size in Iraq is shown by the forecast curve, and for the Egyptian data, the model gives a reasonably good fit. The Gaussian model indicates that the peak value is 4254 in Iraq and 1534 in Egypt, while the logistic model shows that the peak value is 490,900 and 105,000 in Iraq and Egypt, respectively. It is important to note that the lockdown was imposed by the Iraqi government on 30 July 2020.

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The basic reproduction number over a period of time is greater than one, suggesting an exponential growth in cumulative confirmed cases in Iraq, which could indicate that the lockdown regulations are not being properly implemented, which might contribute to a rise in the size and spread of the epidemic. Therefore, in order to lift the restriction, the Iraqi health authorities aim to keep the reproduction rate below one.

Various scenarios for the outbreak of COVID-19 in Iraq were examined in order to provide officials with perspectives for effective intervention measures. Throughout the study, Gaussian and logistic models were used to predict the peaks of daily confirmed cases, the cumulative numbers of infected cases, and the predicted start and end dates of the pandemic. The results of the third scenario illustrate that the highest predicted cumulative cases are estimated at 650,000, with daily cases estimated at 6500 and occurring on 17 November 2020, while the peaks of scenario one and scenario two are expected on 10 October 2020 and 5 November 2020, respectively. Our simulation results indicate that the possible peak time for the COVID-19 outbreak in Iraq is expected to be between 8 October and 15 November 2020. Several lockdown scenarios and appropriate measures were implemented by the Egyptian government. Consequently, the number of confirmed cases was suppressed after the peak time on 19 June 2020. Nowadays, Egypt has reopened its tourism borders to visitors from all over the world; it has opened places of worship, shopping malls, and markets, and also plans to open schools and universities on 17 October 2020. For this reason, the occurrence of the second wave of the COVID-19 epidemic in Egypt is possible; we ran our simulation using a compartmental model with a time-periodic transmission rate to predict the possible timing of the second wave. Three different scenarios with basic reproduction rates between 1.92 and 2.54 indicate that the expected beginning of the second COVID-19 outbreak in Egypt is estimated to be between 7 November and 10 December 2020. These results, which are based on our assumptions and the corresponding parameter sets, were used.

The reproduction number was estimated based on the cumulative confirmed cases by using the exponential growth (EG) method and maximum likelihood method (ML), and was found to be 1.0659–1.1017 and 1.0318–1.0604 for Iraq and Egypt, respectively. Using our compartmental model, a formula for the basic reproduction number was obtained, which allowed us to calculate the value of \mathcal{R}_0 . Using the estimated parameter set resulting from fitting our model to the incidence data in both countries, we found that $\mathcal{R}_0=1.323$ and $\mathcal{R}_0=1.11$ for Iraq and Egypt, respectively. The basic reproduction number is greater than one, indicating that the virus still persists in both countries. The sensitivity analysis and the contour plots of the basic reproduction number (see Figures 8 and 9) suggest that to control the spread of the COVID-19 outbreak, both countries should work to decrease the transmission rate enough by educating the population on how to keep away from contracting the disease, raising the population's awareness of fighting the virus, making wearing a face mask necessary in public places, and making more restrictions on travel between cities that have large numbers of infected people.

The Iraqi government and health authorities need to impose more restrictions on people gathering at places of worship and on religious occasions, particularly in October 2020. In addition, the PCR test is mandatory for every person entering the country. Egypt has stipulated that everyone must have a negative PCR test certificate in order to enter the country, but at the same time, wedding celebrations and all shops, markets, and places of worship were reopened after the number of infected people dropped. To prevent a major outbreak of the COVID-19 disease in Egypt, health authorities should continue to raise people's awareness, educate them on how to protect themselves from the fatal virus, and encourage them to follow the precautions.

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References

- 1. Wu, Z.; McGoogan, J.M. Characteristics of and important lessons from the coronavirus disease 2019 (COVID–19) outbreak in China: Summary of a report of 72,314 cases from the Chinese center for disease control and prevention. *J. Am. Med. Assoc.* 2020, 323, 1239.e42. [CrossRef] [PubMed]
- 2. Gorbalenya, A.E.; Baker, S.C.; Baric, R.S.; de Groot Raoul, J.; Drosten, C.; Gulyaeva, A.A.; Haagmans, B.L.; Lauber, C.; Leontovich, A.M.; Neuman, B.W. The species Severe acute respiratory syndrome-related coronavirus: Classifying 2019-nCoV and naming it SARS-CoV-2. *Nat. Microbiol.* **2020**, *5*, 536–544.
- 3. Centers for Disease Control and Prevention (CDC). How COVID–19 Spreads. Available online: https://www.cdc.gov/coronavirus/2019-ncov/prevent-getting-sick/how-covid-spreads.html (accessed on 8 October 2020).
- 4. European Centre for Disease Prevention and Control. Transmission of COVID–19. Available online: https://www.ecdc.europa.eu/en/COVID--19/latest-evidence/transmission (accessed on 8 October 2020).
- 5. World Health Organization (WHO). Coronavirus. Available online: https://www.who.int/health-topics/coronavirus#tab=tab_1 (accessed on 8 October 2020).
- 6. Centers for Disease Control and Prevention (CDC). Symptoms of Coronavirus. Available online: https://www.cdc.gov/coronavirus/2019-ncov/symptoms-testing/symptoms.html (accessed on 8 October 2020).
- 7. Tosepu, R.; Gunawan, J.; Effendy, D.S.; Lestari, H.; Bahar, H.; Asfian, P. Correlation between weather and Covid–19 pandemic in Jakarta, Indonesia. *Sci. Total Environ.* **2020**, 725, 138436. [CrossRef] [PubMed]
- 8. Batista, M. Estimation of the final size of the second phase of coronavirus epidemic by the logistic model. *MedRxiv* **2020**. [CrossRef]
- 9. Boldog, P.; Tekeli, T.; Vizi, Z.; Dénes, A.; Bartha, F.A.; Röst, G. Risk Assessment of Novel Coronavirus COVID–19 Outbreaks Outside China. *J. Clin. Med.* **2020**, *9*, 571. [CrossRef]
- 10. Almeshal, A.M.; Almazrouee, A.I.; Alenizi, M.R.; Alhajeri, S.N. Forecasting the Spread of COVID–19 in Kuwait Using Compartmental and Logistic Regression Models. *Appl. Sci.* **2020**, *10*, 3402. [CrossRef]
- 11. Kuniya, T. Prediction of the epidemic peak of coronavirus disease in Japan. *J. Clin. Med.* **2020**, *9*, 789. [CrossRef] [PubMed]
- 12. Röst, G.; Bartha, F.A.; Bogya, N.; Boldog, P.; Dénes, A.; Ferenci, T.; Horváth, K.J.; Juhász, A.; Nagy, C.; Tekeli, T.; et al. Early Phase of the COVID–19 Outbreak in Hungary and Post-lock-down Scenarios. *Viruses* **2020**, *12*, 708. [CrossRef]
- 13. Bantan, R.A.R.; Chesneau, C.; Jamal, F.; Elgarhy, M. On the Analysis of New COVID–19 Cases in Pakistan Using an Exponentiated Version of the M Family of Distributions. *Mathematics* **2020**, *8*, 953. [CrossRef]
- 14. Sarhan, A.R.; Flaih, M.H.; Hussein, T.A.; Hussein, K.R. Novel coronavirus (COVID–19) Outbreak in Iraq: The First Wave and Future Scenario. *medRxiv* **2020**. [CrossRef]
- 15. Jebril, N. Distinguishing epidemiological curve of novel coronavirus disease (COVID–19) cases in Iraq: How it does not follow the epidemic curve of China. *SSRN* **2020**, 3571889. http://dx.doi.org/10.2139/ssrn.3571889. [CrossRef]
- 16. Al-Hussein, A.B.A.; Tahir, F.R. Epidemiological characteristics of COVID–19 ongoing epidemic in Iraq. *Bull. World Health Organ. E-Pub* **2020**, *6*. doi: http://dx.doi.org/10.2471/BLT.20.257907. [CrossRef]
- 17. Amar, L.A.; Taha, A.A.; Mohamed, M.Y. Prediction of the final size for COVID–19 epidemic using machine learning: A case study of Egypt. *Infect. Dis. Model.* **2020**, *5*, 622–634. [CrossRef]
- 18. Hasab, A.A.; El-Ghitany, E.M.; Ahmed, N.N. Situational Analysis and Epidemic Modeling of COVID–19 in Egypt. *J. High Inst. Public Health* **2020**, *50*, 46–51. [CrossRef]
- 19. Anwar, W.A.; AbdelHafez, A.M. Forecasting the peak of novel coronavirus disease in Egypt using current confirmed cases and deaths. *medRxiv* **2020**. [CrossRef]
- 20. El Desouky, E.D. Prediction of the Epidemic Peak of Covid19 in Egypt. medRxiv 2020. [CrossRef]

Processes 2020, 8, 1400

21. Asamoah, J.; Jin, Z.; Seidu, B.; Odoro, F.T.; Sun, G.Q.; Alzahrani, F. Mathematical Modelling and Sensitivity Assessment of COVID–19 Outbreak for Ghana and Egypt. *SSRN* **2020**, 3612877. http://dx.doi.org/10.2139/ssrn.3612877. [CrossRef]

- 22. Fahmy, A.E.; Eldesouky, M.M.; Mohamed, A.S. Epidemic Analysis of COVID–19 in Egypt, Qatar and Saudi Arabia using the Generalized SEIR Model. *medRxiv* **2020**. [CrossRef]
- 23. Saba, A.I.; Elsheikh, A.H. Forecasting the prevalence of COVID–19 outbreak in Egypt using nonlinear autoregressive artificial neural networks. *Process Saf. Environ. Prot.* **2020**, *141*, 1–8. [CrossRef] [PubMed]
- 24. Zhao, Z.; Li, X.; Liu, F.; Zhu, G.; Ma, C.; Wang, L. Prediction of the COVID–19 spread in African countries and implications for prevention and controls: A case study in South Africa, Egypt, Algeria, Nigeria, Senegal and Kenya. *Sci. Total Environ.* **2020**, 729, 138959. [CrossRef]
- 25. Worldometer. Available online: https://www.worldometers.info/coronavirus/country/iraq/ (accessed on 8 October 2020).
- 26. Worldometer. Available online: https://www.worldometers.info/coronavirus/country/egypt/ (accessed on 8 October 2020).
- 27. Bacaër, N. Verhulst and the logistic equation (1838). In *A Short History of Mathematical Population Dynamics*; Springer Ltd.: London, UK, 2011; pp. 35–39.
- 28. Schüttler, J.; Schlickeiser, R.; Schlickeiser, F.; KrSchöttlerger, M. COVID–19 Predictions Using a Gauss Model, Based on Data from April 2. *Physics* **2020**, *2*, 197–212. [CrossRef]
- 29. Schlickeiser, R.; Schlickeiser, F. A Gaussian Model for the Time Development of the Sars-Cov-2 Corona Pandemic Disease. Predictions for Germany Made on 30 March 2020. *Physics* **2020**, *2*, 164–170. [CrossRef]
- 30. Barmparis, G.D.; Tsironis, G.P. Estimating the infection horizon of COVID-19 in eight countries with a data-driven approach. *Chaos Solitons Fractals* **2020**, *135*, 109842. [CrossRef]
- 31. McKay, M.D.; Beckman, R.J.; Conover, W.J. Comparison of three methods for selecting values of input variables in the analysis of output from a computer code. *Technometrics* **1979**, *21*, 239–245.
- 32. Blower, S.M.; Dowlatabadi, H. Sensitivity and uncertainty analysis of complex models of disease transmission: An HIV model, as an example. *Int. Stat. Rev.* **1994**, *62*, 229–243. [CrossRef]
- 33. Diekmann, O.; Heesterbeek, J.A.P.; Roberts, M.G. The construction of next-generation matrices for compartmental epidemic models. *J. R. Soc. Interface* **2010**, *7*, 873–885. [CrossRef] [PubMed]
- 34. Obadia, T.; Haneef, R.; Boëlle, P. The R₀ package: A toolbox to estimate reproduction numbers for epidemic outbreaks. *BMC Med. Inform. Decis. Mak.* **2012**, 12, 147. [CrossRef] [PubMed]
- 35. Dénes, A.; Ibrahim, M.A.; Oluoch, L.; Tekeli, M.; Tekeli, T. Impact of weather seasonality and sexual transmission on the spread of Zika fever. *Sci. Rep.* **2019**, *9*, 1–10. [CrossRef] [PubMed]
- 36. Bakary, T.; Boureima, S.; Sado, T. A mathematical model of malaria transmission in a periodic environment. *J. Biol. Dyn.* **2018**, *12*, 400–432. [CrossRef]
- 37. Ibrahim, M.A.; Dénes, A. Threshold and stability results in a periodic model for malaria transmission with partial immunity in humans. *Appl. Math. Comput.* **2021**, 392, 125711. [CrossRef]

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