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# A matrix-based flexible project-planning library and indicators

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<i>Keywords</i> : Project scheduling Project database Flexibility Topology Time- and resource-related indicators	Flexible approaches, such as agile, hybrid, and extreme project management methods in the software project environment, are increasingly being used in nonsoftware environments. Nevertheless, only a few methods and no topological, time-related or resource-related indicators or project databases can address projects of a flexible nature. This study proposes a unified matrix-based model (UMP) to consider single-mode, multimode, individual and multiple projects. Based on the UMP, a CMPD is specified to collect 11 existing project databases. In addition, a flexible structure generator (FSG) is proposed to generate flexible tasks and dependencies for analyzing the effects of flexibility on topology and project demand-related indicators. By correlation graphs, the relations between structure-related and demand-related indicators are analyzed. The comparison of the simulated and real-life databases shows that the interpretation range of the indicators is

different; however, considering the flexibility, this problem can be resolved.

## 1. Introduction

Projects (of all types) can contribute almost 20% of a country's GDP (Denizer et al., 2013; World Bank, 2012). Several studies have shown that to increase the success of these projects (SGI, 2015), traditional project management approaches are gradually being replaced by flexible approaches (Ciric et al., 2019; Hidalgo, 2019; Özkan & Mishra, 2019; Wysocki, 2019) in not only the IT field (see, e.g., in Stare, 2014) but also previously unconsidered fields, such as construction (Yasaman et al., 2022) and maintenance projects (Kosztyán et al., 2019).

Broadly defined, flexibility is the magnitude of the room for scheduling decisions. (Multiple) project scheduling is open to several flexibility types; time-related or scheduling flexibility can result from slacks or topological floats (see Tavares (1999), Vanhoucke et al. (2008)) in the project plan. This type is the most obvious, and it frequently occurs even in traditional projects. In this case, the precedence relations and the implementation modes remain the same, and only the scheduled start and finish times of the tasks change. Hauder et al. (2020) shows how this flexibility can change the logistical (storing or conveying) task duration, but it can be implemented by defining the minimal and maximal time lags of an activity-on-node project network (Ren et al., 2021). The second type is activity (i.e., task) or modal flexibility, in which a task can be performed in several modes or the same result can be achieved by carrying out one of different sets of tasks and utilizing different resource combinations. These alternative (sets of) tasks are modeled by Petri nets in Čapek et al. (2012), by mandatory and optional choices in the project network (Kellenbrink & Helber, 2015), or by the AND/OR network in Tao and Dong (2018). These works extended the resource constrained (multiple) project scheduling problems (RCPSP or RCMPSP) with alternative activity chains (RCPSP-AC or RCMPSP-AC). Combined with time-related flexibility, Hauder et al. (2020) defined the problem set of the resource-constrained multiple project-scheduling problem with alternative activity chains and time-related flexibility (RCMPSP-ACTF).

The third type is dependency flexibility. If the project task technology does not require a strict sequence, some logical dependencies can be omitted. Omitting a dependency lifts the restriction of sequential execution and allows the associated tasks to be performed in parallel or in an arbitrary, relative order.

The fourth type is scope flexibility, in which some low priority tasks can be omitted or postponed to a later project. This situation reduces the resource demand and can shorten the project duration by sacrificing

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Fig. 1. Splitting a waterfall software development project into iterations by an agile project management approach.

quality or fulfillment level. The latter two flexibility types appear typically but not exclusively in agile projects (Kosztyán, 2015). Since these flexibilities affect the logical structure of a project, i.e., which tasks are performed and according to which logical dependencies are they performed, hereinafter, dependency and scope flexibility are together called structural flexibility.

While structurally flexible projects require flexible project plans, allowing the possibility of project restructuring and/or task reprioritization according to the customer's requirements, most project-planning methods assume a fixed (Franco-Duran & Garza, 2019) logic plan or a limited number of scheduling alternatives (Čapek et al., 2012; Creemers et al., 2015; Hauder et al., 2020; Kellenbrink & Helber, 2015; Servranckx & Vanhoucke, 2019; Tao & Dong, 2018). In addition, a few matrix-based methods are available for scheduling structurally flexible projects (Kosztyán, 2015; Kosztyán & Szalkai, 2020); among these, some task realizations and dependency occurrences are treated as variables during the planning phase.

In flexible, such as in agile and extreme project management, the entire project is usually split into smaller parts, called iterations or sprints in the SCRUM, KANBAN, or SCRUMBAN methodology (Wysocki, 2019). These iterations usually take 2-6 weeks. However, every iteration should be closed with a business value, called *the minimum viable product* (MVP). Therefore, an iteration can be considered a mini-project. Based on the customer's requirements, tasks must be prioritized. In addition, most tasks can be parallelized (see Fig. 1).

Fig. 1 shows an example of splitting a waterfall software development project into smaller iterations. The colorful distributions indicate that every iteration contains tasks of most phases of the software development project. It is important to note that without reconsidering the precedences between phases and functions of development, parallelization cannot be completed. It is also important to note that even though agile approaches came from the field of software development, currently, primarily not only software development is managed with agile techniques (Wysocki, 2019; Yasaman et al., 2022). Therefore, we believe that studying flexible projects will be further emphasized. In this context, it is surprising that no databases are currently available to help design and schedule (structurally) flexible projects. We believe that our study fills this gap.

Within an iteration, agile project management approaches do not allow new, so-called unplanned tasks. They have to be planned into the next iterations, while extreme project management approaches allow new tasks, which also have to be scheduled within the iterations (Wysocki, 2019). Kosztyán and Szalkai (2020) showed that in terms of scheduling flexible tasks and dependencies, there is no difference in flexibility, such as agile and extreme project scheduling approaches, which means that the same scheduling algorithm can be used for planned and unplanned tasks. Nevertheless, the rate of flexible tasks and dependencies primarily influences the scheduling performance.

The contributions to the literature and practice are summarized below.

- 1. A unified matrix-based project-planning model (UMP) is proposed to unify a set of heterogeneous single-project databases into a compound matrix-based project database (CMPD).
- 2. The proposed CMPD is complemented by the ability to model flexible dependencies and completion priorities.
- 3. Minimal, minimax, maximin and maximal structures are generated to specify the minimal and maximal demands with the proposed flexible structure generator (FSG).
- 4. Structure-related, time-related and resource-related indicators are modified to address the flexible nature of projects.

In this paper, 10 project databases, 22 datasets, and the real-life project database reported by Batselier and Vanhoucke (2015) were combined into a matrix-based project library. This paper provides a way to extend the databases to address the flexible nature of projects. This paper gives flexibility-dependent versions of the complexity and the time-related and resource-related indicators of individual projects. It also examines the effects of project flexibility.

The remainder of the paper is organized as follows. In the background section (Section 2), related works and databases are reviewed. In Section 3, first, the applied project databases and the considered complexity, time-related and resource-related indicators are introduced. Then, the flexibility-dependent indicators are specified. In Section 4, the applied project databases are compared, and the flexibility effects are examined. Section 5 discusses the results. Finally, in Section 6, we provide a summary, the limitations of this study and directions for future work.

# 2. Background

Project databases play a key role in rendering different scheduling and resource allocation methods (Brucker et al., 1999; Hartmann & Briskorn, 2010) comparable and developing new methods (Franco-Duran & Garza, 2019). Individual projects are available in various databases, such as Patterson (Patterson, 1976), SMCP and SMFF (Kolisch et al., 1995), PSPLIB (Sprecher & Kolisch, 1996), RG300 and RG30 (Debels & Vanhoucke, 2007; Vanhoucke et al., 2008), Boctor (Boctor, 1993), MMLIB (Peteghem & Vanhoucke, 2014), and the real-life project database by Batselier and Vanhoucke (2015), or sets of individual or multiple projects, including MPSPLIB (Homberger, 2007), BY (Browning & Yassine, 2010), RCMPSPLIB (Vázquez et al., 2015), and MPLIB (Van Eynde & Vanhoucke, 2020). All these databases contain tasks and dependencies between tasks and renewable resources. However, most databases do not include costs, quality or nonrenewable resources, and none of them account for flexibility issues. In addition, the source file format is heterogeneous; therefore, if a scholar wants to test a new method in multiple databases, different parsers must first be written for each project database. Heterogeneity is not simply a matter of format; tasks may be assigned different requirements, such as duration, cost, or renewable and nonrenewable resource

Table 1

Applied project databases.

Name	Project plan	Completion modes	Projects	Demands	Cited as
Patterson	Generated	Single	Single	Time, renewable resources	Patterson (1976)
PSPLIB	Generated	Single, Multiple	Single	Time, re/nonrenewable resources	Sprecher and Kolisch (1996)
RG30, RG300	Generated	Single	Single	Time, renewable resources	Vanhoucke et al. (2008)
SMCP, SMFF	Generated	Single	Single	Time, renewable resources	Kolisch et al. (1995)
Boctor	Generated	Multiple	Single	Time, renewable resources	Boctor (1993)
MMLIB	Generated	Multiple	Single	Time, re/nonrenewable resources	Peteghem and Vanhoucke (2014)
Real-life	Collected	Single	Single	Time, cost, renewable resources	Batselier and Vanhoucke (2015)
MPSPLIB	Generated	Single	Multiple	Time, renewable resources	Homberger (2007)
BY	Generated	Single	Multiple	Time, cost, renewable resources	Browning and Yassine (2010)
RCMPSPLIB	Generated	Single	Multiple	Time, renewable resources	Vázquez et al. (2015)
MPLIB1, MPLIB2	Generated	Single	Multiple	Time, renewable resources	Van Eynde and Vanhoucke (2020)

demands. In addition, several databases contain only one completion mode (namely, those of Patterson (Patterson, 1976), SMCP and SMFF (Kolisch et al., 1995), PSPLIB (Sprecher & Kolisch, 1996), RG300 and RG30 (Debels & Vanhoucke, 2007; Vanhoucke et al., 2008), and the real-life database (Batselier & Vanhoucke, 2015)), while others contain multiple completion modes (namely, PSPLIB (Sprecher & Kolisch, 1996), Boctor (Boctor, 1993), and MMLIB (Peteghem & Vanhoucke, 2014)). Table 1 summarizes the properties of the existing project databases.

To the best of our knowledge, no study has comprehensively assessed how well simulated databases describe the plurality of real projects. Some criticism has arisen regarding these simulated project databases. Peteghem and Vanhoucke (2014) reported 4 shortcomings of the widely used PSPLIB. One limitation is the low diversity in the complexity of topology networks indicated by the order strength (OS) values. The authors also found that Boctor's dataset contains mainly serial projects, and the renewable resources are hardly restricted by the constraints. In the results, the instances of the real project dataset (Protrack) are compared to the simulated ones, and the effects are evaluated by introducing flexibility to the implementation priority or precedence relations on the project properties.

The following datasets were not applied in our study, as only a part of their data could be used. However, they can still be useful for further research. The MT dataset (Vanhoucke, 2010b) is mainly used for schedule risk analysis and earned value management, contains project structures that can be combined with ResSet, have additional resource data, and result in the NetRes dataset (Vanhoucke & Coelho, 2018). DC1 (Vanhoucke et al., 2001) and DC2 (Vanhoucke, 2010a) are studied within the context of the RCPSP with discounted cash flows. The CV set (Coelho & Vanhoucke, 2020) contains RCPSP instances that are difficult to solve. MISTA2013 (Wauters et al., 2016) is a dataset and generator for the multimode resource-constrained multiple project scheduling problem (MRCMPSP) and combines instances from PSPLIB.

Other sources of projects are project generators, such as ProGen (Kolisch et al., 1995), Progen/max (Schwindt & Schwindt, 1995) and Progen/ $\pi$ x (Drexl et al., 2000), RanGen1 and RanGen2 (Demeule-meester et al., 2003; Vanhoucke et al., 2008), RiskNet (Tavares, 1999), and the random generator by Browning and Yassine (2010). These project generators have been used to generate several project databases, such as PSPLIB (Sprecher & Kolisch, 1996), RG300 and RG30 (Debels & Vanhoucke, 2007; Vanhoucke et al., 2008), MMLIB (Peteghem & Vanhoucke, 2014), and BY (Browning & Yassine, 2010). When generating a new project, only very few structure-related, time-related and resource-related indicators can be set. Therefore, numerous undiscovered and untested project structures cannot be generated by the existing project generators. Although this study does not aim to develop a new project generator, our consideration of flexibility extends the domain of the indicator values.

To unify the heterogeneous project databases, in this study, we propose a matrix-based model that can accommodate both individual and multiple projects, both single- and multimodal completions and both renewable and nonrenewable resources. Although the proposed unified matrix-based model can consider different types of projects, to ensure the comparison between the existing real-life and simulated databases, which consist mainly of single projects, only single modes are considered.

Projects are usually represented as graphs in which activities (i.e., tasks) are depicted as either arcs (activity-on-arrow [AoA] networks) (Demeulemeester et al., 1996) or nodes (activity-on-node [AoN] networks) (Ren et al., 2021). The matrix representation of projects usually describes an AoN network (Minogue, 2011). Kosztyán (2015) suggested a project domain matrix (PDM) that can be used for both single and multimodal project plans. PDMs allow mandatory and supplementary tasks with priorities and flexible dependencies between tasks. Kosztyán (2020) subsequently extended this matrix-based model to address multiple projects, programs and project portfolios. This matrix-based multiple project management model is denoted as  $M^4$ . In this study, we unified and extended  $M^4$  and PDM to consider nonrenewable resources. The proposed matrix-based method is called the *unified matrix-based project-planning model* (UMP).

The UMP contains two mandatory and four supplementary domains (see Fig. 2).

- **LD** The logic domain is an n by n matrix, where n is the number of tasks. Each cell contains a value from the [0,1] interval.
- **TD** The time domain is an n by k matrix with positive real values, where k is the number of completion modes.

The first mandatory domain is the logic domain,  $LD \in [0, 1]^{n \times n}$ . The diagonal values in LD represent the task priority values. If a diagonal value is 0, the task will not be completed, and if the diagonal value is 1, the task is mandatory. If the diagonal value is between 0 and 1, the task is supplementary, indicating that depending on the decision, it will be either completed or omitted/postponed. In the case of flexible projects, tasks are prioritized by the product owner according to their business value and the risks involved in their development (Abad et al., 2010). To help decision-makers prioritize task completion, several methods, such as MoSCoW rules, are available, and the requirements are prioritized based on their importance by sorting them into the four groups of must-have, should-have, could-have, and will-not-have features. In addition to the categories, tasks can be ranked by their importance, or the importance/priority values can be calculated by the analytic hierarchy process (AHP) method (Srivastava et al., 2021). The prioritization of task completions is an essential part of all flexible, such as agile, hybrid, and extreme project management methods. Nevertheless, in this study, only the rate of the existing supplementary (i.e., lower priority) tasks was analyzed; therefore, priority rankings were not studied. Fig. 3 shows an example of MoSCoW prioritization of requirements applied by an agile, namely, the Dynamic System Development Method (DSDM). The DSDM method was one of the first, which suggests that the MoSCoW method prioritizes task completion (Stapleton, 1997). This technique indicates that the rate of mandatory tasks should be approximately 60%. Nevertheless, the concept of task prioritization is



Fig. 2. Structure of the unified matrix-based project planning model (UMP).



Fig. 3. An example of MoSCoW of the prioritization of requirements and tasks (based on the DSDM (Stapleton, 1997)).

generally applied in most agile techniques (Dingsøyr et al., 2012; Govil & Sharma, 2021).

A task can fulfill more than one requirement (see T13); however, usually, to fulfill requirements, more than one task should be completed. In an agile project, only 'MUST (called Maximum Usable SubseT) have' tasks (appr. 60% of tasks and efforts) will be completed necessarily; the other tasks (appr. 40%) are supplementary tasks with different classes of priorities.

The out-diagonal values represent the dependencies between the tasks. If an out-diagonal value  $a_{ij} = l_{ij} = [\mathbf{LD}]_{ij}$  ( $i \neq j$ ) is 1, task *i* precedes task *j*. In the case of  $l_{ij} = 0$ , no precedence relation exists from task *i* to task *j*. If  $0 < l_{ij} < 1$ , a flexible dependency exists between task *i* and task *j*, indicating that task *i* may precede or follow task *j* depending on the manager's (algorithm's) decisions. All flexible techniques, such as agile, hybrid, or extreme techniques, require flexible dependencies between tasks (Ciriello et al., 2022; Fernandez & Fernandez, 2008).

Since none of the project networks from the considered databases contains any cycles, they can be ordered topologically, and the logic domain of the topologically ordered project networks is an upper triangular matrix (formally,  $l_{ij} = 0$  if i > j). Although the matrixbased representation does not require acyclic structures and feedback can be resolved (see, e.g., in Kosztyán, 2015) since most indicators are defined for acyclic project structures, the upper triangular logic domain is considered for the topologically ordered tasks in the rest of this study. Flexible project management allows iterations; however, the databases lack cycles; thus, we can investigate only one iteration at a time. Fig. 4 shows how to schedule prioritized tasks using the SCRUMBAN method. SCRUMBAN is a combination of SCRUM, which is the first agile method suggesting sprints (=iterations) (Hidalgo, 2019), and KANBAN, which limits parallel work-in-progress (WIP) tasks (Williams, 2010). These two techniques, SCRUM and KANBAN, are most widely used in agile project management (Wysocki, 2019).

The other mandatory UMP domain is the time-related domain. The positive values of the time domain represent the possible task durations. For each task, k types of durations can be assigned; the duration values may also match each other.

Matrix-based methods can also address general precedence relations (GPRs) (Minogue, 2011); however, most databases allow only finish-to-start (F-S) relations between tasks. F-S relations indicate that a

successor task can be started only if all predecessor tasks have been finished. In this study, we assume that tasks can only have F-S relations. The additional supplementary domains are as follows:

- **CD** The cost domain is an n by k nonnegative matrix of the task costs
- **QD** The quality domain is an *n* by *k*, nonnegative matrix of the task quality parameters, where the quality parameters are between [0,1]
- **ND** The nonrenewable resource domain is an *n* by  $k \cdot \eta$  nonnegative matrix of nonrenewable resource demands, where  $\eta$  is the number of types of nonrenewable resources.
- **RD** The renewable resource domain is an *n* by  $k \cdot \rho$  nonnegative matrix of renewable resource demands, where  $\rho$  is the number of types of renewable resources.

The optional domains can be either ignored or filled in with zero values. In this study, we always used the LD, TD and CD domains, and if there were renewable resources, the RD was also filled in, but if there was no information regarding resources, the RD was ignored. The applied database does not contain quality data; therefore, QD was omitted. The study focuses only on the structure, time-related and (renewable) resource demands; therefore, a nonrenewable domain was not used. Since the real-life database counts of the task and resource costs can also be calculated from the multiplication of resource and time demands, CD was not ignored. However, in this study, the costs were not analyzed.

If the logic domain of the UMP contains supplementary tasks and/or flexible dependencies, the minimal (maximal) makespan of the project (henceforth, the total project time [TPT]) can be specified. When the supplementary tasks and all supplementary dependencies are excluded from (included), project (Kosztyán, 2015) (see the example in Fig. 5) are called *minimal (maximal) project structures*, denoted as  $S_{\min}$  ( $S_{\max}$ ).

In the case of an early schedule, maximal (minimal) resource use occurs when all supplementary tasks are included in (excluded from) the project while all flexible dependencies are excluded from (included in) the project structure. These structures are henceforth called *maximin (minimax) project structures* denoted as  $S_{\text{maximin}}$  ( $S_{\text{minimax}}$ ) (see the left side of Fig. 5 and Eqs. (2) through (5)).



Fig. 4. Example of a schedule of prioritized tasks with the SCRUMBAN method ('X'=1 represents mandatory (MUST HAVE) tasks in diagonal, fixed dependencies in out-diagonal; 0 <'? '< 1 represents supplementary (either SHOULD HAVE or COULD HAVE)tasks in the diagonal or flexible dependencies in the out-diagonal.



Fig. 5. Minimal, maximal, minimax and maximin structures of the flexible project plan.

To indicate that the minimal, maximal, minimax and maximin structures are the results of a decision, the mandatory tasks and fixed dependencies are represented by X, while the omitted tasks and independence are represented by empty cells.

The project plan indicators can be classified into two groups. The first group characterizes the project structure, including measures of its complexity, and the second group characterizes the project time-related and resource demands.

Table 2 summarizes the indicators of the project plans (exact definitions are given in Appendices B.1–B.3).

Table 2 shows that the characterization of both the project structure and demands has several indicators. However, flexibility has no indicators, and quality and cost demands have very few indicators. None of the indicators are interval indicators. This result indicates that the result of each indicator is a scalar or, in the case of multimode completions, a vector. However, in the case of flexible projects, several possible projects have different project demands; therefore, the indicators should be specified as an interval. Appendix B contains the detailed formal description of employed and extended indicators.

#### 3. Research methods

# 3.1. Data

The different datasets and libraries mentioned in this paper were collected from the project scheduling literature. During our research, we identified suitable data sources that are commonly used and shared by scholars to evaluate scheduling approaches and find the best solutions.

The first challenge is usually accessing different datasets published by various researchers in the field. One of our intentions was also to review and collect a wide range of available data.

The second challenge arises when the data must be addressed, as they often have unique formatting and a structure that lacks proper documentation. This situation might lead to additional reverse engineering efforts that increase the research time and, of course, involve their own risks. Thus, there is a need to harmonize and integrate a wide range of datasets into a library that is accessible, is ready to process, and respects the original content. To overcome limitations, such as a lack of standardization and database integration efforts, we wrote a parser tool (a software program that reads inputs, e.g., a text file for further processing) for the most commonly used datasets found in the project-scheduling literature. The parser extracts all information from the existing libraries or the output of project generators in an automated and reproducible way. The resulting data are ready for research and analysis and, if needed, can be further adapted to various formats or platforms. Although our parser covers most available formats, the aim is to continually extend the list of supported extensions. The following two main dataset categories are considered in our study: generated and empirical (see also Table 1). Our parser was written in MATLAB and works as follows. It reviews the existing project files in search of network-related data (tasks and their precedence relations); timerelated and resource-related data, including demands and constraints, and if present, data of the costs and multiple modes of completion. Additional fields are captured from the original data files even if the input is not used directly for scheduling (e.g., the MPM-time field in the case of PSPLIB). The obtained data were then preprocessed into a matrix-based representation and saved to a MAT file that contained the data as variables. This container file can be easily loaded into MATLAB's workspace. The parser addresses renewable resource types, and the tool is designed such that it can be extended easily to use other types (e.g., nonrenewable and doubly constrained resource types). Since real-life projects and most simulated project databases contain neither these resource types nor quality parameters, these domains are not used in this study. From all parsed libraries and datasets considered, we selected datasets specifically for this paper. To allow a straightforward comparison of the different indicators, we chose only single-mode examples, and cost-related data were not considered, as these data were available in only one library.

#### Table 2 Applied indicators

Name	Short description	Adapted from	Besides single me	ode single project, app	licable for	For the results see
			single mode multi-project	multi-mode single project	multi-mode multi-project	
Structural indicate	ors					
I1	Number of nodes (i.e., tasks)	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8
12	Serial or parallel structure	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8, F11a, F14
13	Task distribution	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8
4	Rate of short arcs	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8
15	Rate of long arcs	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8
16	Topological float	Tavares (1999), Vanhoucke et al. (2008)	Х	Х	Х	F8
T-DENSITY	Total activity density	Patterson (1976)	Х	X	х	F8
XDENSITY	Average activity density	Patterson (1976)	Х	Х	Х	F8
С	Network complexity	Sprecher (1994)	Х	Х	Х	F8, F11b, F14,F16
CNC	Coefficient of network complexity	Davis (1975)	Х	Х	Х	F8
OS	Order strength	Mastor (1970)	Х	Х	Х	F8
Time related indi	cators					
TPT	Total project time		Х	Х	Х	F9
XDUR	Average activity duration	Patterson (1976)	Х	Х	Х	F9
VA-DUR	Variance in activity duration	Patterson (1976)	Х	Х	Х	F9
PCTSLACK	Percent of activities possessing positive total slack	Patterson (1976)	Х			F9
XSLACK	Average total slack per activity	Patterson (1976)	Х			F9
TOTSLACK-R	Total slack ratio	Patterson (1976)	Х			F9, F13, F15, F16
XSLACK-R	Average slack ratio	Patterson (1976)	Х			F9, F13, F15
PCTFREESLACK	Percent of activities possessing positive free slack	Patterson (1976)	Х			F9
XFREESLACK	Average free slack per activity	Patterson (1976)	Х			F9
Renewable resour	ee-related indicators					
RF	Resource factor (i.e., density of RD)	Kolisch et al. (1995)	х			F10
PCTR <sub>i</sub>	Percent of activities that require resource type j	Patterson (1976)	Х			F10
RU	Resource use	Demeulemeester et al. (2003)	Х			F10
DMND i	The average demand resource type j	Patterson (1976)	Х			F10
RC	Resource constrainedness	Patterson (1976)	х			F10, F14, F15, F1
RS	Resource strength	Kolisch et al. (1995)	X			F10
UTIL	Utilization of resources	Patterson (1976)	X			F10
ICON <sub>i</sub>	Constraints of resource <i>j</i> over time	Patterson (1976)	x			F10
OFACT i	Obstruction of resource <i>j</i>	Patterson (1976)	x			F10, F14, F15
UFACT;	Underutilization of resource <i>j</i>	Patterson (1976)	X			F10

## 3.2. Methods

Two indicator types are examined. The first group is *structural indicators*, such as complexity and flexibility indicators, which consider only the logic domain of the project domain matrices. The second group of indicators consists of *demand indicators*, which consider other domains, such as time domains (time-related indicators) and renewable resource indicators (such as renewable resource-related indicators).

An original logic structure of a project yields an activity-on-node network, which is denoted as a G = (N, A) directed graph, where  $N = \{A_1, ..., A_n\}$  ( $A_i$  is often shortened to *i*) is the set of nodes (i.e., tasks), and  $A \subset N \times N$  is the set of arcs (i.e., dependencies). n = |N| is the number of tasks, and |A| is the number of dependencies. Furthermore, the matrix representation of the logic plan is the logic domain (LD) of the UMP matrix, where  $LD \in \{0, 1\}^{n \times n}$ , for each  $i \leq n [LD]_{ii} = 1$ , and for each  $i \neq j$ , we have  $(A_i, A_j) \in A$  if and only if  $[LD]_{i,j} = 1$  (otherwise  $[LD]_{i,i} = 0$ ).

Since none of the project databases considers flexible project structures, in the first step, flexible project structures are generated. Let  $LD \in \{0, 1\}^{n \times n}$  and  $LD' \in [0, 1]^{n \times n}$  the modified logic domain as follows:

$$l'_{ij} = [\mathbf{LD'}]_{ij} := \begin{cases} u_{ij} \text{ if } l_{ij} = 1 \text{ and } v_{ij} \le fp \\ l_{ij} \text{ otherwise} \end{cases}$$
(1)

where  $l_{ij} = [\mathbf{LD}]_{ij}$  and  $u_{ij}, v_{ij} \sim U[0, 1]$  are uniformly distributed random probability variables (r.v.), and  $f p \in [0, 1]$  is a fixed flexibility parameter we set for computer runs. We want the ratio of the number of (supplementary tasks + flexible dependencies) w.r.t. the total number of LD elements is approximately f p, which is ensured by " $v_{ij} \leq f p$ ". The *weights* of these flexible objects are set by the r.v.  $u_{ij}$ . Note that  $\mathbf{LD}'$ already contains flexible dependencies ( $i \neq j$ ) and supplementary tasks (i = j). However, complexity and time-related and resource-related indicators address only fixed project structures.

The modified logic domain is used to specify only the minimal, maximal, minimax and maximin structures as follows:

$$l_{ij}^{\min} = \left[ l_{ij}' \right], \tag{2}$$
$$l_{ij}^{\max} = \left[ l_{ij}' \right], \tag{3}$$

$$l_{ij}^{\min \max} = \begin{cases} \begin{bmatrix} l_{ij}' \end{bmatrix} & \text{if } i = j \\ \begin{bmatrix} l_{ij}' \end{bmatrix} & \text{if } i \neq j \text{ and } \lfloor l_{ii}' \end{bmatrix} = \begin{bmatrix} l_{jj}' \end{bmatrix} = 1$$
(4)  

$$l_{ij}^{\max \min} = \begin{cases} \begin{bmatrix} l_{ij}' \end{bmatrix} & \text{if } i = j \\ \lfloor l_{ij}' \end{bmatrix} & \text{if } i \neq j, \end{cases}$$
(5)

where  $l_{ij}^{\min}$ ,  $l_{ij}^{\min}$ ,  $l_{ij}^{\min}$ ,  $l_{ij}^{\min}$  are the (i, j) cells of the logic domains of the minimal, maximal, minimax and maximin structures, respectively, with i, j = 1, 2, ..., n (see Fig. 5).<sup>1</sup> (<sup>)</sup>)

Minimal, maximal, minimax and maximin structures are also included in the databases. Of course, any other possible implementation structure can be specified by rounding up or down the cell values of the logic domain. However, in the case of single completion modes and the early schedule, the minimal structure provides the minimal task duration and minimal project budget, while a maximal structure provides the highest project score (widest project scope). In addition, the minimax (maximin) structure provides the highest (lowest) renewable resource demands.

To ensure comparability between the real and simulated databases, we examined primarily individual projects; however, both individual and multiple projects can be compared by calculating the average of the indicators per project. However, the calculation of most indicators differs in the single and multimode cases.

## 3.3. Structural indicators

Two structural indicator types are investigated in detail. The first group describes the rates of the flexible dependencies and supplementary tasks, and the second group describes the project structure complexity.

 $<sup>^1</sup>$  ) The  $\lceil \cdot \rceil$  ([·]) operators denote the rounding up (rounding down) of real numbers.



Fig. 6. Example of generating flexibility.

# 3.3.1. Structural flexibility

$$S-\text{SET} := \{l'_{ii} | l'_{ii} \sim P(0, 1), 0 < l'_{ii}\}$$
(6)

$$F-\text{SET} := \{l'_{ij} | l'_{ij} \sim P(0,1), i \neq j, 0 < l'_{ij}\}$$
(7)

where P(0, 1) is an arbitrary continuous distribution on interval ]0,1[. Then, we let

f p = flexibility parameter, shows the total number of flexible dependencies and supplementary tasks across all tasks and dependencies as follows:

$$fp = \frac{|F\text{-}\text{SET} \cup S\text{-}\text{SET}|}{n(n+1)/2}$$
(8)

We set  $f_p$  before the computer runs as the *approximate* ratio of flexible objects in Eq. (1), while Eq. (8) calculates the *exact* value of this ratio. Hereafter, we use this latter value of  $f_p$ .

f% = rate of flexible dependencies shows the sum of flexible dependencies across all dependencies as follows:

$$f\% = \frac{|F-\text{SET}|}{n(n-1)/2}$$
(9)

*s%* = *rate of supplementary tasks* shows the sum of supplementary (prioritized) tasks across all tasks as follows:

$$s\% = \frac{|S-\text{SET}|}{n} \tag{10}$$

Observe that  $fp = \frac{a+b}{c+d}$  if  $f\% = \frac{a}{c}$  and  $s\% = \frac{b}{d}$ , which has the notation  $\frac{a}{c} \bigoplus \frac{b}{d} = \frac{a+b}{c+d}$ . For a, b, c, d positive (which is our case)  $\frac{a}{c} \bigoplus \frac{b}{d}$  is always between  $\frac{a}{c}$  and  $\frac{b}{d}$ . Thus, fp is always between f% and s%, and all three depend only on Eq. (1). Fig. 6 shows the mechanism of generating flexibility. The left side of Fig. 6 shows the original logic domain, where the flexibility parameter is set to be 0.4. In the first step, fixed dependencies/mandatory tasks (denoted by the "X" symbol) become flexible (denoted by "?", where "?" indicates a number between 0 to 1). The right side of Fig. 6 shows the minimal structure of the project. The center of Fig. 6 shows three possible outcomes from  $\binom{10}{4}$ . Because the number of "X" symbols is 10, we have fp = 0.4.

Outcome i retains all tasks but cuts almost all dependencies, while outcome j retains only one task from the original project. In the general case, several dependencies are cut, and several tasks are omitted; see, e.g., in outcome k.

In Appendices B.1–B.3 below, we give the exact mathematical definitions of the indicators listed in Table 2. Using these indicators, we can compare the databases in Section 4, and the reader can decide based on these indicators which databases provide the closest match to the real case or problem they intend to study.

# 3.4. Applied multivariate analysis

In addition to the descriptive statistics, multivariate and network analyses were used to explore the relationships between the indicators. First, a correlation graph is specified between the indicators, represented by nodes, where the arcs represent the strength of the correlation between these nodes (i.e., indicators). The clustered correlation graph collects subsets of highly correlated indicators and groups them into a module by the Leiden method (Traag et al., 2019). In addition, the Force Atlas II (FA2) algorithm (Jacomy et al., 2014) arranges central indicators, which have many correlations between other variables, to the center of the module, and peripheral indicators are arranged at the edge of the correlation graph.

## 4. Results

#### 4.1. Descriptive statistics-Data source comparison

Table 3 shows the number of projects in the 12 datasets of the 7 project databases.

The total considered project number in a single project database was 79,875. This value was nine times greater than the original 8,875 projects. This result is due to the inclusion of both minimum and maximum structures in the database with four different flexibility parameter ( $f_p$ ) values. Most projects were derived from the MMLIBPLUS dataset (29,160) from the MMLIB database and the RG30 dataset from the RG database (16,200). The average task number within a project in the original databases was between 24 and 300 (see column  $f_p = 0$  in Table 3); this value decreased for minimal structures when the flexibility parameter ( $f_p$ ) was increased. The considered multiple project database contains 5 databases and 10 datasets. Considering demands by projects shows the same effects of increasing flexibility. Nevertheless, this database does not contain any real-life data; therefore, only simulated projects can be compared.

Fig. 7 shows the relationship between the specified rate of constraints and the observed rates of the supplementary tasks and flexible dependencies.



Fig. 7. Observed rate of the supplementary tasks (s%) and flexible dependencies (f%) by flexibility parameter rate (fp).

Table 3

Descriptive statistics of the applied project database. (a) Descriptive statistics of the single project database

Database	Set	Ν	Task nu	number mean $(\overline{I}_1)$						
			original	minima	1 structures					
			fp = 0	0.1	0.2	0.3	0.4			
Boctor	Boctor	2160	75.00	67.38	60.09	52.40	44.81			
Kolisch	SMCP	1800	29.00	26.16	23.29	20.51	17.40			
Kollsch	SMFF	4320	30.00	26.97	23.84	21.08	17.77			
	MMLIB50	4860	50.00	45.05	40.14	35.18	29.86			
MMLIB	MMLIB100	4860	100.00	89.94	80.00	70.10	59.97			
	MMLIBPLUS	29160	75.00	67.50	60.05	52.54	44.85			
Patterson	Patterson	990	24.02	21.73	19.51	16.85	14.91			
PSPLIB	j30	5760	30.00	27.14	24.08	20.86	17.91			
PSPLIB	j30sm	4320	30.00	27.06	24.02	21.11	17.78			
Real-life	PROTRACK	1125	65.56	58.83	52.09	45.50	39.78			
DC	RG30	16200	30.00	26.96	24.07	21.08	18.01			
RG	RG300	4320	300.00	270.16	240.11	210.25	180.31			
(b) Descri	ptive statistics	of the n	nultiple p	oroject da	atabase					
Database	Set	Ν	Mean of task numbers (by projects) ( $\overline{I}_1$ )							
			original minimal structures							
			fp = 0	0.1	0.2	0.3	0.4			
BY	BY	110880	60.00	53.99	47.98	42.04	35.94			
	Set 1	7497	360.00	324.08	287.95	251.59	216.39			
MPLIB1	Set 2	13167	720.00	648.13	576.42	503.87	431.86			
	Set 3	20286	1440.00	1296.34	1151.50	1007.89	863.79			
	Set 1	91125	1000.00	900.19	800.08	700.10	599.91			
MDUDO	Set 2	77760	1000.00	900.40	800.39	700.30	600.16			
MPLIB2	Set 3	77760	1000.00	900.01	799.77	700.09	599.89			
	Set 4	69120	1000.00	899.88	800.25	700.17	600.29			
MPSPLIB	MPSPLIB	1260	872.14	785.12	698.91	610.79	522.21			
RCMPSPL	B RCMPSPLIB	234	164.62	149.00	131.65	117.15	98.38			

f p is maximized to 40% for both theoretical and practical reasons. However, the expected value of f% and s% is 40% if fp% is 40%, which is in line with the guide of the DSDM (see Fig. 3), Fig. 6. indicates that a further increase in the fp% above 40% might cause all tasks to be flexible and could be omitted or postponed in the minimal structure in which only mandatory tasks are completed. In addition, since we consider an iteration (sprint) as a logic plan, the number of flexible tasks may be higher than 40%. However, on average, this number should not be greater than 40%. In the case of hybrid projects, the number of flexible tasks is less than that in agile ones; therefore, f p between 0.0 to 0.4 well simulates the traditional-hybrid-agile transitions.

Fig. 7 shows that the observed rates of the supplementary tasks and those of flexibility dependencies covered most combinations of flexibility parameters.

#### 4.2. Flexibility effects on the indicators

Fig. 8 shows a comparison of the structural indicators in the 22 datasets with 5 different flexibility parameters.

Fig. 8 shows that the considered datasets provide various complexity values. Regarding most complexity measures, such as  $I_1 - I_6$ , OS, and C, the real-life database covers the greatest intervals of the structure-related and complexity-related values, while regarding the CNC, T-DENSITY, and X-DENSITY indicators, the RG300 datasets cover the most possible values. Nevertheless, generally, the flexibility extends to the covered intervals of the structural indicators in all datasets. Nevertheless, the multiple project databases do not contain real-life databases can only be analyzed in a single project database. Therefore, we focused on a single project database; however, all results based on multiple project databases can be found in Appendix A.

Fig. 9 compares the time-related indicators of projects from the 7 single project databases and 12 datasets.

Fig. 9 also shows that the real-life database and the RG300 dataset covered most possible values of the time-related measures/indicators. Nevertheless, despite the spread of the time-related value intervals induced by Considering flexibility, the real-life database covered significantly more possible values of the time-related indicators. Without considering flexibility, any single simulated database focuses on a narrow interval of time-related indicators that can be very far from real-life project values.

Fig. 10 shows a comparison of the resource-related indicators of the projects from the 7 databases and their 12 datasets.

The difference between the simulated and real-life projects based on the resource-related indicators can also be identified in Fig. 10. Nevertheless, in contrast to the time-related indicators, Fig. 10 shows that the MMLIBPLUS dataset provided resource-related indicator values, e.g., the resource strength (RS) values, that never occur in a reallife project. For example, the number of resources (num\_r\_resources), resource constrainedness (RC), and underutilization factor (UFACT) values varied in a wider range in the real-life database. In all cases, by introducing flexibility to the project structures and including the generated minimal structures, the interval of the possible values of the structure-related, time-related, and resource-related indicators can be widened and brought closer to the values of the real-life database. We broadened the interpretation ranges of the indicators of multiple projects; see Fig. A.17 in Appendix A.

Fig. 11 compares the complexity (C) and parallelization ( $I_2$ ) values of the minimal and maximal structures regarding the ratio of flexible dependencies (f%) (marked on the horizontal axis).

Fig. 11 shows that when the flexibility parameter ( $f_p$ ) was increased via an increase in the rate of flexibility dependencies (f%) in the minimal structures, the complexity (C) decreased (see Fig. 11(a)), as did the serial completions (see Fig. 11(b)).



(a) Single project database

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# (b) Multiple project database

Fig. 8. Flexibility effects on the structural indicators.

# 4.3. Flexibility effects on indicator interdependence

Fig. 12 shows the clustered correlation graph between the indicators in the single-project database detailed in Section 3.4.

One interpretation of Fig. 12 is that several redundant indicators were highly correlated with each other. This was especially true among the topological indicators (Module 3). In comparison, the proposed (s%, f%) flexibility indicators were located on the periphery and in another module (i.e., in Module 2), suggesting that although they are related to the other indicators, they should not be merged with them. Another finding is that the modules in the simulated datasets were quite well provided with the structure-related, time-related and resource-related indicators, where the complexity (*C*), resource constrainedness (*RC*), and project duration (*TPT*)) played central roles. Furthermore, the real-life dataset provided more mixed modules. Thus, the correlation direction did not change, four modules were specified, and at least one structural indicator was included in all modules, indicating the greater importance of the structural indicators in the description of real-life projects. The separation of the three modules can also

be considered in the case of multiple projects (see Fig. A.18). When Figs. 12 and A.18 are compared, more significant differences can be observed between the simulated and real-life indicators than between the single and multiple project indicators. The multiple project database also produced three modules. Nevertheless, these modules were more mixed than those in the single-project cases.

Flexibility considerations not only expand the interval of the indicator values but also specify new value pairs for the coupled indicators. Fig. 13 shows the effect of including minimal structures on the complexity and time-related indicators. In all subfigures, the blue circles and plus signs represent the original pairs of indicator values. Fig. 13 shows the pairs of indicator values of the total slack ratio (TOTSLACK-R) and average slack ratio (XSLACK-R) as time-related indicators on the vertical axis and complexity (C) and parallelization ( $I_2$ ) as structural parameters on the horizontal axis.

Fig. 13 shows that including minimal structures helps explore new areas on the planes spanned by the structure-related and time-related indicator pairs. These combinations better cover the area of the possible value pairs. Flexibility can also be expressed in other ways as follows:



Fig. 9. Flexibility effects on the time-related indicators.



Fig. 10. Flexibility effects on the resource-related indicators.



Fig. 11. Structural changes in complexity and parallelization.

the minimal structures of flexible projects have higher average slacks, which can be better utilized in resource allocation. When the minimal structures of flexible projects are included, the domain is better covered if a combination of (1) resource-related indicators, such as the mean of resource constrainedness  $(\overline{\text{RC}})$ /the mean of the obstruction

factor ( $\overline{OFACT}$ , and (2) a structural indicator, such as complexity (C)/parallelization ( $I_2$ ), is studied (see Fig. 14).

Fig. 14 shows that while minimal structures decreased complexity (C) and increased parallelization (i.e., decreased serialization) ( $I_2$ ), they also increased the obstruction factor and resource constrainedness.



(a) For the simulated projects

(b) For the real-life database (RS, UTIL cannot be used in correlation graph)

Fig. 12. Clustered correlation graph between the indicators (Notes: Only significant correlations are represented. The correlation strengths are proportional to the tightness of the arcs between the nodes. The blue (red) arcs indicate positive (negative) correlations. Applied grouping was accomplished using the Leiden modularity-based community detection method. The nodes are represented only where there is variance).



Fig. 13. Flexibility effects on the relations between the time-related and complexity indicators.

Fig. 15 shows the relations between the slack ratios (TOTSLACK-R, XSLACK-R) and the resource-related indicators in the earliest start schedule. Considering the minimal structures of flexible projects increases the slack ratio, resource constrainedness, and the obstruction factor because of parallelization. These combinations of time-related and resource-related indicator values occurred only in flexible project plans.

Fig. 16 shows the mutual effect of flexibility on a structure-related (C), a time-related (TOTSLACK-R) and a resource-related (RC) indicator. Considering flexibility can reduce complexity (compare Figs. 16(a) and (b)), while it increases the slack ratios and reduces the resource constrainedness (RC).

#### 5. Discussion

# 5.1. Evaluation of the project library comparison

When testing project-scheduling and resource allocation algorithms only in simulated databases, two error types can be made. The first problem is whether new algorithms are applied to real-life projects that have different types of complexity (see Fig. 8, time-related (see Fig. 9) or resource-related (see Fig. 10) indicator values than simulated projects in (benchmark) databases. Even if scheduling simulated projects is more difficult for the current objectives and algorithms, these algorithms may not be prepared for the challenges of the new objectives often found in real-life projects. Creating a specified database tailored to one type of problem can cause discrepancies in real-life usage because of indirect constraints rooted in unconsidered properties. Second, if the algorithms are optimized to properties of simulated projects that never appear in real life, resources are squandered.

An interesting result is that the differences in the indicator values are much larger between simulated and real-life projects than they are between individual and multiple projects (compare Figs. 8–10 and Figs. A.17(a-b)). The relationship between the indicators illustrated by the clustered correlation graph (see Figs. 12 and A.18) also shows significantly different results, mainly between the simulated and traditional projects. We could not include a real-life multiple project database in our study, as we have not yet found one. Therefore, we must focus on the individual project databases, but we consider it



Fig. 14. Flexibility effects on the relations between the resource-related and complexity indicators.



Fig. 15. Flexibility effects on the relations between the time-related and the resource-related indicators.



Fig. 16. Alluvial diagrams of the complexity, time-related and resource-related indicators.

#### Table 4

Number of significantly different indicators between the simulated and the real-life databases (pvalue = 0.01).

Indicators	fp = 0	f p = 0.1	fp = 0.2	fp = 0.3	fp = 0.4	All
Structural	11/13	11/13	10/13	10/13	11/13	11/13
Time-related	9/9	9/9	9/9	9/9	9/9	9/9
Resource-related	9/11	8/11	8/11	8/11	8/11	8/11

essential to examine real-life projects, when possible, to study schedules. The simulated datasets should also be combined because an individual dataset usually covers only a small range of an indicator (see Figs. 8–10).

Figs. 8–10, A.17 also show that including minimal structures (see Fig. 5) widened the indicator intervals; therefore, even if flexible structures are not studied, the extended dataset may cover larger indicator intervals.

Table 4 compares the simulated and real-life databases. The indicators from the two groups, i.e., (1) a real-life database and (2) simulated datasets, were compared by ANOVA. Table 4 shows the number of indicators that had significantly different values between these groups.

When flexibility and generating minimal structures are considered, the indicator interval can be widened; therefore, this operation should be covered in the testing of project scheduling or a resource allocation algorithm to widen the scope of the application of that algorithm. Nevertheless, considering minimal structures does not solve the problem that most complexity, time-related and resource-related measures remain significantly different between the real-life and simulated databases.

Fig. 11 shows that an increase in flexibility reduces complexity and increases parallelization (decreases the task sequence length). These results are in line with the requirements of flexible project management approaches for reducing project complexity (Williams, 2010). However, Fig. 12(a) shows that especially in the simulated databases where resource constraints are prespecified, structural flexibility correlates with the resource-related indicators. For real-life projects, structural flexibility forms a separated module.

In contrast to the simulated projects, the structural flexibility indicators mainly correlated with the other structural and topological indicators; because of the lack of resource constraints, indicators RS and UTIL could not be calculated.

## 5.2. Flexibility effects on demands

Considering flexibility not only widens the indicator intervals but also specifies new demand combinations. Figs. 13–15 indicate that including minimal structures of flexible projects covered more of the domain. The new combination of indicators specified new structures that have never been tested by project scheduling and resource allocation algorithms. However, the fact that flexible projects are becoming increasingly popular implies that tasks must be prioritized and technological dependencies must be rethought. Minimal structures have the advantage of eliminating the need to use algorithms. Existing algorithms can be tested in new structures generated by the FSG. Nevertheless, maintaining flexibility values, flexible project planning and scheduling algorithms can also be tested in a large set of project databases.

## 6. Summary and conclusion

In this study, a unified matrix-based project planning model (UMP) is proposed to model heterogeneous project plans. To combine heterogeneous project databases, a compound matrix-based project database (CMPD) is proposed. In addition, a flexible structure generator (FSG) is proposed to extend the existing project databases to address possible structures of flexible project plans (see Table 5). The proposed minimal and maximal structures specify new combinations of the structural and demand indicator values to test algorithms in flexible project management environments.

As Table 5 highlights the applicability of the proposed models and methods, the UMP addresses both individual and multiple projects and single and multimodal completions. In addition, it handles renewable and nonrenewable resources, cost, and quality parameters, which are essential in real-life projects. In addition, the unified database contains both simulated and real-life data sources. The proposed parsers are prepared for single and multimode completion modes. Therefore, the proposed CMPD provides a wider range of test project schedules and resource allocation algorithms. However, to the best of our knowledge, there is no existing real-life database for multiprojects and multimodal completion modes. Therefore, the proposed model and methods cannot be tested in these types of real-life projects. The proposed parsers and generators are freely available (Kosztyán & Novák, 2022a, 2022b).

The proposed matrix-based model addresses cost and nonrenewable demands and quality parameters and manages multiple completion modes and multilevel projects. Nevertheless, to ensure the comparison between simulated and real-life projects, this study examined mainly a single-project, single-mode environment with time and renewable resource demands. The proposed matrix-based model not only unifies heterogeneous databases but also allows the user to test both traditional and flexible project-scheduling algorithms.

#### Nomenclature

Latin symbols	
$a_i(T)$	scheduled execution time interval of task $a_i$
a <sub>i</sub>	task i
D	maximal number of short arcs
$EF_i, LF_i$	early and late finish for task <i>i</i>
$ES_i, LS_i$	early and late start to task <i>i</i>
f%	rate of flexible dependencies
f p	flexibility parameter, the ratio of flexible
	dependencies and prioritized tasks to all tasks
	and dependencies
$FS_i$	free slack of task i
k	number of task completion modes
$L(i_1, i_2)$	length of an arc between tasks $i_1$ and $i_2$ ,
	i.e., the difference between their progressive
	level numbers
$\vec{L}$	longest (critical) path
$l_{ij} = [\mathbf{LD}]_{ij}$	element of the logic domain, task occurrence if
	i = j, and arc that represents the precedence
	relation between tasks <i>i</i> and $j \neq i$ (in this case,
	$l_{ij} = 1$ means task <i>i</i> precedes task <i>j</i> )
n	number of tasks
$n'_L$	number of arcs with length <i>L</i>
$\xrightarrow{m}$	maximal number of progressive levels
$\overrightarrow{P}$	task path (sequence)
$P_i$	set of immediate predecessors of task <i>i</i>
r <sub>ij</sub>	demand of task <i>i</i> for renewable resource type <i>j</i>
$r_{ij}(\tau)$	demand of task <i>i</i> for renewable resource type <i>j</i>
	at time $\tau$
<i>s</i> %	rate of supplementary tasks
$S_i$	set of immediate successors of task <i>i</i>
t <sub>i</sub>	duration of task $a_i$
$TS_i$	total slack of task <i>i</i>
$w_i$	width of progressive level $i, i = 1,, m$
Greek symbols	and lability of non-anable measures to a state
$\alpha_j$	availability of renewable resource type <i>j</i>
$\alpha_w$	total absolute deviation from the average width

Table 5

Data	Type of	Completion	UMP	UMP			FSG	Analyzed?	
source	projects	modes	Traditional	Flexible	Traditional	Flexible		Traditional	Flexible
Simulated	Single project	Single-mode	Х	Х	Х	Х	Х	Х	Х
Simulated	Single project	Multi-mode	Х	Х	Х	Х	Х	-	-
Simulated	Multi-project	Single-mode	Х	Х	Х	Х	Х	?	?
Simulated	Multi-project	Multi-mode	Х	Х	-	-	Х	-	_
Real-life	Single project	Single-mode	Х	Х	Х	Х	Х	Х	Х
Real-life	Single project	Multi-mode	-	-	-	-	-	-	-
Real-life	Multi-project	Single-mode	-	-	-	-	-	-	-
Real-life	Multi-project	Multi-mode	-	-	_	_	-	-	-

Notations: 'X' addressed, '-' not addressed, '?' partly addressed.

η	number of types of nonrenewable resources
ρ	number of types of renewable resources
Calligraphic	
symbols	
$\mathcal{A}$	set of arcs (dependencies)
$ \mathcal{A} $	number of dependencies in a project structure
S	project structure, set of (to-be-) realized tasks
$\vec{s}$	project schedule of project structure S
Abbreviations	
CD	cost domain of the UMP
CMPD	compound matrix-based project database
FSG	flexible structure generator
LD	logic domain of the UMP
TD	time domain of the UMP
QD	quality domain of the UMP
ND	nonrenewable resource domain of the UMP
PDM	project domain matrix
PL	progressive level
RD	renewable resource domain of the UMP
RL	regressive level
UMP	unified matrix-based project-planning model

#### CRediT authorship contribution statement

Zsolt T. Kosztyán: Conceptualization, Methodology, Software, Writing – original draft, Writing – review & editing. Gergely Novák: Data curation, Software, Writing – review & editing. Róbert Jakab: Investigation, Validation. István Szalkai: Methodology, Writing – review & editing. Csaba Hegedűs: Writing – review & editing.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

# Data availability

All data and parsers can be downloaded from Code Ocean. The links to approved codes are incorporated in the revised manuscript.

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## Appendix A

See Figs. A.17 and A.18.

#### Appendix B. Formal description of employed indicators

## B.1. Structural complexity

We denote *S* as a realized project structure,  $\mathbf{LD} \in \{0, 1\}^{n \times n}$  of *S*,  $|\mathcal{A}| = \sum_{i \neq j} l_{ij} (l_{ij} = [\mathbf{LD}]_{ij})$  is the total number of dependencies (arcs) between tasks.

 $I_1$ , the number of tasks (nodes), is calculated as follows:

$$I_1 := n \tag{B.1}$$

 $I_2$ , the serial-parallel structure, measures the closeness to a serial or parallel completion. For  $I_2$ , we need the following notations:  $S_i(P_i)$  denotes the *set* of immediate successors (predecessors) of task *i*. For topologically ordered, acyclic project networks,  $|S_i| = \sum_{j=i+1}^{n} l_{ij}$ ,  $|P_i| = \sum_{j=1}^{i-1} l_{ji}$ . The progressive ( $PL_i$ ) and regressive ( $RL_i$ ) level *numbers* of each task *i* can be calculated as follows:

$$PL_{i} := \begin{cases} 1 & \text{if } P_{i} = \emptyset \\ \max_{j \in P_{i}} PL_{j} + 1 & \text{if } P_{i} \neq \emptyset \end{cases}$$
(B.2)

and

$$RL_{i} := \begin{cases} m & \text{if } S_{i} = \emptyset \\ \min_{j \in S_{i}} RL_{j} - 1 & \text{if } S_{i} \neq \emptyset \end{cases}$$
(B.3)

where  $m = \max_i PL_i$ . Next, we have the following:

$$I_2 := \begin{cases} 1 & \text{if } n = 1\\ \frac{m-1}{n-1} & \text{if } n > 1 \end{cases}$$
(B.4)

 $I_3$ , the task distribution, measures the distribution of tasks over the progressive levels by calculating the total absolute deviations.

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(a) The effects of flexibility for time-related indicators



(b) The effects of flexibility for resource-related indicators

Fig. A.17. Flexibility effects on demand-related indicators among multiple projects.

First, we define the *j*th progressive *level* of j = 1, ..., m as follows:  $\mathbf{PL}_j := \{i \le n : PL_i = j\}$ , i.e., the *set* of all tasks having progressive level number *j*. Then,

$$I_{3} := \begin{cases} 0 & \text{if } m = 1 \text{ or } m = n \\ \frac{\alpha_{w}}{\alpha_{\max}} = \frac{\sum_{j=1}^{m} |w_{j} - \overline{w}|}{2(m-1)(\overline{w} - 1)} & \text{if } 1 < m < n \end{cases}$$
(B.5)

where  $w_j = |\mathbf{PL}_j|$  is the width (size) of progressive level j = 1, ..., m,  $w = (w_1, w_2, ..., w_m)$  is the vector containing the widths of each progressive level, and  $\overline{w} = n/m$ ,  $\alpha_w$  is the total absolute deviation from the average width. Then,  $\alpha_{\max}$  is the maximal value of  $\alpha_w$  of a network (ranging for all possible  $\mathcal{A}$ ); thus,<sup>2</sup>)

 $\alpha_{\max} = (m-1)(\overline{w}-1) + (n-m+1-\overline{w}) = 2(m-1)(\overline{w}-1).$ 

 $I_4$ , the ratio of *short* arcs. The length of an "arc" (called a path in graph theory) between tasks  $i_1$  and  $i_2$  is defined as  $L(i_1, i_2) :=$  $|PL_{i_1} - PL_{i_2}|$ , the difference between their progressive level numbers. Arcs of length 1 are called *short*, and  $D := \sum_{j=1}^{m-1} w_j \cdot w_{j+1}$  is the *maximal* number of short arcs.  $n'_L$  denotes the number of arcs of length L for  $1 \le L \le m-1$ . Then,  $I_4$  is calculated as follows:

$$I_4 := \begin{cases} 1 & \text{if } D = n - w_1 \\ \frac{n_1' - n + w_1}{D - n + w_1} & \text{if } D > n - w_1 \end{cases}$$
(B.6)

<sup>&</sup>lt;sup>2</sup>) The maximal value of  $\alpha_w$  is achieved (*n* and *m* are fixed,  $\sum_{j=1}^m w_j = n$ ) when all levels are singletons, except for one with n - (m - 1) tasks; repetitive

use of the inequality  $|a - \overline{w}| + |b - \overline{w}| < |a - 1 - \overline{w}| + |b + 1 - \overline{w}|$  for  $1 < a \le \overline{w} \le b < n$  proves this extrema.



Fig. A.18. Clustered correlation graph of the multiple project database indicators. (Note: Indicators indicate the average values for a project.

 $I_5$ , the ratio of *long* arcs (L > 1), is calculated as follows:

$$I_{5} := \begin{cases} 1 & \text{if } |\mathcal{A}| = n - w_{1} \\ \frac{\left(\sum_{L=2}^{m-1} n'_{L} \frac{m-L-1}{m-2}\right) + n'_{1} - n + w_{1}}{|\mathcal{A}| - n + w_{1}} & \text{if } |\mathcal{A}| > n - w_{1} \end{cases}$$
(B.7)

 $I_6$ , the topological float, considers the differences between the regressive and progressive level numbers of task *i*, i.e.,  $|RL_i - PL_i|$ , as follows:

$$I_{6} := \begin{cases} 0 & \text{if } m \in \{1, n\} \\ \frac{\sum_{i=1}^{n} |RL_{i} - PL_{i}|}{(m-1)(n-m)} & \text{if } m \notin \{1, n\} \end{cases}$$
(B.8)

CNC, the coefficient of network complexity, is calculated as follows:

$$CNC = \frac{|\mathcal{A}|}{n} \tag{B.9}$$

OS, the order strength, is calculated as follows:

$$OS = \frac{|A|}{n(n-1)/2}$$
(B.10)

C, the network complexity, is calculated as follows:

$$C = \begin{cases} \frac{\log \frac{|A|}{n-1}}{\log \frac{n^2-1}{4(n-1)}} & \text{if } n \text{ is odd} \\ \frac{\log \frac{|A|}{n-1}}{\log \frac{n^2}{4(n-1)}} & \text{if } n \text{ is even} \end{cases}$$
(B.11)

T-DENSITY, the total activity density, is calculated as follows:

T-DENSITY := 
$$\sum_{i:=1}^{n} \max\left\{0, |P_i| - |S_i|\right\}$$
 (B.12)

( $S_i$  and  $P_i$  were defined immediately before  $I_2$ .)

XDENSITY, the average activity density, is calculated as follows:

$$XDENSITY := \frac{T - DENSITY}{n}$$
(B.13)

Flexibility-related structural indicators. All structural indicators depend on the realized structure (*S*), i.e., on the set of included flexible dependencies and supplementary tasks from  $\mathbf{LD}' \in [0, 1]^{n \times n}$ .  $I_1 =$ number of tasks; therefore,  $I_1(S_{\min}) = I_1(S_{\min\max}) \le I_1(S) \le I_1(S_{\max}) =$  $I_1(S_{\max\min})$ . Nevertheless, since the fixed dependencies between the supplementary tasks must be excluded if the supplementary tasks are excluded, the minimal (maximal) structures are the lower (upper) bounds of C. The CNC and OS indicators of these cases are those in which only mandatory tasks exist. Regarding the other structural indicators, the connection between them and the maximal–minimal structures are not obvious, and no such rules can be defined.

## B.2. Time-related indicators

To ensure the validity of the comparison of the simulated and real-life datasets, only networks with single modes are considered. Therefore, only the single-mode version of the indicators was considered. We denote *S* as a realized project structure that determines the nonmandatory tasks and dependencies from  $\mathbf{LD}' \in [0, 1]^{n \times n}$ . In the following, all quantities depend on *S*, but we omit indicating *S* everywhere. For example, *S* determines  $\mathbf{LD}'' \in \{0, 1\}^{n'' \times n''}$  from  $\mathbf{LD}' \in [0, 1]^{n \times n}$ , However, we simply denote  $\mathbf{LD}''$  and n'' by  $\mathbf{LD}$  and *n*, similarly for **TD**, and  $|\mathcal{A}| = \sum_{i < j} l_{ij} (l_{ij} = [\mathbf{LD}]_{ij})$ . We denote  $t_i := [\mathbf{TD}]_{ii}$  as the duration of task *i* and  $\vec{P} = \}a_1 < a_2 < \ldots < a_N \varepsilon$  is a path of preceding tasks, where  $a_j < a_{j+1}$  indicates  $l_{a_j,a_{j+1}} = 1$  for  $1 \leq j < N$  ( $N \leq n$ ).  $\ell(\vec{P}) := N$  is the *length* of the path, and  $d(\vec{P}) := \sum_{i \in \vec{P}} t_i$  is the *duration* of path  $\vec{P}$ . A path  $\vec{L}$  is called the *longest* or *critical* path if  $d(\vec{L})$  is maximal among all paths. Next, the TPT, the total project time, is calculated as follows:

$$\Gamma PT := d(\vec{L}) \tag{B.14}$$

for any longest path  $\vec{L}$ .  $\vec{X}$ DUR, the average task duration, is calculated as follows:

$$\overline{X}\text{DUR} := \frac{1}{n}\sum_{i=1}^{n}t_{i}$$
(B.15)

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VA-DUR, the variance in task duration, is calculated as follows:

VA-DUR := 
$$\frac{1}{n-1} \sum_{i=1}^{n} \left( t_i - \overline{X} DUR \right)^2$$
 (B.16)

PCTSLACK, the percent of tasks with positive total slack, is calculated as follows:

$$\text{PCTSLACK} := \frac{1}{n} \sum_{i=1}^{n} \begin{cases} 1 & \text{if } LS_i - ES_i > 0\\ 0 & \text{if } LS_i - ES_i = 0 \end{cases}$$
(B.17)

where  $LS_i$  ( $ES_i$ ) is the latest (earliest) start time, and  $TS_i := LS_i - ES_i$  is the total slack of task *i*.

XSLACK, the average total slack per task, is calculated as follows:

$$XSLACK := \frac{1}{n} \sum_{i=1}^{n} TS_i$$
(B.18)

TOTSLACK-R, the total slack ratio, is calculated as follows:

$$TOTSLACK-R := \frac{\sum_{i=1}^{n} TS_i}{TPT}$$
(B.19)

XSLACK-R, the average slack ratio, is calculated as follows:

$$XSLACK-R := \frac{XSLACK}{TPT}$$
(B.20)

PCTFREESLK is the percent of tasks with positive free slack. First, the earliest finishing time of task *j* is  $EF_j = ES_j + t_j$ ; then, we denote  $FS_i := \min_{l_{ij}=1} ES_j - EF_i$  the free slack of task *i* (lowest early start of successors - early finish). Here, we have the following:

PCTFREESLK := 
$$\frac{1}{n} \sum_{i=1}^{n} \begin{cases} 1 & \text{if } FS_i > 0 \\ 0 & \text{if } FS_i = 0 \end{cases}$$
 (B.21)

XFREESLK, the average free slack per task, is calculated as follows:

$$XFREESLK := \frac{1}{n} \sum_{i=1}^{n} FS_i$$
(B.22)

*Flexibility impacts of the time-related indicators.* Since the average task duration and variance in activity duration depend on the inclusion/ exclusion of tasks but not on their dependencies (see (B.15) and (B.16)), the following equations are easy to verify:

$$\overline{X}\text{DUR}(S_{\text{max}}) = \overline{X}\text{DUR}(S_{\text{maximin}})$$
(B.23)

 $\overline{X}\text{DUR}(S_{\min}) = \overline{X}\text{DUR}(S_{\min})$ (B.24)

$$VA-DUR(S_{max}) = VA-DUR(S_{maximin})$$
(B.25)

$$VA-DUR(S_{\min}) = VA-DUR(S_{\min})$$
(B.26)

*Large samples.* Large samples refer to large *n* for which we can use the central limit theorem (CLT). Here, we offer some mathematical results regarding  $\overline{X}$ DUR(*S*). Similar results are also used for resource indicators, such as RF, PCTR, RU, DMND, and RC in Eq. (B.38).

*XDUR*(*S*) contains (finally) mandatory tasks only; thus, we may consider  $S \subseteq I_n$ , where we denote  $I_n := \{1, 2, ..., n\}$  and let s = |S|.

In the following, we assume that *n* and *s* are large numbers,  $t_i \sim U(a, b)$  (for  $i \in \mathbb{I}_n$ ) are uniform random variables (**r.v.**) on the *fixed* finite interval  $[a, b] \subset \mathbb{R}$ , and  $t_i$  are independent and identically distributed (**i.i.d.**) r.v.

**STEP ONE:** *n* and *S* are fixed. Next,  $\overline{X}DUR(S)$  is the mean of *s* i.i.d. uniform r.v., and thus, the CLT yields the following:

$$\frac{XDUR(S) - \mu}{\frac{\sigma}{\sqrt{s}}} \sim \Phi(0, 1)$$
(B.27)

where:

$$\mu = E\left(\overline{X}DUR(S)\right) = \frac{a+b}{2} \quad , \quad \sigma = D(\overline{X}DUR(S)) = \frac{|b-a|}{\sqrt{12}} \tag{B.28}$$

and  $\Phi(0, 1)$  is the standard normal distribution<sup>3</sup>).

**STEP TWO:** *n* is fixed, but *S* may be any nonempty subset of  $\mathbb{I}_n$ , i.e., the event space is currently the power set of  $\mathbb{I}_n$ :  $\Omega = \mathcal{P}(\mathbb{I}_n)$ . Next, we consider  $\overline{X}DUR(S)$  on  $\Omega$  and use the notation  $\overline{X}_{DUR}$  instead of  $\overline{X}DUR(S)$ . The probability of any *S* is  $\frac{1}{n!}$ ,  $E(\overline{X}_{DUR}[S]) = \mu$  and  $D\left(\overline{X}_{DUR}[S]\right) = \frac{\sigma}{\sqrt{s}}$  when s = |S|, which has the probability  $\binom{n}{s}/2^n$ ; thus, we have the following:

$$D\left(\overline{\mathcal{X}}_{DUR}\right) = \sqrt{\frac{1}{2^n} \sum_{s=1}^n \binom{n}{s} \left(\frac{\sigma}{\sqrt{s}}\right)^2} = \sigma \sqrt{\frac{1}{2^n} \sum_{s=1}^n \frac{\binom{n}{s}}{s}}$$
(B.29)

Finally, by CLT, we obtain the following:

$$\frac{\overline{X}DUR(S) - \mu}{D\left(\overline{X}_{DUR}\right)} \sim \Phi(0, 1)$$
(B.30)

In the case |S| is limited, i.e.,  $c \le |S| \le d$  is required for some fixed  $c \le d \le n$ , (B.29) becomes the following:

$$D\left(\overline{\mathcal{X}}_{DUR}\right) = \sigma \sqrt{\frac{1}{2^n} \sum_{s=c}^d \frac{\binom{n}{s}}{s}}$$
(B.31)

#### B.3. Resource-related indicators

We denote *S* as a realized project structure and  $\mathbf{LD} \in \{0, 1\}^{n \times n}$ ,  $\mathbf{T} \in \mathbb{R}^{n}_{+}$  and  $\mathbf{RD} \in \mathbb{R}^{n \times \rho}_{+}$  domains of the matrix representation of *S*, where *n* is the number of tasks and  $|\mathcal{A}| = \sum_{ij,i \neq j} l_{ij} (l_{ij} = [\mathbf{LD}]_{ij})$  We denote  $t_i = [\mathbf{TD}]_{ii}$  as the duration of task *i*, TPT as the duration of the project, and  $r_{ii} = [\mathbf{RD}]_{ii}$  as the resource demand of task *i* of resource *j*.

 $\vec{S}$  is a project *schedule* of project structure *S* if for each realized task  $a_i \in S$ , the interval  $T_i \subseteq [0, \text{TPT}]$  is determined when  $a_i$  is addressed (scheduled). To ensure compatibility with other papers, we use the redundant notation  $a_i(T) \in \vec{S}$ .

We denote  $S(a_i(T)) \in [0, TPT - t_i]$  the start and  $F(a_i(T)) \in [t_i, TPT]$ the finish time of task *i*. The early schedule, denoted as  $\vec{S}_{\min}$ , satisfies  $\forall a_i(T) \in \vec{S}_{\min} S(a_i(T)) = \text{ES}_i$  and  $F(a_i(T)) = \text{EF}_i$ . We denote the *resource demand j* of task *i* at time  $\tau$  as follows:

$$r_{ij}(\tau) := \begin{cases} r_{ij} \text{ if } a_i(T) \in \vec{S}, \tau \in T_i \\ 0 \text{ otherwise} \end{cases}$$
(B.32)

Furthermore, we denote the total (renewable) resource *demand* of *j* at time  $\tau$  as  $r_j(\tau) = \sum_i r_{ij}(\tau)$ ,  $\tau \in [0, \text{TPT}]$ .

#### B.3.1. Nonscheduled

RF, the resource factor, is the density of **RD**, the resource matrix from a domain mapping matrix (DMM). RF gives the rate of how often resources required are from all possible resource type-activity pairings. Higher RF values indicate a more complex scheduling problem.

$$RF := \frac{1}{n\rho} \sum_{i=1}^{n} \sum_{j=1}^{\rho} \begin{cases} 1 & \text{if } r_{ij} > 0\\ 0 & \text{otherwise} \end{cases} = \frac{1}{\rho} \sum_{j=1}^{\rho} PCTR_j$$
(B.33)

where  $r_{ik}$  denotes the amount of resource type *j* required by task *i*, and PCTR<sub>*j*</sub> denotes the percent of activities that require the given resource type, which gives a columnwise view of RF as follows:

$$PCTR_j := \frac{1}{n} \sum_{i:=1}^n \begin{cases} 1 & \text{if } r_{ij} > 0\\ 0 & \text{otherwise} \end{cases}$$
(B.34)

RU, the resource use, represents the resource use for each activity, i.e., the number of resource types used. RU varies between 0 and r (the number of resource types). It is a rowwise view of RF (i = 1, ..., n) as follows:

$$\mathrm{RU}_{i} := \sum_{i=1}^{p} \begin{cases} 1 & \text{if } r_{ij} > 0\\ 0 & \text{otherwise} \end{cases}$$
(B.35)

 $<sup>^3</sup>$  ). In the denominator of (B.27), one may write  $\sqrt{\text{VA-DUR}(S)}$  instead of  $\frac{\sigma}{\sqrt{s}}$  .

 $\text{DMND}_j$  is the average quantity of resource *j* demanded when required by an activity (*j* = 1, ...,  $\rho$ ) as follows:

$$DMND_{j} := \frac{\sum_{i=1}^{n} r_{ij}}{\sum_{i=1}^{n} \begin{cases} 1 & \text{if } r_{ij} > 0\\ 0 & \text{if } r_{ij} = 0 \end{cases}}$$
(B.36)

RC is the resource constrainedness of each resource type and is calculated as follows:

$$\mathrm{RC}_j := \frac{\mathrm{DMND}_j}{\alpha_j} \tag{B.37}$$

where  $\alpha_i$  is the *availability* of renewable resource type *j*.

*Flexibility impacts on the nonscheduled renewable resource indicators.* The nonscheduled resource-related indicators are independent of the schedule. Therefore, they are independent of the rate of flexible dependencies.

All possible structures can be considered a random sample from the maximal structure if the elements of S-SET follow a uniform distribution. In this case, the following formula can be specified:

$$\frac{\text{NRI}(S) - Exp(\text{NRI}(S))}{\sqrt{Var(\text{NRI}(S))}} \sim \Phi(0, 1)$$
(B.38)

where NRI(S) denotes any mean of the nonscheduled resource indicators, such as RF, PCTR, RU, DMND, and RC for project structure S.

#### B.3.2. Resource-related indicators for the early schedule

The following indicators from (Patterson, 1976) require early scheduling ( $\vec{S}_{min}$ ) of the activities regarding the precedence relations but not the resource constraints.

RS is the resource strength of each renewable resource type and is calculated as follows:

$$RS_j := \frac{\alpha_j - r_j^{\min}}{r_j^{\max} - r_j^{\min}}$$
(B.39)

where  $\alpha_j$  denotes the total availability of renewable resource type *j*,  $r_j^{\min} := \max_{i=1,...,n}(r_{ij})$  is the highest *individual* resource demand, and  $r_j^{\max}$  denotes the peak total demand at any moment for resource type *j* in the precedence preserving the earliest start schedule.

UTIL<sub>j</sub> is the utilization (rate) of resources and is measured based on the critical path length. Higher values indicate more constraints, less room for scheduling, and less possibility of changing the task starting times without increasing the TPT.

$$\text{UTIL}_j := \frac{\sum_{i=1}^n r_{ij} t_i}{\alpha_j \cdot \text{TPT}}$$
(B.40)

 $\text{TCON}_{j}$  is the constrainedness of (renewable) resource type j over time. In practice, it is the average utilization (UTIL<sub>j</sub>) considering only those tasks that use that particular resource type as follows:

$$TCON_{j} := \frac{\sum_{i=1}^{n} r_{ij}t_{i}}{\alpha_{j} \cdot TPT \cdot \sum_{i=1}^{n} \begin{cases} 1 & \text{if } r_{ij} > 0\\ 0 & \text{otherwise} \end{cases}}$$
(B.41)

 $OFACT_j$  is the obstruction factor of (renewable) resource type *j* and is calculated as follows:

OFACT<sub>j</sub> := 
$$\frac{\int_{0}^{1r_{1}} \max\{0; r_{j}(\tau) - \alpha_{j}\} d\tau}{\sum_{i=1}^{n} r_{ij}t_{i}}$$
 (B.42)

UFACT, is the underutilization factor and is calculated as follows:

UFACT<sub>j</sub> := 
$$\frac{\int_{0}^{1r_{1}} \max\{0; \alpha_{j} - r_{j}(\tau)\} d\tau}{\sum_{i=1}^{n} r_{ij} t_{i}}$$
 (B.43)

трт

Interval of the scheduled resource indicators. Since the minimax (maximin) structure requires minimal (maximal) resource demands, the following equations can be specified.

$$\text{SRI}_{j}(S_{\text{minimax}}) \le \text{SRI}_{j}(S) \le \text{SRI}_{j}(S_{\text{maximin}})$$
 (B.44)

$$SRI(S_{minimax}) \le SRI(S) \le SRI(S_{maximin})$$
 (B.45)

where  $SRI_j$  denotes the scheduled resource indicators, such as RS, UTIL, TCON, OFACT, and UFACT, of resource *j*, and SNI denotes the mean of a scheduled resource indicator of all resource types.

*Resource indicator mean.* Since the number of resource demands is very heterogeneous, in this study, the mean of the resource indicators was considered instead of calculating the values of all resources. Moreover, to ensure the comparability of the resource indicators, when the resource numbers differ across projects, we must use the means of these indicators.

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