

First determination of β -delayed multiple neutron emission beyond $A = 100$ through direct neutron measurement: The P_{2n} value of ^{136}Sb .

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Background: β -delayed multiple neutron emission has been observed for some nuclei with $A \leq 100$, being the ^{100}Rb the heaviest $\beta 2n$ emitter measured to date. So far, only 25 P_{2n} values have been determined for the ≈ 300 nuclei that may decay in this way. Accordingly, it is of interest to measure P_{2n} values for the other possible multiple neutron emitters throughout the chart of the nuclides. It is of particular interest to make such measurement for nuclei with $A > 100$ to test the predictions of theoretical models and simulation tools for the decays of heavy nuclei in the region of very neutron-rich nuclei. In addition, the decay properties of these nuclei are fundamental for the understanding of astrophysical nucleosynthesis processes such as the r -process, and safety inputs for nuclear reactors.

Purpose: To determine for the first time the two neutron branching ratio, P_{2n} value, for ^{136}Sb through a direct neutron measurement, and to provide precise P_{1n} values for ^{136}Sb and ^{136}Te .

Method: A pure beam of each isotope of interest was provided by the JYFLTRAP Penning trap at the Ion Guide Isotope Separator On-Line (IGISOL) facility of the University of Jyväskylä, Finland. The purified ions were implanted into a moving tape at the end of the beam line. The detection setup consisted of a plastic scintillator placed right behind the implantation point after the tape to register the β -decays, and the BELEN detector, based on neutron counters embedded in a polyethylene matrix. The analysis was based on the study of the β - and neutron-growth-and-decay curves and the β -one-neutron and β -two-neutron time correlations, which allowed us the determination of the neutron-branching ratios.

Results: The P_{2n} value of ^{136}Sb was found to be 0.14(3)% and the measured P_{1n} values for ^{136}Sb and ^{136}Te were found to be 32.2(15)% and 1.47(6)%, respectively.

Conclusions: The measured P_{2n} value is a factor 44 smaller than predicted by the finite-range droplet model plus the quasiparticle random-phase approximation (FRDM+QRPA) model used for r -process calculations.

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I. INTRODUCTION

The β decay Q value (Q_β value) increases when going towards neutron-rich nuclei in the chart of nuclides. This makes β^- decay the dominant decay mode for this region. In very neutron-rich nuclei, the emission of one

or more neutrons may also occur after a β -decay. This process of β -delayed neutron (βn) emission was discovered in 1939 by Roberts et al. [1] and is energetically allowed when the $Q_{\beta n}$ value is positive, i.e. the Q_β value of the decay exceeds the neutron separation energy (S_n) of the daughter nucleus. This phenomenon becomes dominant when the populated state in the daughter nucleus, following the β -decay, is higher in excitation energy than S_n , which gets lower going towards neutron-rich nuclei in the chart of nuclides. When the populated

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states lie even higher than the two-neutron separation energy, S_{2n} , i.e. $Q_{\beta 2n} > 0$, two neutron emission may also occur. This phenomenon was predicted in 1960 by Goldansky [2]. The first studies of multiple-neutron emission were carried out in the 1980s in which detection of two-neutron emission was observed for nuclei up to mass $A=33$ and predictions for the emission of three neutrons were made for masses around $A=100$ [3]. The β -delayed two-neutron ($\beta 2n$) emission probability, P_{2n} value, has only been experimentally determined for 25 isotopes (two of them only approximations) [4] of out of ≈ 300 potential multiple neutron emitter candidates [5]. The importance of providing more precise data for neutron emitting isotopes has been highlighted by the IAEA Coordinated Research Projects in Refs. [6] and on *β -delayed neutron emission evaluation* [7]. The latter emphasizes the importance of these data for safety improvement purposes for emerging nuclear power reactors, as well as for astrophysical studies. Indeed, these experimental data, involving isotopes in the neutron-rich region, are needed to achieve a better knowledge of the “freeze-out” of the rapid neutron capture (r -process) [8] when theoretical calculations of nucleosynthesis [9–11] are applied. The delayed neutron emission is an important input for these models as it shifts the final isobaric solar system abundances of some species to lower masses, and introduces neutrons in the stellar environment that can be re-captured by other nuclei at later stages. This is of special interest in the regions of the r -abundance peaks such as $A \approx 130$ near the doubly-magic ^{132}Sn isotope ($N=82$ and $Z=50$). Up to now, the P_n data available for the heavy mass region is scarce, especially above $A = 150$ [12], and non-existent for multiple neutron emitters above $A = 100$.

This paper presents a measurement of the P_{2n} neutron branching ratio for ^{136}Sb . With a $Q_{\beta 2n}$ window of 1884(6) keV [5], ^{136}Sb has been suggested to be a multiple-neutron emitter in several theoretical models [13–15] and by some experiments: these include estimates based on the Finite Fermi-system theory [16] and more recently an experiment involving several isotopes of mass $A = 136$ in which the isobars could not be separated well enough to determine their neutron branching ratios precisely [17]. In order to get a successful measurement of multiple β -delayed neutron emission, we used a high efficiency neutron detector and a beam free from contamination of other isotopes. The pure ^{136}Sb beam was obtained with the Penning trap mass spectrometer, JYFLTRAP, at the Ion Guide Isotope Separator On-Line (IGISOL) facility [18, 19], located in the Accelerator Laboratory of the University of Jyväskylä, Finland (JYFL). This contribution describes the experimental setup in Section II, the details of the data analysis following the methodology reported in [20] and the results in Sec. III. A summary and discussion are presented in Sec. IV, and the conclusions are given in Sec. V.

II. EXPERIMENTAL SETUP

The experiment presented in this paper was carried out at the IGISOL facility of JYFL. The isotopes of interest were produced in nuclear fission induced with a 25 MeV proton beam, with an intensity of around 7-10 μA , impinging on a natural uranium target. The fission fragments produced were extracted from the helium gas cell using a sextupole ion guide (SPIG) [21] and differential pumping, accelerated to 30 keV and mass-separated with a dipole magnet. The continuous beam was cooled and bunched using an RFQ cooler-buncher device [22] before injecting the ions into the JYFLTRAP double Penning trap. The purification took place in the first trap, where a mass-selective buffer gas cooling technique [23] was employed to resolve different isobars based on their cyclotron resonance frequencies $\nu_c = qB/(2\pi m)$, where q and m are the charge and the mass of the ion of interest and B is the magnetic field strength inside the trap. The description and the principles of the JYFLTRAP at IGISOL are reported in Ref. [24], and Figs. 1 and 2 of Ref. [25] detail the layout of the IGISOL facility.

In this experiment, pure ion beams of ^{95}Rb , ^{137}I , ^{136}Te and ^{136}Sb were extracted from the trap without isobaric contaminants and transported to the implantation system. ^{95}Rb and ^{137}I were used for calibration purposes, as their P_{1n} values are well known from previous experiments [26–28]. The implantation system consisted of a moving magnetic tape placed inside an aluminum tube, with a thickness of 1 mm and diameter of 46 mm, under vacuum. This tube linked JYFLTRAP and the end of the beamline, shown in Fig. 1. The moving tape sys-

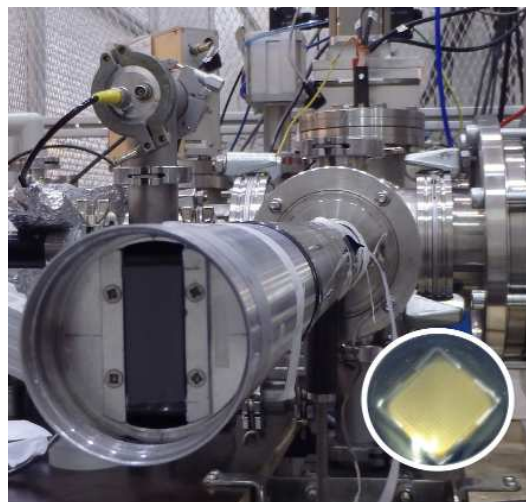


FIG. 1. (Color online) Aluminum tube linking JYFLTRAP and the end of the beamline. The rear side of the moving tape at the implantation position can be seen. The plastic scintillator detector used as a β decay counter, shown in the bottom-right, was placed 6 mm behind the moving implantation tape at the end of the aluminum tube.

tem allowed control of the ion-implantation (beam on) and decay (beam off) times according to the half-life of the isotope measured, in order to be able to reproduce the growth-and-decay curves in the analysis (see Section III). The detection system in this experiment consisted of a 3 mm-thick plastic scintillator β counter, shown in Fig. 1 (bottom-right), placed at the end of the vacuum tube, surrounded by the Beta dELayEd Neutron (BELEN) detector [29–31]. The latter consisted of 48 ^3He counter tubes of 2.54 cm diameter manufactured by LND Inc. [32], distributed in three concentric rings, and embedded in a high-density polyethylene (HDPE) matrix to moderate the neutrons, see Fig. 2. BELEN was surrounded by 20 cm of HDPE shielding in order to moderate and absorb neutrons scattered from the surroundings (see also Fig. 2). Table I summarizes its characteristics.

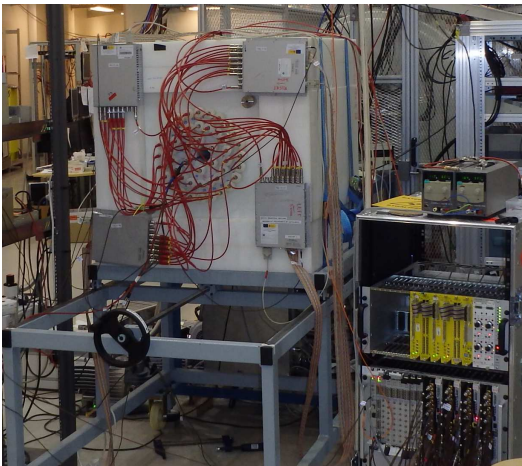


FIG. 2. (Color online) The BELEN detector embedded in the high-density polyethylene (HDPE) matrix and shielding, and the data acquisition system.

TABLE I. Characteristics of the BELEN detector (units in millimeters)

	Central		Ring	
	hole	Inner	Middle	Outer
Position (diameter)	60	120	230	340
Number of counters (10 atm)		0	8	0
Number of counters (8 atm)		6	10	24

The version of the BELEN detector used in this experiment was specifically designed and optimized by means of Monte Carlo MCNPX [33–36] and GEANT4 [37, 38] simulations in order to achieve a high and flat efficiency detection in the range from 0.1–2 MeV (see Fig. 3). The most important constraint was in terms of efficiency: for the detection of two correlated neutrons, the efficiency, ε_{2n} , is roughly proportional to the square of the detection

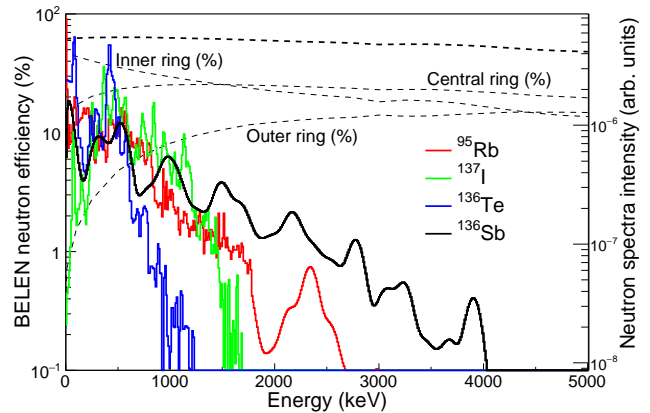


FIG. 3. BELEN detector efficiency from the GEANT4 simulation: total efficiency and for each one of the 3 rings of ^3He proportional counters (dashed lines) [38], and neutron spectra of the measured isotopes (from ENSDF [39]) as a function of the neutron energy (colored lines). See text and Table I for details.

efficiency for a single neutron, ε_{1n} :

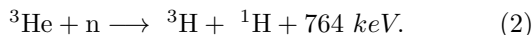
$$\bar{\varepsilon}_{2n} \approx \bar{\varepsilon}_{1n}^2 \quad (1)$$

To avoid a low detection probability the central hole of BELEN was kept at 6 cm diameter, restricted to the diameter size of the vacuum tube of the implantation system. With this geometry, BELEN reached a one-neutron efficiency of $\approx 60\%$, and $\approx 36\%$ for a two-neutron event, in the $Q_{\beta n}$ energy range of the isotopes of interest. The disadvantage of this optimization compared to other designs was the impossibility of placing a high-purity germanium (HPGe) detector right behind the implantation point to verify the identity of the isotope implanted by γ -ray detection. This latter technique was used in the prior experiment during the same experimental campaign with another version of the BELEN detector, measuring isotopes in the same region of the nuclear chart [40]. The one-neutron efficiency for that version of BELEN detector was 40% in the same energy range (0.1–2 MeV) due to a different geometry, while using the same number of ^3He neutron counters. For the present work, the efficiency obtained in the simulations, shown in Fig. 3, was experimentally validated at $E_n=2.13$ MeV using a ^{252}Cf source, and with beams of isotopes with well-known P_{1n} values, such as ^{95}Rb and ^{137}I , as reported in Section III.

Previous experiments using the BELEN detector demonstrated that it works well with the self-triggered data acquisition system specifically implemented for BELEN, named *GASIFIC* [20, 41]. This system integrates all signals from the β - and the ^3He neutron counters recording their energy, and a time-stamp with a clock of 10 ns resolution to be able to build the β -neutron time-correlations over a certain time-window. In this

experimental campaign, differential to single-ended converter modules, designed at JYFL, were added in the electronic chain. This made possible to link the output signals from the MPR-16-HV Mesytec preamplifiers, directly connected to the ^3He tubes, to the SIS3316 [42] sampling ADC modules in the data acquisition system [40]. This improvement enabled the recording of the data without requiring the signal shapers used in previous experiments.

Regarding the response of the neutron detection system, the energy spectrum obtained for the neutron events comprises the range from a low-energy threshold at 191 keV up to the 764 keV peak. This energy is attributed to the kinetic energy released in the reaction:



The 764 keV peak corresponds to the sum of the collection of the total energy released by the two reaction products, a triton and a proton. The lower energy detection threshold is related to the partial collection of the energy and the wall effect [43]. Gain-matching with a calibrated ^{252}Cf source was carried out for all 48 ^3He counters before the experiment. The stability of the overall detector response was checked regularly during the experiment. The accumulated spectrum for all 48 tubes during the ^{136}Sb measurement is shown Fig. 4. The latter includes the uncorrelated neutron events, which were removed in the data analysis process together with other light particles and the noise at lower energies.

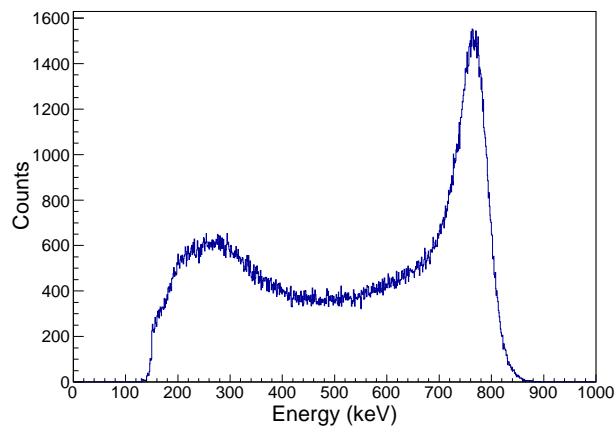


FIG. 4. BELEN energy spectrum acquired with the 48 ^3He tubes for the ^{136}Sb measurement.

III. DETERMINATION OF THE NEUTRON BRANCHING RATIOS

The equation that describes the total β -delayed neutron branching probability, P_n , of a nucleus is defined

as the sum of all, single and multiple, neutron emission contributions present in the decay:

$$P_n = \sum_{x=1}^N P_{xn} \quad (3)$$

For nuclei with only one-neutron emission energetically allowed, i.e. $Q_{\beta n} > 0$ and $Q_{\beta 2n} < 0$, the P_n value is equal to P_{1n} . This is the case for the ^{95}Rb , ^{137}I , and ^{136}Te isotopes measured in this experiment. In order to determine their P_{1n} values, we followed the methodology successfully implemented in a previous experiment with a similar setup at the IGISOL facility [20] in which the P_{1n} values were deduced as:

$$P_{1n} = \frac{\bar{\varepsilon}_\beta}{\bar{\varepsilon}_n \bar{\varepsilon}_\beta'} \frac{N_{\beta 1n}}{N_\beta} \quad (4)$$

where $N_{\beta 1n}$ is the number of the net β and neutron time-correlated events, N_β the number of β decays registered, $\bar{\varepsilon}_\beta$ is the mean β efficiency, $\bar{\varepsilon}_\beta'$ the averaged β efficiency above the S_n weighted according to the $Q_{\beta n}$ and the neutron energy spectrum range (see Fig. 5), and $\bar{\varepsilon}_n$ the neutron efficiency (see Fig. 3).

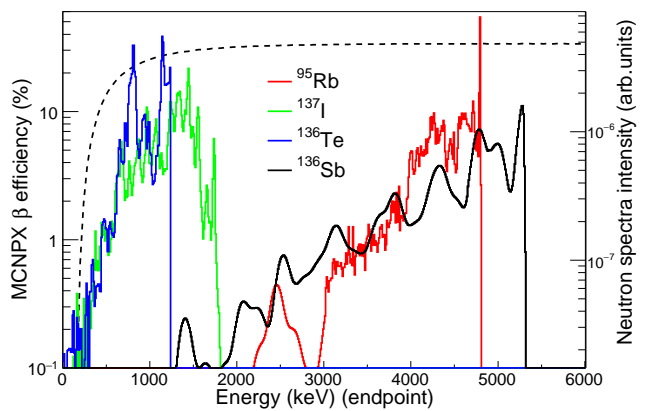


FIG. 5. The MCNPX simulation of the β counter efficiency (dashed line), and electron endpoint energies from the neutron energy spectra of the measured isotopes (colored lines) [39]. The lower β efficiency at low energies affects the detection of correlated βn events for those isotopes with a low Q_{β} value (see text for details).

The analysis of the acquired data directly provides three parameters that are needed to evaluate and determine the neutron branching ratios. These are the number of β particles and the number of neutrons detected, together with the βn time-correlation events. Figure 6 shows the analysis to determine the β and neutron integrals for each measured isotope, ^{95}Rb , ^{137}I , ^{136}Te , and ^{136}Sb , from the growth-and-decay curves, using the Bateman equations [44]. The particular growth (implantation) and decay times in the curves were precisely set according to the half-lives, taken from the literature [39], of

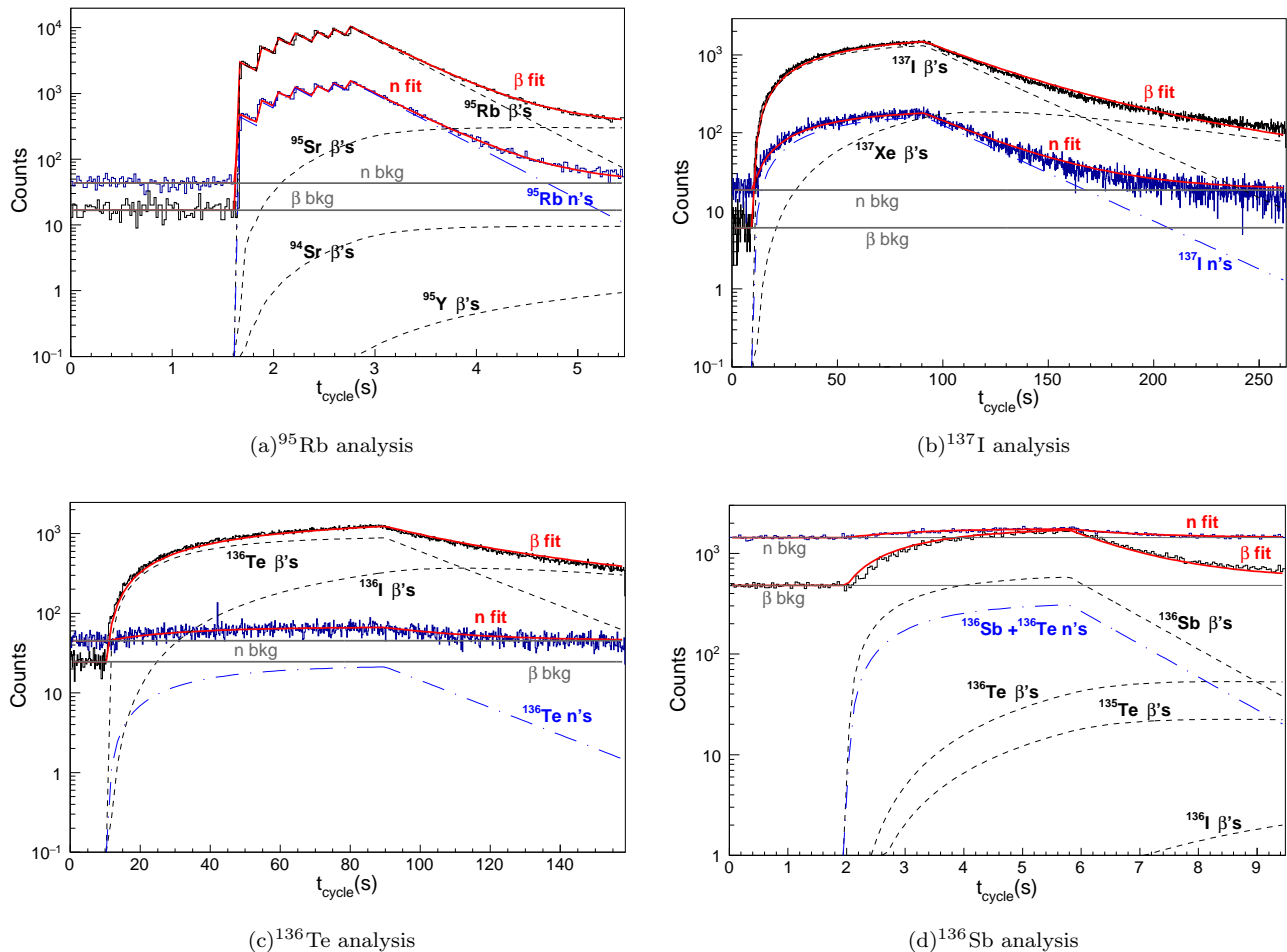


FIG. 6. Analysis of the β and neutron events accumulated during the implantation-and-decay cycles in the growth-and-decay curves for each isotope measured. In the analysis of ^{137}I (b) the fit function also includes a parameter to reflect the loss of the xenon isotopes in the chain. As xenon is a noble gas, a fraction of the nuclei rapidly escape from the implantation tape. Details of this effect are presented in Ref. [20]. In the case of ^{95}Rb (a) the trap purification cycle can be identified. In all cases the ions were extracted from the trap in bunches, once in every 181 ms according to the length of this cycle. This was repeated as many times as needed during the “beam on” time. So the beam was not continuous but rather a quasi-continuous.

the isotopes present in the decay chain. The flat area at the beginning of the timing cycle (see fig. 6) corresponds to the characterization of the β and neutron background. Table II provides the Q_β values of interest together with half-lives and the details of their implantation and decay cycle times. The numerical results from Fig. 6 for the precursor isotopes are shown in later tables.

In the present work ^{137}I and ^{95}Rb beams were used as calibration isotopes because of their well-known P_{1n} values [26–28]. In addition, these two isotopes have very different neutron energy spectra (see Fig. 3). In the case of ^{95}Rb , its neutron energy spectrum is mainly centered at lower energies, with a large $Q_{\beta n}$ value of 4.8 MeV. This indicates that the lower β detection probability at lower energies (see Fig. 5) does not miss βn correlated events in the analysis. Therefore, assuming $\bar{\varepsilon}_\beta \approx \bar{\varepsilon}'_\beta$ in Eq. 4, it is possible to determine its P_{1n} value to a first

TABLE II. Half-lives [39] and Q_β values [4] of the investigated isotopes and characteristics of the implantation-and-decay cycle, corresponding to the growth-and-decay curves (see Fig. 6).

Nuclei	^{95}Rb	^{137}I	^{136}Te	^{136}Sb
$t_{1/2}$ (s)	0.3777(8)	24.5(2)	17.63(8)	0.923(14)
Q_{β^-} (keV)	9228(20)	6027(8)	5120(14)	9916(7)
$Q_{\beta n}$ (keV)	4881(20)	2002(8)	1292(6)	5147(7)
$Q_{\beta 2n}$ (keV)	-1951(20)	-6082(8)	-6509(15)	1884(6)
Impl. time (s)	1.27	81.3	79.5	3.80
Decay time (s)	2.54	171.5	68.5	3.71

approximation with the equation:

$$P_{1n} \simeq \frac{1}{\bar{\varepsilon}_n} \frac{N_{\beta 1n}}{N_\beta} \quad (5)$$

The resulting P_{1n} value for ^{95}Rb , considering a constant $\bar{\varepsilon}_n$ value of 62.98%, taken from the simulation and weighted with the neutron spectrum, is 8.6(4)%, in agreement with the literature value of 8.94(37)% [28]. On the other hand, ^{137}I has a neutron spectrum spread over the whole energy range up to its endpoint at ≈ 2 MeV (see Fig. 3). In this case its analysis is affected due to the non-constant β efficiency at low energies (see Fig 5), and the simplified expression detailed in Eq. 5 is not accurate enough. Thus, we defined an expression to avoid the $\bar{\varepsilon}_\beta$ and $\bar{\varepsilon}_\beta'$ dependence in Eq. 4 as in Ref. [20], using the total number of detected neutrons, N_n , independently of the coincidence or not with the β s:

$$P_{1n} = \frac{\bar{\varepsilon}_\beta}{\bar{\varepsilon}_n} \frac{N_n}{N_\beta}, \quad (6)$$

from which, it is then possible to determine the $\bar{\varepsilon}_n/\bar{\varepsilon}_\beta$ ratio with the well-known P_{1n} values of the ^{95}Rb and ^{137}I calibration isotopes. The ratio obtained can be used to determine the remaining P_{1n} values in this experiment. Table III summarizes the integral values of the βn correlated events, the number of β events, N_β , and the number of neutrons, N_n , for the ^{95}Rb and ^{137}I measurements, together with the calculated $\bar{\varepsilon}_n/\bar{\varepsilon}_\beta$ ratio.

TABLE III. The experimental values measured for ^{95}Rb and ^{137}I and their respective $\bar{\varepsilon}_\beta/\bar{\varepsilon}_n$ ratio.

Nuclei	$P_{1n}(\%)$	$N_{\beta n}$	N_β	N_n	$\bar{\varepsilon}_n/\bar{\varepsilon}_\beta$
^{95}Rb	8.94(37) [28]	33011	610229	90445	1.66(7)
^{137}I	7.66(14) [28]	21888 ^a	592009	72031	1.59(3)

^a Biased value due to the lower $\bar{\varepsilon}_\beta$ at lower energies.

The average of the $\bar{\varepsilon}_n/\bar{\varepsilon}_\beta$ ratio, calculated from ^{95}Rb and ^{137}I measurements in Table III, is 1.62(7). As these two isotopes have large Q_β values this ratio value is expected to be alike. Thus, we assume that this value also applies for all the other isotopes measured in this experiment.

A. The P_{1n} value of ^{136}Te

With a $Q_{\beta n}$ value of 1292(6) keV, ^{136}Te has an energy window that allows β -delayed one-neutron emission. In this case the expected energy spectrum of the emitted neutrons is also affected by the non-constant $\bar{\varepsilon}_\beta$ at low energies described above for ^{137}I . Thus, the equation to determine its neutron branching ratio can be defined by

Eq. 6, using the $\bar{\varepsilon}_n/\bar{\varepsilon}_\beta$ ratio determined with the calibration isotopes. With the integral values obtained in the analysis of the growth-and-decay curves in Fig. 6, the analysis yields a P_{1n} of 1.47(6)%. This value is slightly higher but in fair agreement with those reported in the literature and the IAEA evaluation: 1.31(5)% [26, 28] and 1.26(20)% [27]. Using the simplified Eq. 5, with the βn correlated detected events derived from the analysis of Fig. 7, the P_{1n} value would be 0.90(5)%. Comparing

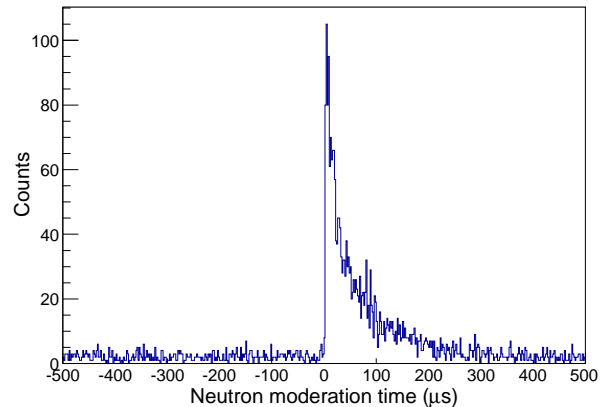


FIG. 7. $\beta 1n$ correlation events for the ^{136}Te analysis. The 2630 forward and 548 backward events were registered during the experiment. According to the βn background level on the left side, the neutron moderation time in the polyethylene for this experiment was determined to be 500 μs .

this value with the one obtained using the efficiency ratio correction we observe an increase of about 63%. This gives an idea of the fraction of correlated events missed because of the lower $\bar{\varepsilon}_\beta$ at low energies when measuring an isotope with a neutron energy spectrum such as ^{136}Te (see Fig. 5). The acquired data for this isotope in this measurement were recorded for 165 cycles which included a background measurement of 10 s, an implantation time of 79.5 s, and a decay time of 68.5 s for each one, giving 158.5 s per cycle (see Fig. 6 and Table II), i.e. 7.3 h of beamtime. A total of 2082 net $\beta 1n$ correlated events were registered for this isotope. The values of this analysis are reported in Table IV.

TABLE IV. ^{136}Te and ^{136}Sb neutron emission probability results.

Nuclei	$N_{\beta 1n}$	$N_{\beta 2n}$	N_β	N_n	$P_{1n}(\%)$	$P_{2n}(\%)$
^{136}Te	2082	-	360655	8645	1.47(6)	-
^{136}Sb	9328	21.8	57590	30455 ^a	32.2(15)	0.14(3)

^a Includes the 1n and 2n events from ^{136}Sb , and 1n events from ^{136}Te .

B. P_{1n} and P_{2n} values of ^{136}Sb

As described in Section I, when the state populated after the β decay is higher than the two-neutron separation energy, S_{2n} , in the daughter nucleus ($Q_{\beta 2n} > 0$), double neutron emissions are allowed. This is the case for ^{136}Sb with $Q_{\beta 2n}=1884(6)$ keV. Its measurement in this experiment comprised 26465 recorded implantation-and-decay cycles of 9.51 seconds (≈ 3 days). As can be observed in Fig. 6, in each cycle the first 2 s were used to characterize the β and neutron background. Table II details the implantation-and-decay cycle times. The neutron branching ratios of this isotope have two contributions to the P_n (Eq. 3): the P_{1n} and the P_{2n} values.

In order to determine its neutron branching ratios, several steps are necessary. Eq. 7 describes the total number of neutrons, N_n , after background subtraction:

$$N_n = N_{1n}(^{136}\text{Sb}) + 2N_{2n}(^{136}\text{Sb}) + N_{1n}(^{136}\text{Te}). \quad (7)$$

As can be seen the total number of neutrons has contributions from the one- and two-neutron emission branching ratios of ^{136}Sb plus a small contribution from its daughter ^{136}Te . The latter is present in the decay chain and the relevant number of neutrons can be determined with the information extracted from the ^{136}Sb β -decay analysis (Fig. 6) and its P_{1n} value. In order to calculate the contributions of one-neutron and two-neutron events from the ^{136}Sb decay in Eq. 7, we define the following expressions:

$$N_{1n(^{136}\text{Sb})} = \bar{\epsilon}_n P_{1n} \frac{N_\beta}{\bar{\epsilon}_\beta} + 2 \times \bar{\epsilon}_n (1 - \bar{\epsilon}_n) P_{2n} \frac{N_\beta}{\bar{\epsilon}_\beta} \quad (8)$$

and

$$N_{2n(^{136}\text{Sb})} = \bar{\epsilon}_n^2 P_{2n} \frac{N_\beta}{\bar{\epsilon}_\beta} \quad (9)$$

These expressions relate the number of β events, N_β , and neutron events, N_{xn} , and their detection efficiency, to the unknown P_{1n} and P_{2n} values. However, from the available information, the analysis only provides the net number of N_β events for each one of the species in the decay chain, and the net number of the total neutron events, N_n , after background subtraction. Firstly, we attempted to determine the net number of two-neutron correlations, N_{2n} , from the decay of ^{136}Sb subtracting the two-neutron correlations determined in a background run. As shown in Fig. 8, this method is not useful because of the large uncertainty in the background subtraction. The large background can be associated with different kinds of interactions between particles, either cosmic rays or reactions of the beam with materials, and the BELEN detector.

Therefore, the strategy to determine the neutron branching ratios was based on the evaluation of the direct $\beta 2n$ and $\beta 1n$ correlation events recorded in the data analysis. Figures 9 and 10 show, respectively, the $\beta 2n$

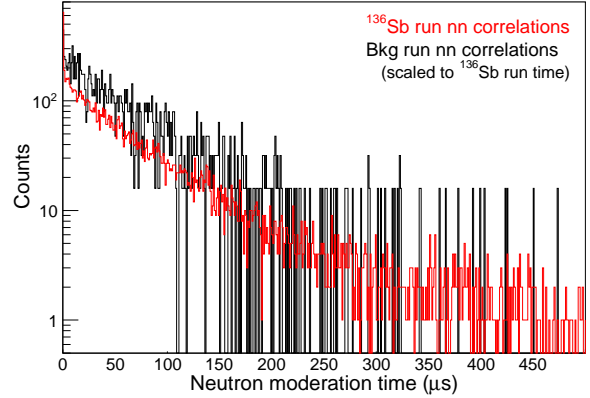


FIG. 8. (Color online) Background level evaluation of double neutron events, N_{2n} , for the ^{136}Sb setting. As can be observed, the number of events in a background measurement is of the same order as in the setting of interest. See text for details.

and $\beta 1n$ time-correlation events registered within a neutron moderation time-window of 500 μs . In the analysis

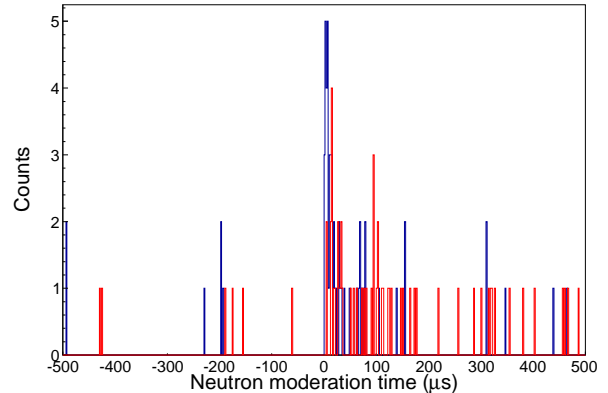


FIG. 9. (Color online) ^{136}Sb $\beta 2n$ correlation events. In blue are shown the first correlated neutrons after a β decay, in red the second neutrons in the correlation. A total of 55 forward events were recorded, in which are included several background contributions (see text for details).

of the $\beta 2n$ correlation were registered 55 forward events, $N_{\beta 2n}^f$, and 6 backward events, $N_{2n\beta}$, corresponding to the number of two accidental neutrons in the neutron moderation time-window. In order to evaluate the total background contributions present in the 55 $\beta 2n$ detected events, we assume that the neutron rates are the same within the neutron moderation time-window, before and after a β decay. For the case of two neutrons accidentally correlated per detected β , we define the parameter r_{2n} as the number of backward time-correlations, $N_{2n\beta}$, and the total number of β -decays, N_β , obtained from Fig. 6

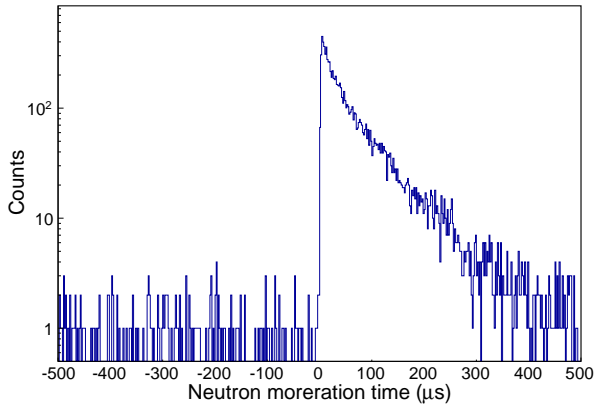


FIG. 10. $\beta 1n$ correlation for the ^{136}Sb analysis. A total of 9494 forward and 168 backward events were registered. Beyond the calculation to determine the number of $\beta 1n$ net events, the background rate in this $\beta 1n$ channel is relevant in the determination of the truly $\beta 2n$ events. (See text for details).

and reported in Table IV:

$$r_{2n} = \frac{N_{2n\beta}}{N_{\beta}}. \quad (10)$$

The amount of events contributing due to this r_{2n} rate includes all β decays except those coming from the $\beta 1n$ and $\beta 2n$ events, i.e. $r_{2n} \times (N_{\beta} - N_{\beta 1n} - N_{\beta 2n})$. However, according to the measured values, we can assume that $N_{\beta} \gg N_{\beta 1n} \gg N_{\beta 2n}$, and the background from this β -2n channel is approximately of $r_{2n}N_{\beta}$. Another relevant background contribution comes from the detection of one accidental neutron inside the same correlation time-window of a truly correlated neutron. In this case we define the parameter r_{1n} as the $\beta 1n$ backward time-correlations, $N_{1n\beta}$, as obtained in the analysis presented in Fig. 10, and the total number of β -decays N_{β} from Fig. 6:

$$r_{1n} = \frac{N_{1n\beta}}{N_{\beta}}. \quad (11)$$

In addition, this β -1n background channel has also contributions from those neutrons in the β -2n channel in which one of the neutrons has not been detected. This can be estimated with the neutron efficiency factor defined as:

$$r_{\epsilon} = \frac{(1 - \epsilon_n)}{\epsilon_n}, \quad (12)$$

being the total contribution of the one neutron channel as $r_{1n} \times (N_{\beta 1n} + 2 \times r_{\epsilon}N_{\beta 2n})$. To summarize, Eqs. 13 and 14 describe the system that relates the number of measured $\beta 1n$ and $\beta 2n$ (forward) events, $N_{\beta 1n}^f$ and $N_{\beta 2n}^f$, with the true events, $N_{\beta 1n}$ and $N_{\beta 2n}$, and background contributions, assuming $N_{\beta} \gg N_{\beta 1n} \gg N_{\beta 2n}$:

$$N_{\beta 1n}^f \approx (1 - r)(N_{\beta 1n} + 2r_{\epsilon}N_{\beta 2n}) + r_{1n}N_{\beta} \quad (13)$$

$$N_{\beta 2n}^f \approx (1 - r)N_{\beta 2n} + r_{2n}N_{\beta} + r_{1n}(N_{\beta 1n} + 2r_{\epsilon}N_{\beta 2n}) \quad (14)$$

where r is the sum of all accidental neutrons per detected β , $r = r_{1n} + r_{2n} + r_{3n} \dots$, which are added on each particular background channel in the latter equations. In this measurement, this sum was simplified considering that $r_{1n} \gg r_{2n} \gg r_{3n}$, and only the first two contributions were taken into account. Solving the system presented in Eqs. 13 and 14, the resulting values for the $N_{\beta 2n}$ and $N_{\beta 1n}$, in the ^{136}Sb measurement, are 21.8 and 9328 respectively. The method described above is presented in detail in Ref. [45] within the BRIKEN Project [46].

If we were to assume that the mean energy of the neutron spectrum is not affected by the lower ϵ_{β} at low energies, the P_{2n} value could be calculated with a simplified expression such as Eq. 15, analogously to Eq. 5 used for the case of ^{95}Rb for its P_{1n} value:

$$P_{2n} = \frac{1}{\bar{\epsilon}_n^2} \frac{N_{\beta 2n}}{N_{\beta}} \quad (15)$$

With this assumption, the P_{2n} value would be 0.10(2)%. However, due to the expected low $\bar{\epsilon}_{\beta}$ in the energy region of interest for the two-neutron energy spectrum ($Q_{\beta 2n}$ value = 1884(6) keV, see Fig. 5), it is necessary to apply the correction based on the $\bar{\epsilon}_{\beta}'$ (Eq. 16) in the same way as Eq. 4 for the case of one-neutron emission (see Section III):

$$P_{2n} = \frac{1}{\bar{\epsilon}_n^2 \bar{\epsilon}_{\beta}'} \frac{N_{\beta 2n}}{N_{\beta}} \quad (16)$$

The unknown neutron energy spectrum for the ^{136}Sb two-neutron emission suggests the use of the calculated $\bar{\epsilon}_{\beta}'$ value for ^{137}I , as its $Q_{\beta n}$ value, 2002 keV, is very close to the ^{136}Sb $Q_{\beta 2n}$ value. So, using the $\bar{\epsilon}_n/\bar{\epsilon}_{\beta}'$ coefficient, 1.62(7), previously determined, the P_{2n} value is calculated to be 0.14(3)%. Having obtained the P_{2n} , the P_{1n} value, has been determined to be 32.2(15)%.

IV. SUMMARY AND DISCUSSION

The P_{1n} and P_{2n} values obtained in this work are summarized in Table V together with the previously available experimental values and theoretical predictions from several models, including the finite-range droplet model plus the quasiparticle random-phase approximation (FRDM+QRPA) [13], the density functional theory plus continuum QRPA plus relativistic QRPA(DF3+cQRPA+RQRPA) [47, 48], the Koura-Tachibana-Uno-Yamada (KTUY) [49], the relativistic Hartree-Bogoliubov plus RQRPA (RHB+RQRPA) [50], the QRPA plus Hartree-Fock (QRPA-HF) [51], and the semi-empirical effective density model [52]. The P_{1n} value obtained for ^{136}Te , 1.47(6)%, is higher but in fair agreement with those reported in Refs. [26, 27] and [28].

TABLE V. Results

Isotope	$t_{1/2}$ (s) [39]	Experimental		Technique	Date and Ref.	Theory			Model	Ref.
		P_{1n} (%)	P_{2n} (%)			$t_{1/2}$ (s)	P_{1n} (%)	P_{2n} (%)		
$^{136}_{52}\text{Te}^{84}$	17.63(8)	1.47(6)	-	β, n	(This work)	10.166	2.43	0.0	FRDM+QRPA	[13]
		1.26(20)	-	β, n	(2002) [27]	21.189	1.80	-	DF3+cQRPA+RQRPA	[48]
		1.31(5)	-	β, n	(1993) [26]	0.600	0.41	-	KTUY	[49]
		1.7(8) ^a	-	Fission, β, n	(1978) [53]	0.548	0.4	0.1	RHB+RQRPA	[50]
		0.7(4)	-	Fission, n	(1977) [54]	-	2	0	QRPA-HF	[51]
		1.31(5)	-	Evaluation	(2018) [28]	-	2.8	0.0	Semi-empirical	[52]
$^{136}_{51}\text{Sb}^{85}$	0.923(14)	32.2(15)	0.14(3)	β, n	(This work)	1.998	33.5	6.19	FRDM+QRPA	[13]
		-	1.4(2) ^b	β, n	(2011) [17]	0.8	10.5(51)	4.15(1.05)	DF3+cQRPA+RQRPA	[14]
		19.5(18)	-	β recoil	(2015) [55]	0.760	33.20	0.0	KTUY	[49]
		23.2(68)	-	β, n	(2002) [27]	0.175	3.8	0.2	RHB+RQRPA	[50]
		16.3(32)	-	β, n	(1993) [26]	-	30.0	0	QRPA-HF	[51]
		33(40) ^a	-	Fission, β, n	(1978) [53]	-	37.3	0.0	Semi-empirical	[52]
		44(57) ^a	-	Fission, n	(1977) [54]	0.46	17.1	0.28	Microscopic Finite	[16]
		18.7(18)	<1 ^c	Evaluation	(2018) [28]				Fermi-system theory	

^a Updated values from the evaluation performed in Ref. [26].

^b Measurement with $A = 136$ isobaric contamination.

^c Based on preliminary results of this study.

Concerning ^{136}Sb , the analysis yields a P_{1n} value of 32.2(15)%. This is higher than previous experimental results also taken from Refs. [26, 27] and [28]. In the case of the P_{2n} we have obtained a value of 0.14(3)%. This is one order of magnitude lower than the 1.4% estimated in a measurement with isobaric contamination [17], and the predictions of the FRDM+QRPA and the DF3+cQRPA+RQRPA models.

As shown in Table V, the values of most of the theoretical predictions are far from the experimental values. Some of them are compatible for ^{136}Sb but not for ^{136}Te , and vice versa. With the current results it is not easy to decide which of the models reproduces better the experimental results. The DF3+cQRPA [14, 48] approaches better the magnitudes of the P_{1n} and half-life for ^{136}Te , but in the case of ^{136}Sb , although the predicted half-life is close to the experimental value, it underestimates P_{1n} value and overestimates the P_{2n} value. The model which better reproduces the ^{136}Sb data is the KTUY [49] but the half-life predicted for ^{136}Te remains far from the experimental value. Regarding the QRPA-HF [51] model, it is the one which better reproduces the P_{1n} and P_{2n} values for both isotopes according to the obtained experimental results.

To date, several calculations and estimates for multiple-neutron emission beyond $A=100$ have also been reported. Table V reports the available ones for the isotopes measured in this study. Some of them follow

the main theoretical models describing the strength functions and some others are estimates and extrapolations like [52]. Concerning experimental measurements, there is a recent P_{2n} value reported for ^{140}Sb [56]. This value was determined through an indirect measurement based on relative intensities of γ -rays observed from transitions that were identified as belonging to ^{138}Te . The value reported is “*about*” 8% and no uncertainty was given. This suggests again the need for direct neutron measurements in order to obtain more precise data on neutron emission branching ratios.

V. CONCLUSIONS AND OUTLOOK

We have determined the neutron branching ratios for ^{136}Te and ^{136}Sb through a direct neutron measurement. This represents the first experimental multiple-neutron emission value above $A=100$ and an improvement for the values available so far for these isotopes. As discussed above, some of the theoretical predictions agree well with the values obtained, but none shows agreement for all of the parameters present in the decay. This, together with the discrepancies with the experimental data available, indicates that more measurements with pure beams and direct neutron detection are needed in order to provide further input for the models in this region, and to study the nuclear properties above the neutron separation energies. Consequently, this experimental campaign in which six more isotopes included in the IAEA priority list for

reactor physics [57] were also measured [40], and present and future campaigns like BRIKEN [46] are an opportunity to increase the amount of data available in this field.

It is also of interest to determine whether the two neutrons are emitted simultaneously or sequentially in the β -delayed two neutron-emission process. In the first case an angular correlation between both neutrons and the γ -ray emitted by the final nucleus would be expected. In the second case it would be necessary to correlate these events with very narrow time-windows to be able to confirm the phenomenon. In this work we were not able to address this question because of the moderation of the neutrons in the polyethylene matrix and the statistics available.

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