

# Introduction to TEM and electron diffraction in the TEM

*János L. Lábár*

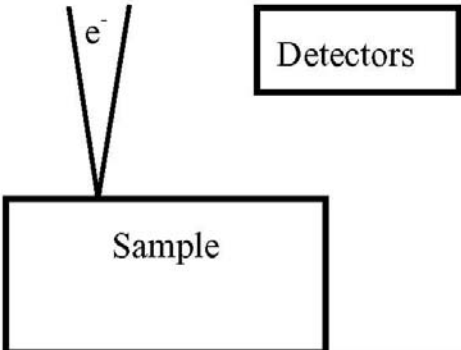
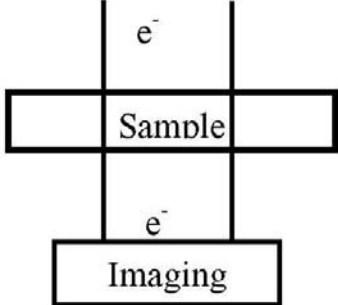
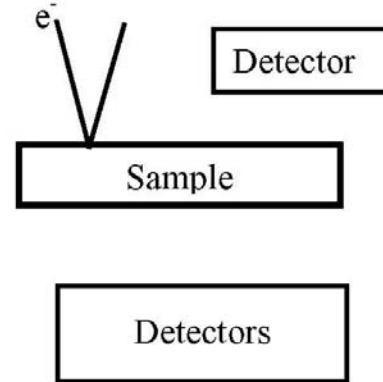
## Outline

- SEM/EPMA vs. TEM/STEM (AEM)
- CTEM modes of operation
- HTREM vs. Z-contrast imaging
- SAED vs. CBED
- Grain boundaries
- Nanocrystals
- Amorphous materials



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| SEM                                                                                                                | TEM                                                                                 | STEM (AEM)                                                                           |
|--------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------|
| Bulk sample                                                                                                        | Thin sample                                                                         | Thin sample                                                                          |
| 0.2-50 kV                                                                                                          | 80-1250 kV (typical 100-400 kV)                                                     | 100-300 kV                                                                           |
| Image formation is electronic (and NOT optical)                                                                    | Image formation is based on optical principle (lenses after the sample)             | Characteristic imaging is electronic                                                 |
| Typical signals: SE, BE, AE, EBIC/EBIV, roentgen, EBSD                                                             | Typical signal: TE                                                                  | Typical signal: TE, X-rays                                                           |
| Characteristic information: surface topography, average atomic number, potential, crystal orientation, composition | Characteristic information: grain structure, crystallography, defect structure      | Characteristic information: average atomic number, composition, crystallography      |
|                                  |  |  |

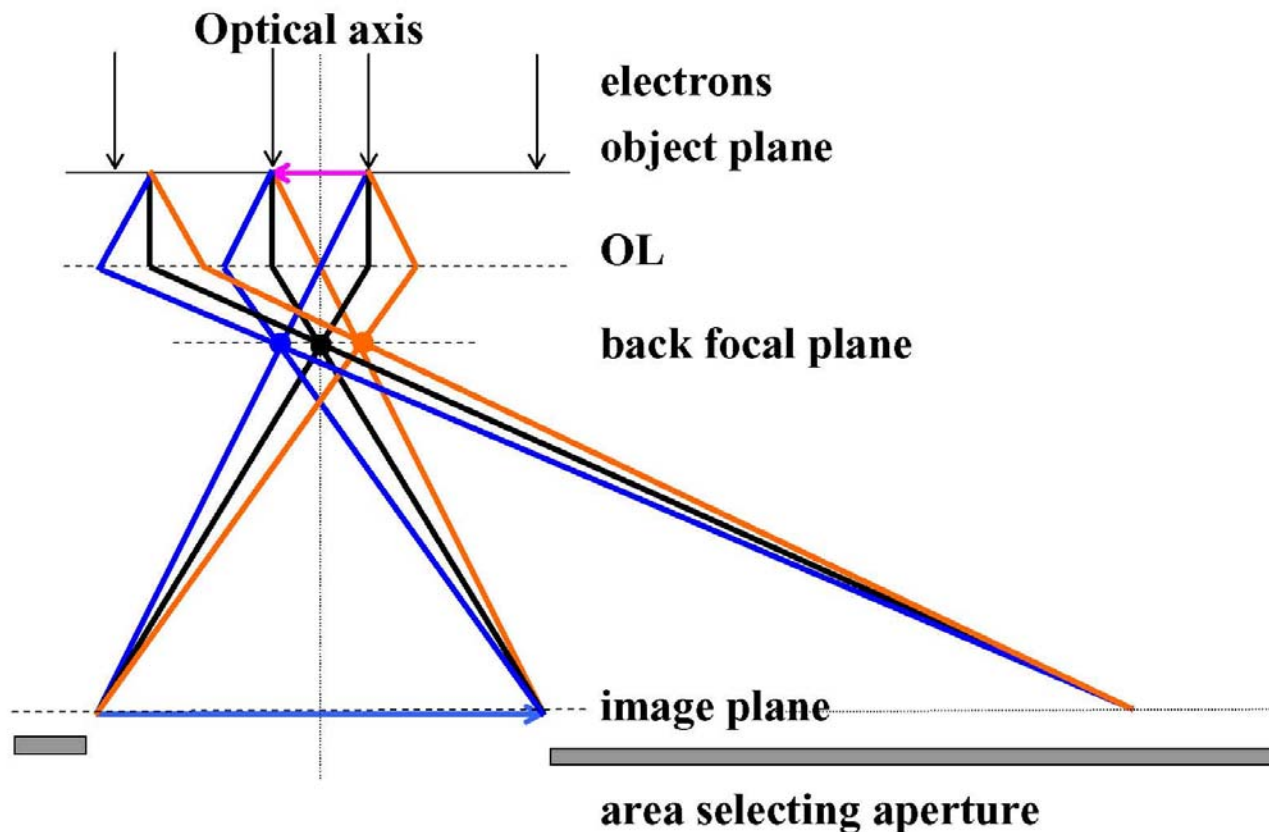


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# Conventional TEM: Image formation of a concave lens

## Image formation in a concave lens



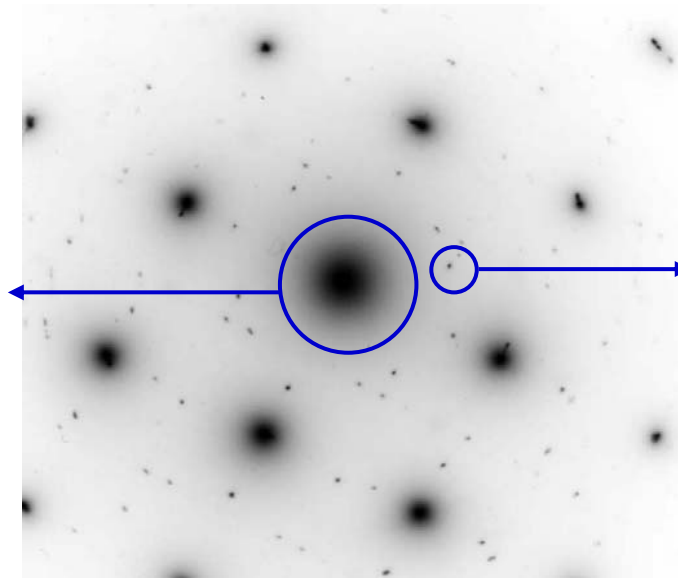
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# Conventional TEM: basic modes of operation: BF/DF, SAED



Bright-field image



Selected area electron diffraction



Dark-field image

BF / DF images are formed by  
amplitude-contrast (diffraction-contrast)



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# Phase contrast

An ideal phase object imaged with perfect lenses would produce no contrast

$$\psi(x) = \psi_0 \cdot \exp(i\varphi(x))$$

$$I = |\psi|^2 = |\psi_0|^2 = \text{const}$$

Obviously, it is the same for weak phase objects: no contrast to first order

$$\psi(x) = 1 + i\varphi(x)$$

Zernike phase-contrast for weak phase objects: shift the relative phase between diffracted beams and the central beam by 90°

$$\psi(x) = 1 + i \cdot i \cdot \varphi(x) = 1 - \varphi(x)$$

Then the intensity to first order is proportional to the phase shift with no loss of resolution.

$$I(x) = |\psi(x)|^2 = 1 - 2\varphi(x)$$

In OM the 90° phase shift is done by the Zernike phase plate. In HRTEM, we approximate this phase shift by the phase shift, caused by the imperfect microscope.

$$\psi_i(x, y) = 1 - i \cdot \sigma \cdot \Phi_p(-x, -y) \otimes F\{A(u, v) \cdot \exp(i \cdot \chi[u, v])\}$$



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# Phase shift, contrast, resolution

OM:  $\chi=\pi/2$

Zernike phase plate

TEM: no phase plate  $\Rightarrow$

we use the phase shift caused by the spherical aberration and the de-focus

$$\chi(u, v) = i \cdot 2\pi \cdot \left( \Delta f \cdot \lambda \cdot \frac{u^2 + v^2}{2} + c_s \cdot \lambda^3 \cdot \left\{ \frac{u^2 + v^2}{2} \right\}^2 \right)$$

$C_s > 0 \Rightarrow$  **Solution:**

Scherzer de-focus ( $\chi = -\pi/2$ ):

„Black atom” contrast

Resolution:

**Requirements:**

- $\chi = \pm\pi/2$  in broad band
  - No oscillation at small  $u$
- $\Rightarrow$  Minimum of parabola

$$- \Delta f = \left( \frac{3}{2} \cdot C_s \cdot \lambda \right)^{1/2}$$

$$d_p = 0.66 \cdot C_s^{1/4} \cdot \lambda^{3/4}$$

**Consequences:**

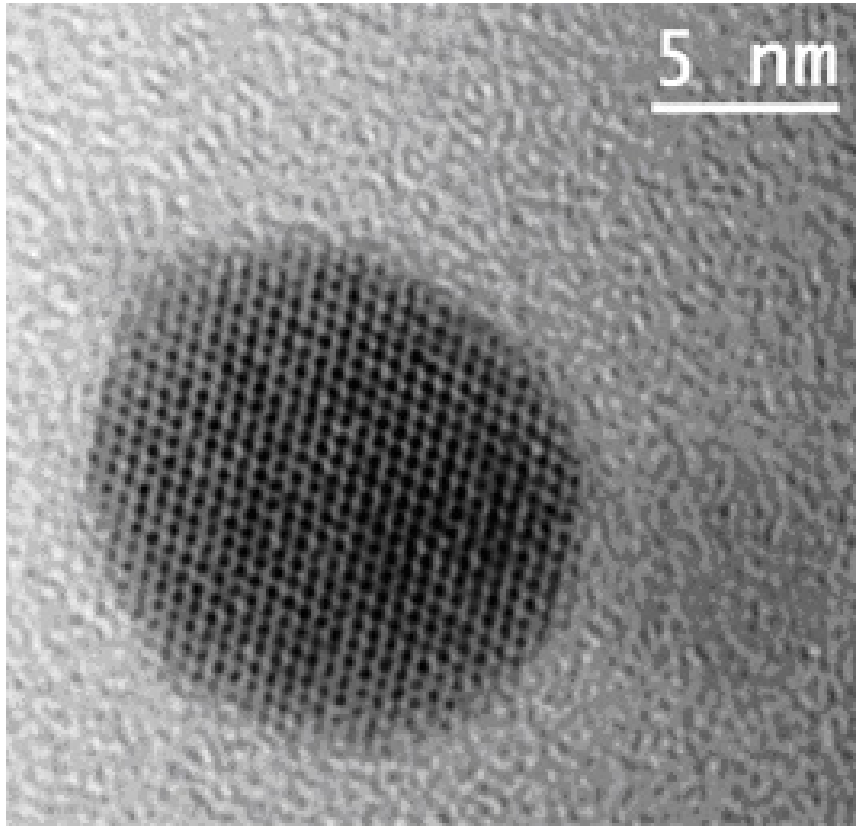
- Can be fulfilled for any  $C_s \neq 0$
- Size of contrast is not affected if it is fulfilled at small  $C_s$
- Better resolution for lower  $C_s$
- $\Rightarrow C_s$ -corrected microscope
- For  $C_s < 0$  it can be fulfilled with  $\Delta f > 0 \Rightarrow \chi = \pi/2 \Rightarrow$  „Bright atom” contrast  $\Rightarrow$  Visibility of light atoms



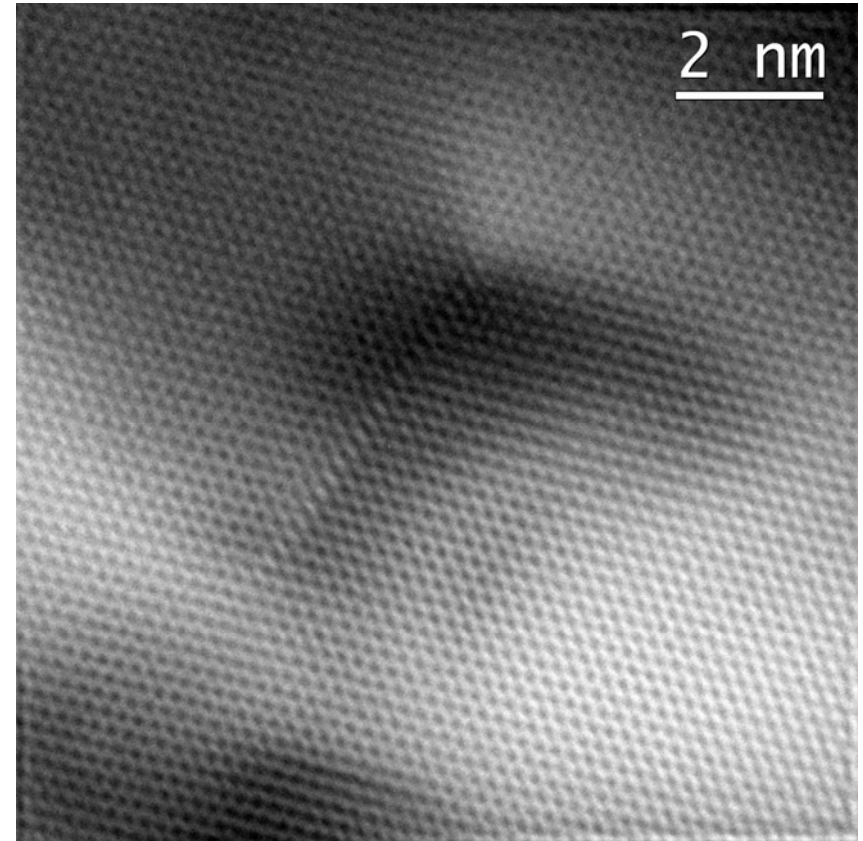
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# High resolution TEM (HRTEM): phase contrast Example



Magnetite nano-crystal on  
amorphous Carbon supporting film



Stacking fault in Ag

$C_s > 0$



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# Interpretation of phase contrast HRTEM images

Interpretation is based on **assumptions**

- The sample is so thin that it is an ideal weak phase object
- The image was recorded at **Scherzer** focus. In that case the atomic columns are **dark**.
- B/W contrast periodically reverses with both thickness and de-focus.

Interpretation is **not intuitive** in general case. A structure is generally assumed a priori and the images in a focal and thickness bi-series are calculated and **compared** to the experimental ones to prove that the assumed structure is in accordance with the measured one. If yes, it is declared to be the measured structure.

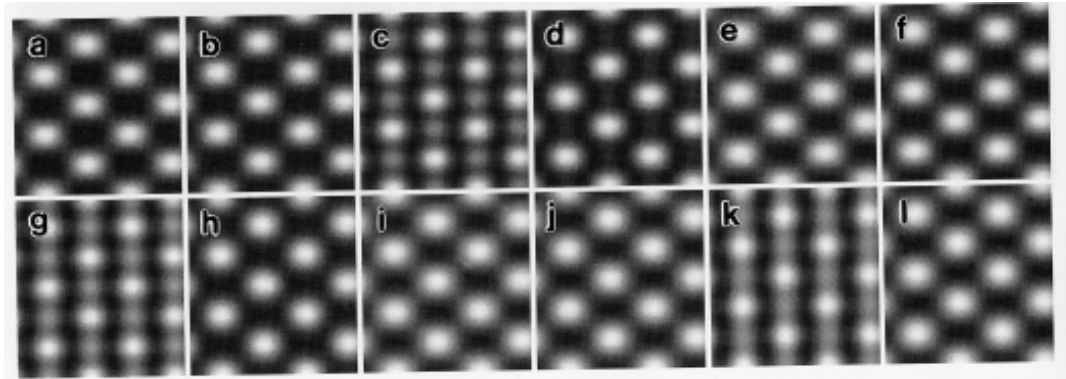


Fig. 2.6. Defocus dependency of lattice images of a Si crystal with incidence  $[0\bar{1}1]$ . Use of a 200 kV EM and a thickness of 6 nm are assumed. The defocus changes from  $-20$  nm (overfocus) to  $90$  nm (underfocus) in steps of  $10$  nm

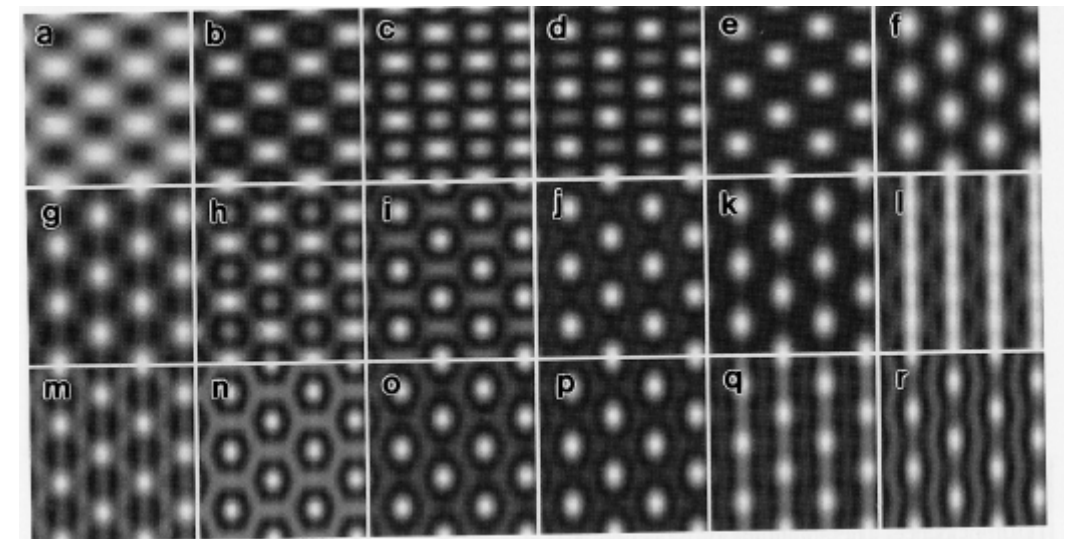


Fig. 2.5. Thickness dependency of lattice images of a Si crystal with incidence  $[0\bar{1}1]$ . Use of a 200 kV EM and a defocus value of  $65$  nm are assumed. The thickness changes from  $a$   $1$  nm to  $r$   $86$  nm in steps of  $5$  nm



# (D)STEM and Z-contrast imaging

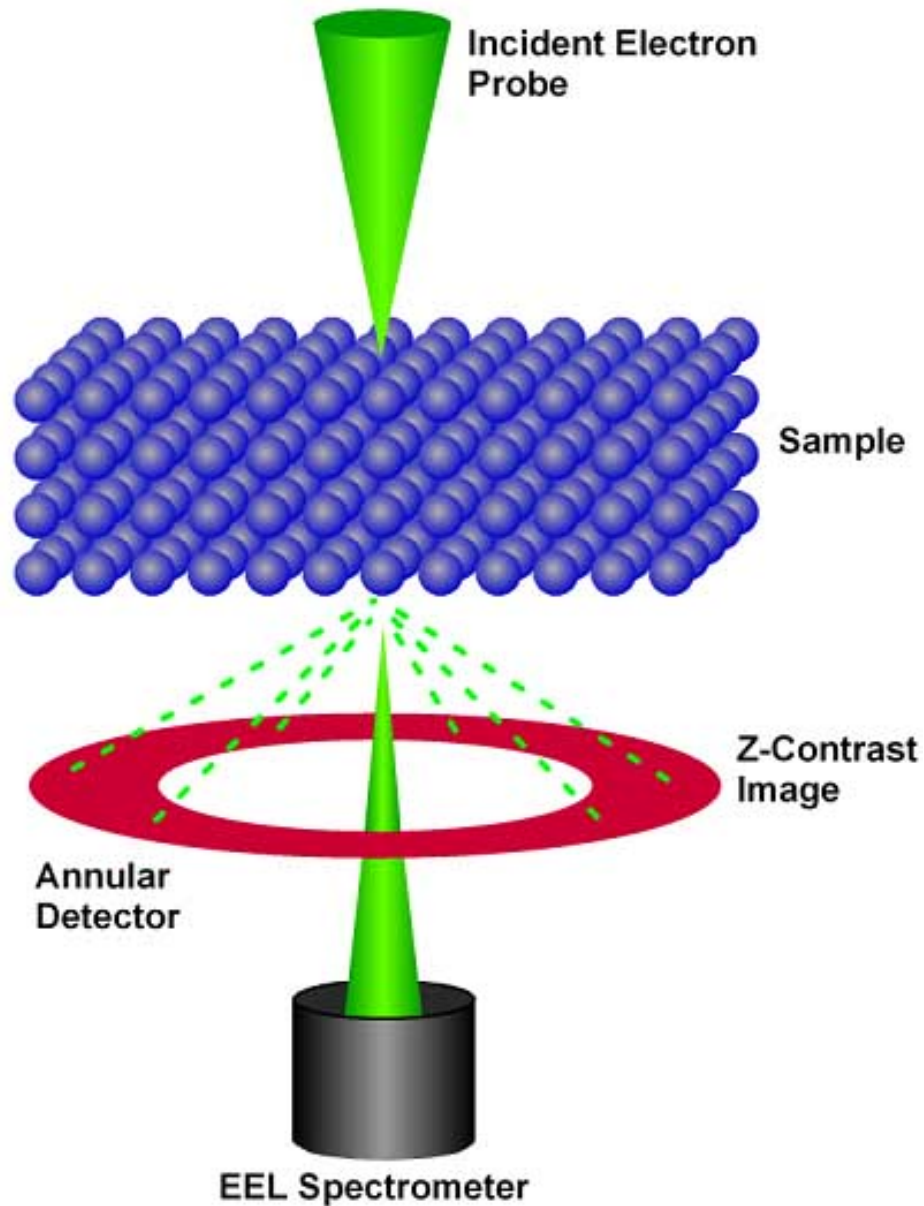


Image is dominated by thermal diffuse scattering (TDS)  $\Rightarrow$  monotonic function of atomic number ( $Z$ ).

No contrast reversal with sample thickness.

No contrast reversal with defocus.

$\Rightarrow$  Intuitive interpretation.



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# STEM Z-contrast imaging: example

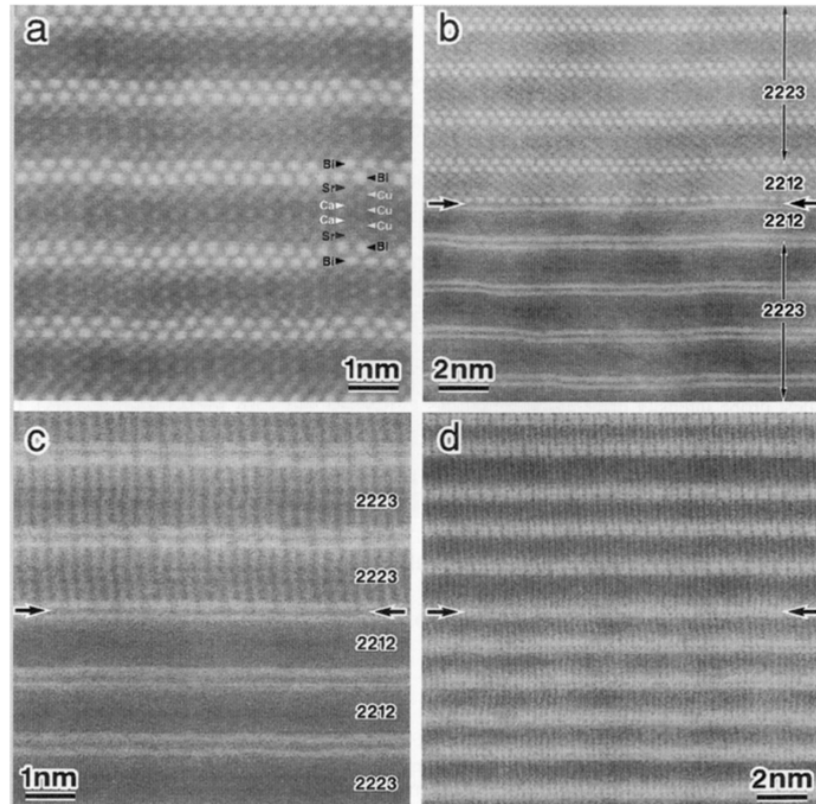


Fig.3. Z-contrast images of the BSCCO semiconductor: (a) the Bi-2223 phase in the [110] projection, (b, c) (001) twist boundaries at arbitrary misorientations and (d) a (001) twist boundary with a 90° twist angle. Positions of the grain boundaries are indicated by arrows.

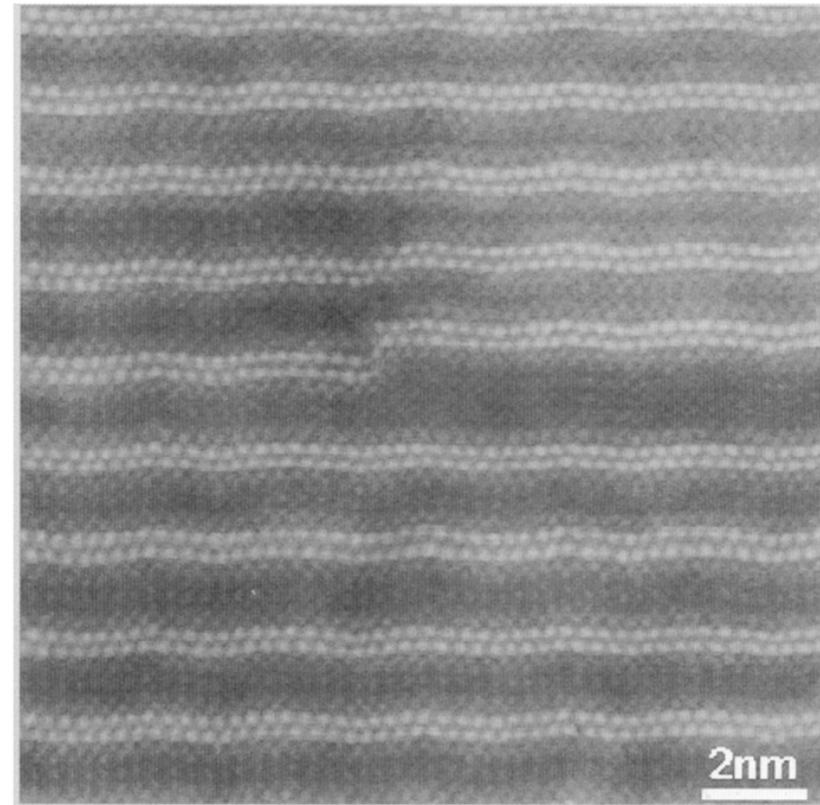


Fig.4. Z-contrast image of the BSCCO semiconductor in [110] projection. Departures from the Bi-2223 phase can be seen in the vicinity of the defect.

Incoherent  $\Rightarrow$  Unambiguous contrast  $\Rightarrow$  *Intuitive interpretation*  $\Rightarrow$  Determination of unexpected structures

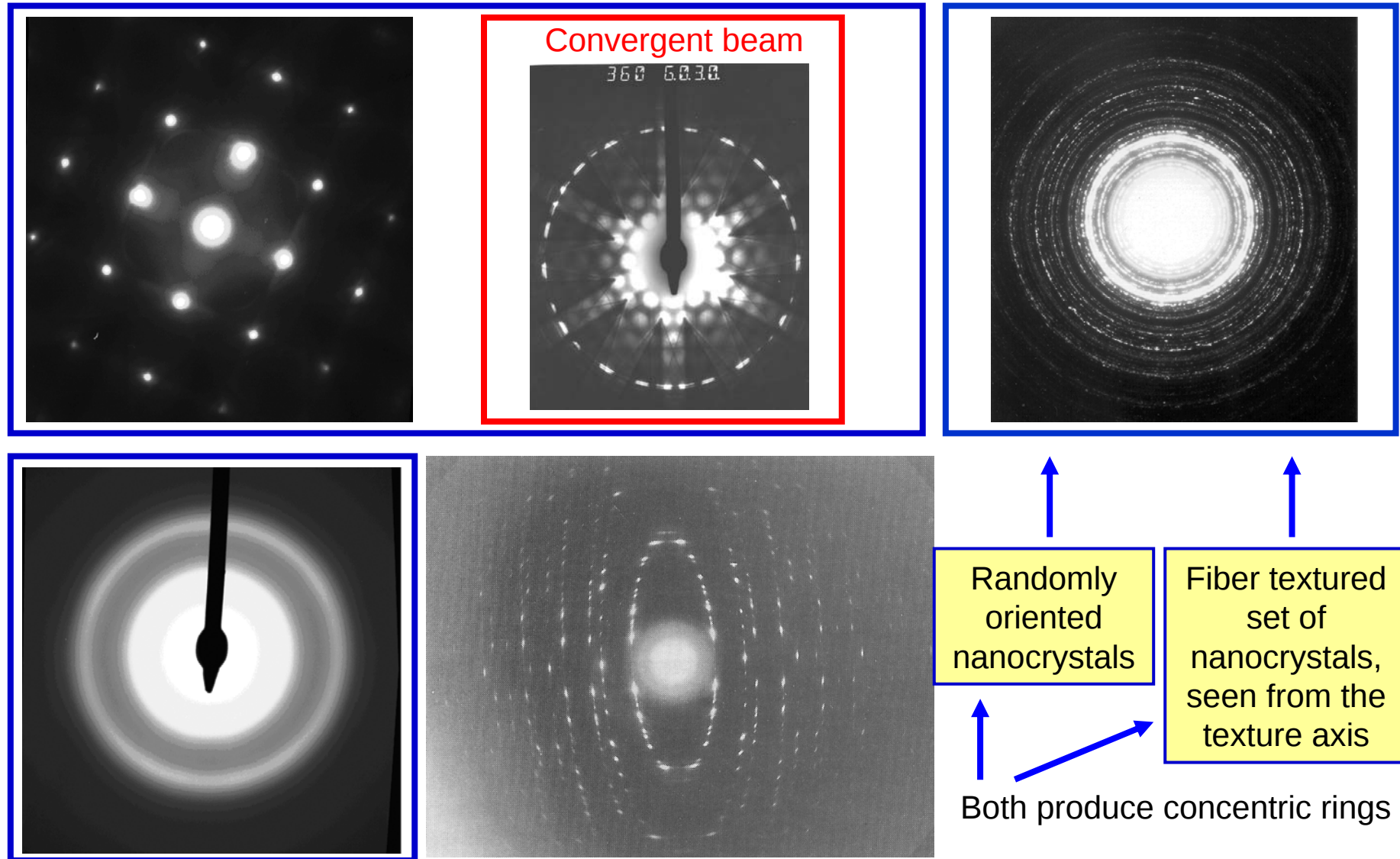
**Determining factor:** beam diameter must be comparable to the atomic distances



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# Basic types of ED patterns in the TEM



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# Indexing single crystals from a tilt series

24 Symmetry equivalent solutions

1. Angle  $[-1 -5 8]$  &  $[0 -1 1] = 14,3^\circ$

...

| Goniometer Holder                                                      |                  |      |    |
|------------------------------------------------------------------------|------------------|------|----|
| Calculate<br>angle<br>difference<br>between<br>goniometer<br>positions | Position1        | 9    | -2 |
|                                                                        | Position2        | 22   | 3  |
|                                                                        | Angle difference | 13,9 |    |

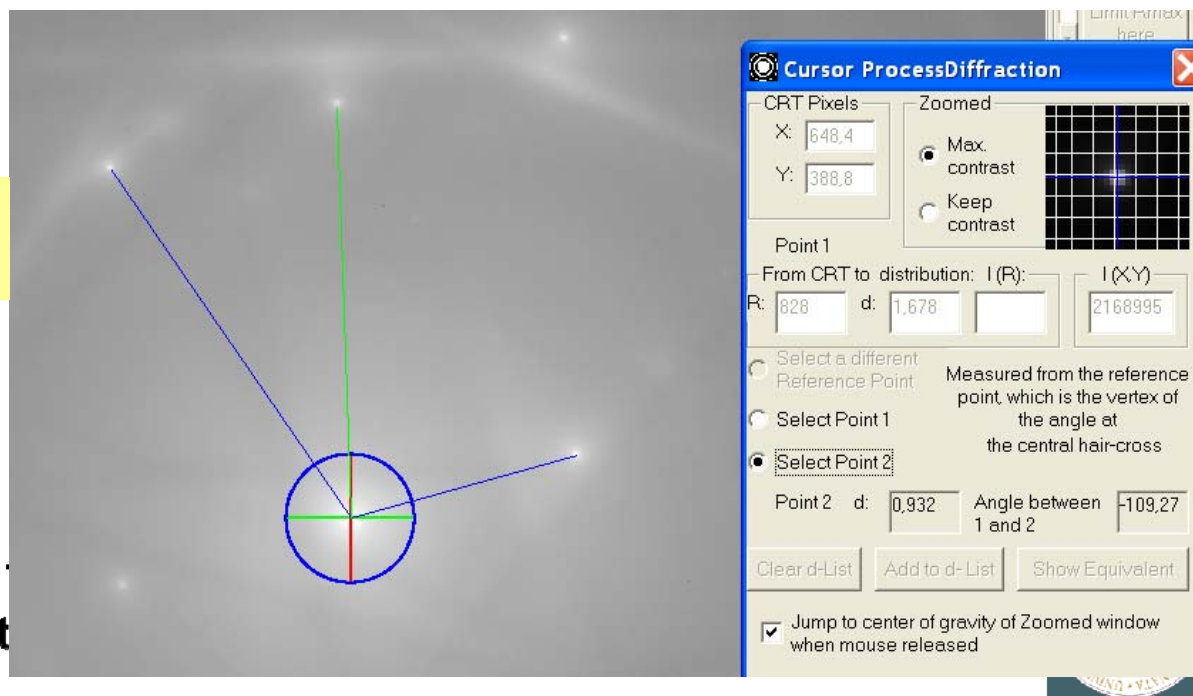
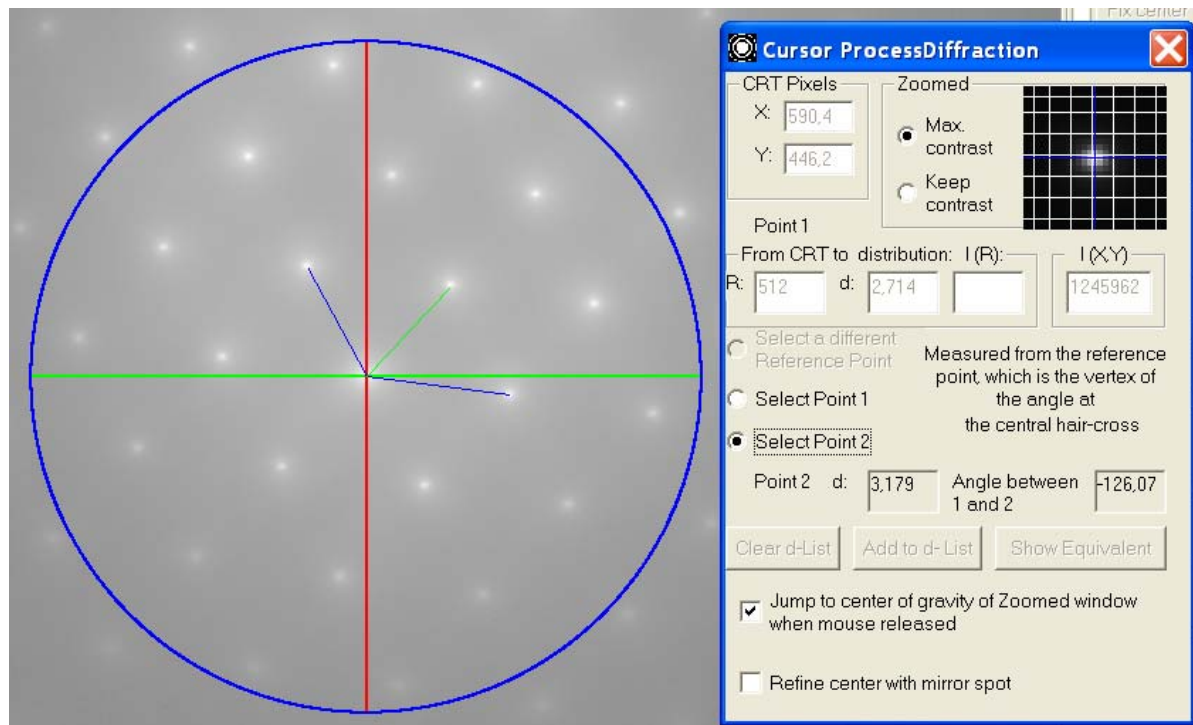
Exp. angle between GoniPos :  $13.9^\circ$

Three zones along an angular triangle can be processed together.

**Phase identification  
orientation determination**

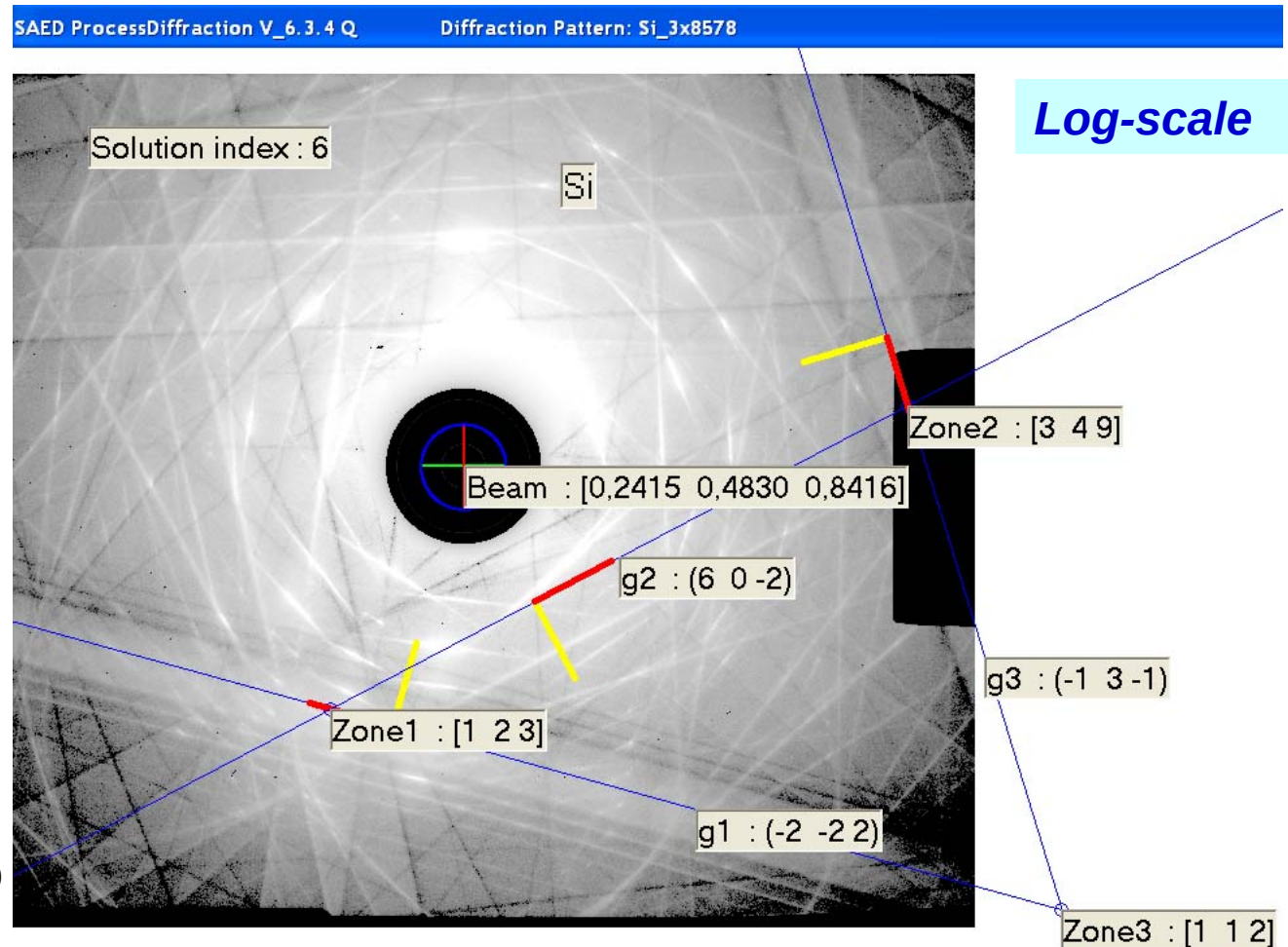


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# Orientation of single crystals from CBED

- Non-linear BKG correction for visibility
- Indexed triangle
  - d-value
  - plane-angle
  - zone-angle
  - handedness
- Indexed zone can be slightly outside of the measured range
- Beam position (PC)
- Transformation to Photo coordinate system



One, out of the 24 symmetry equivalent solutions is shown

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# Orientation / Misorientation → $\underline{\underline{M}} = \underline{\underline{O}}_2 * \underline{\underline{O}}_1^{-1}$

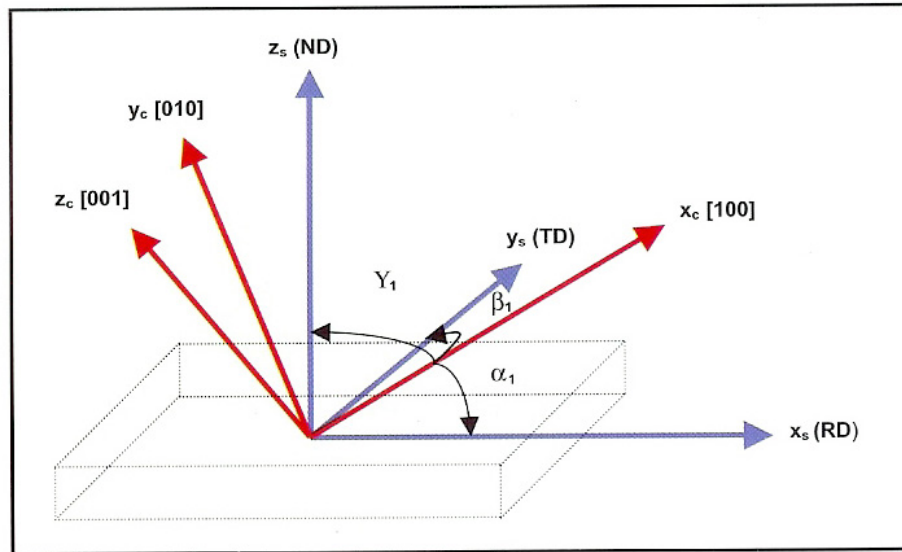


Figure 36: Relationship between crystal and sample coordinate systems.  $\alpha_1$ ,  $\beta_1$  and  $\gamma_1$  are the angles between the crystal direction [100] and RD, TD and ND respectively.

$$\underline{\underline{O}} = \begin{pmatrix} \cos \alpha_1 & \cos \beta_1 & \cos \gamma_1 \\ \cos \alpha_2 & \cos \beta_2 & \cos \gamma_2 \\ \cos \alpha_3 & \cos \beta_3 & \cos \gamma_3 \end{pmatrix}$$

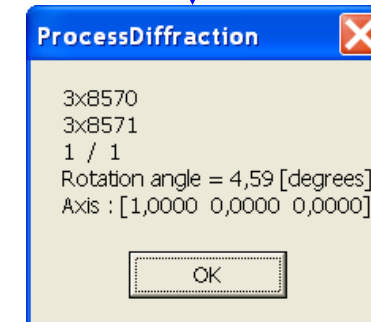
The orientation can also be related to the photo coordinate system.

Calculate symmetry related equivalent solutions from stored Orientation matrices.

Disorientation is picked.

Error reduction by using *redundant* data in misorientation matrix:

- **Diagonal** elements
- **Off-diagonal** elements



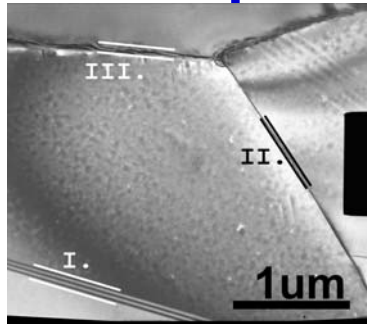
Geometrical characterization of **grain boundaries**



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# Measurement of the orientation of the GB plane: **Advantage over EBSD**

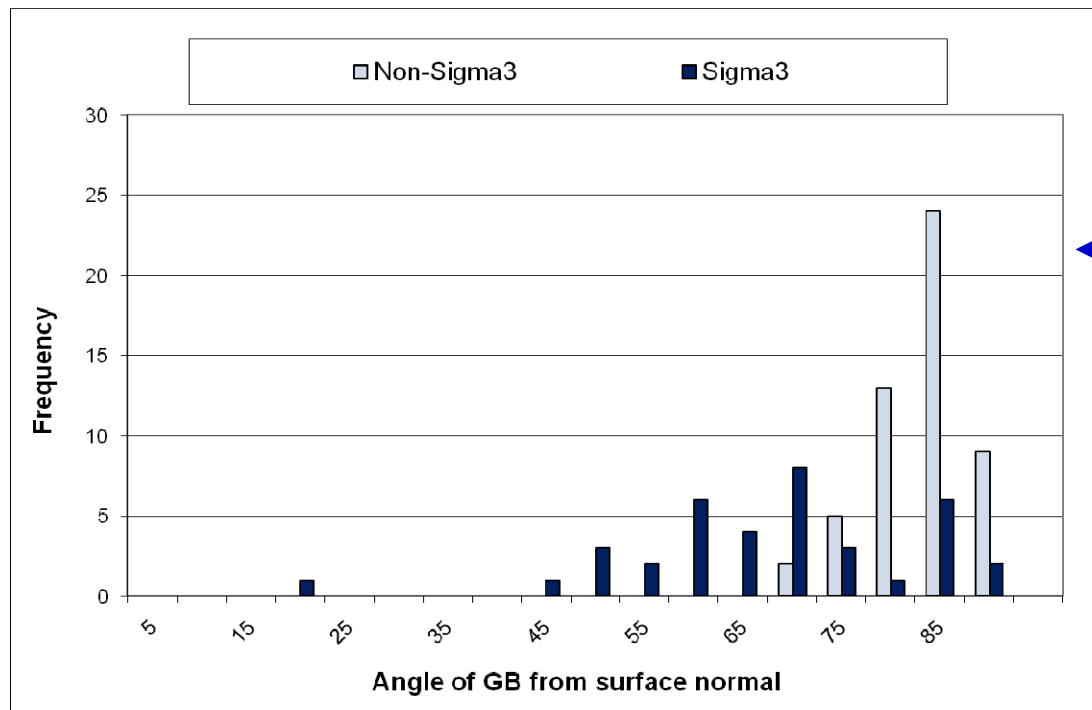


Example of projections of different GB planes.

Width of projection is measured.

Projections are measured at two distinct goniometer settings.

Local thickness is determined from two-beam CBED.



**Example:** GB characterization by **combining** diffraction and imaging (=misorientation and plane orientation)

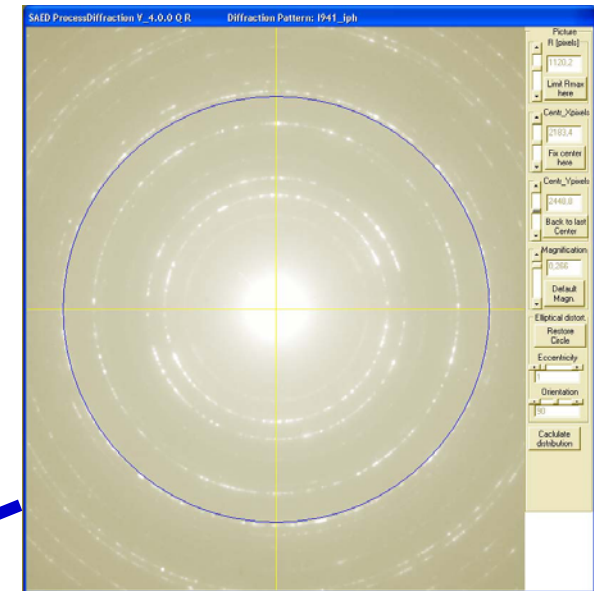
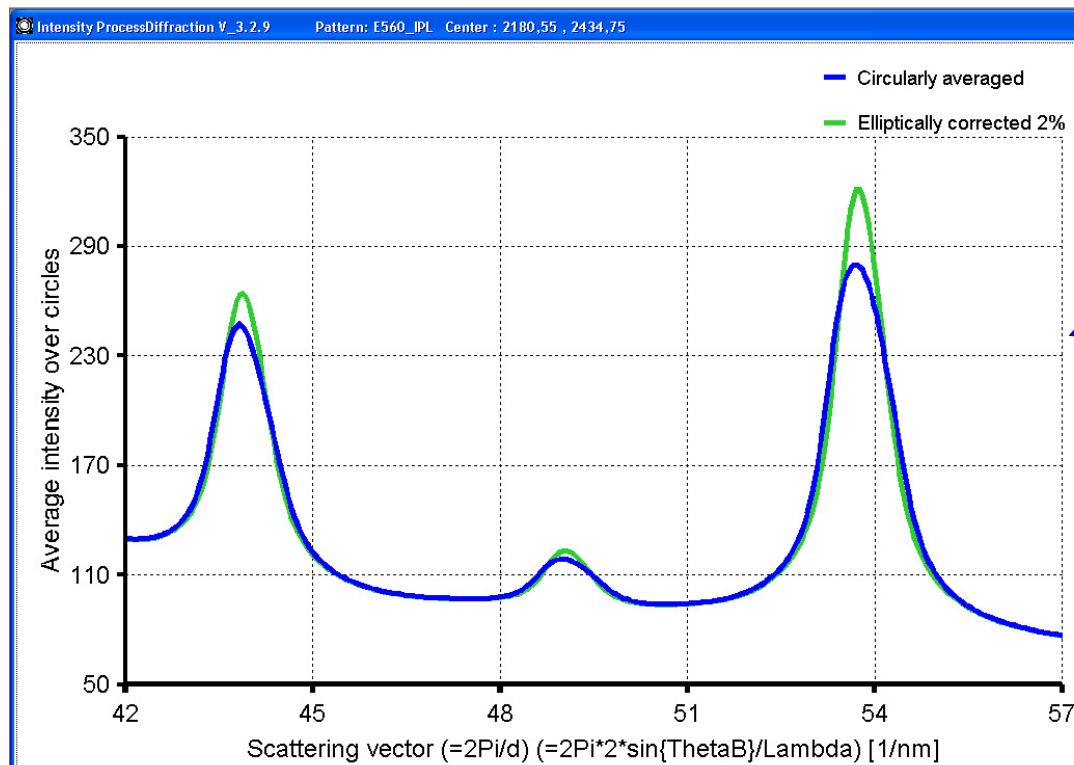


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# Identification of phases in *nanocrystalline* thin films (SAED ...)

- Conversion of 2D patterns into 1D distributions
- Correction for elliptical distortion
- Extension of dynamic range



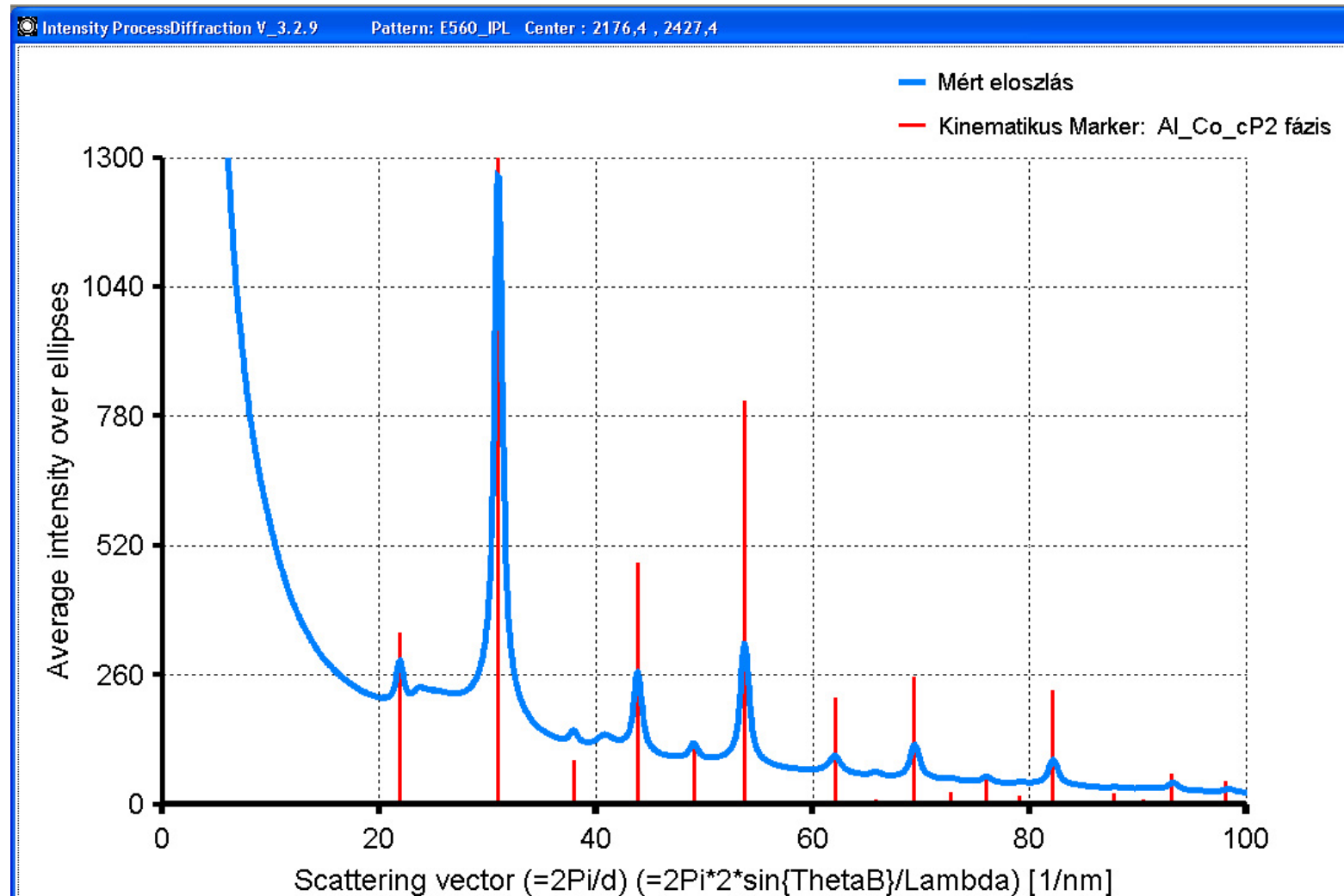
- Units of x-axis (pixel, Q,  $2\theta$ ),
- peak search
- Average above average (Beam-stop, etc.)
- Background, net, ...



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# Qualitative phase analysis (identification of phases): Visual comparison to *Markers*



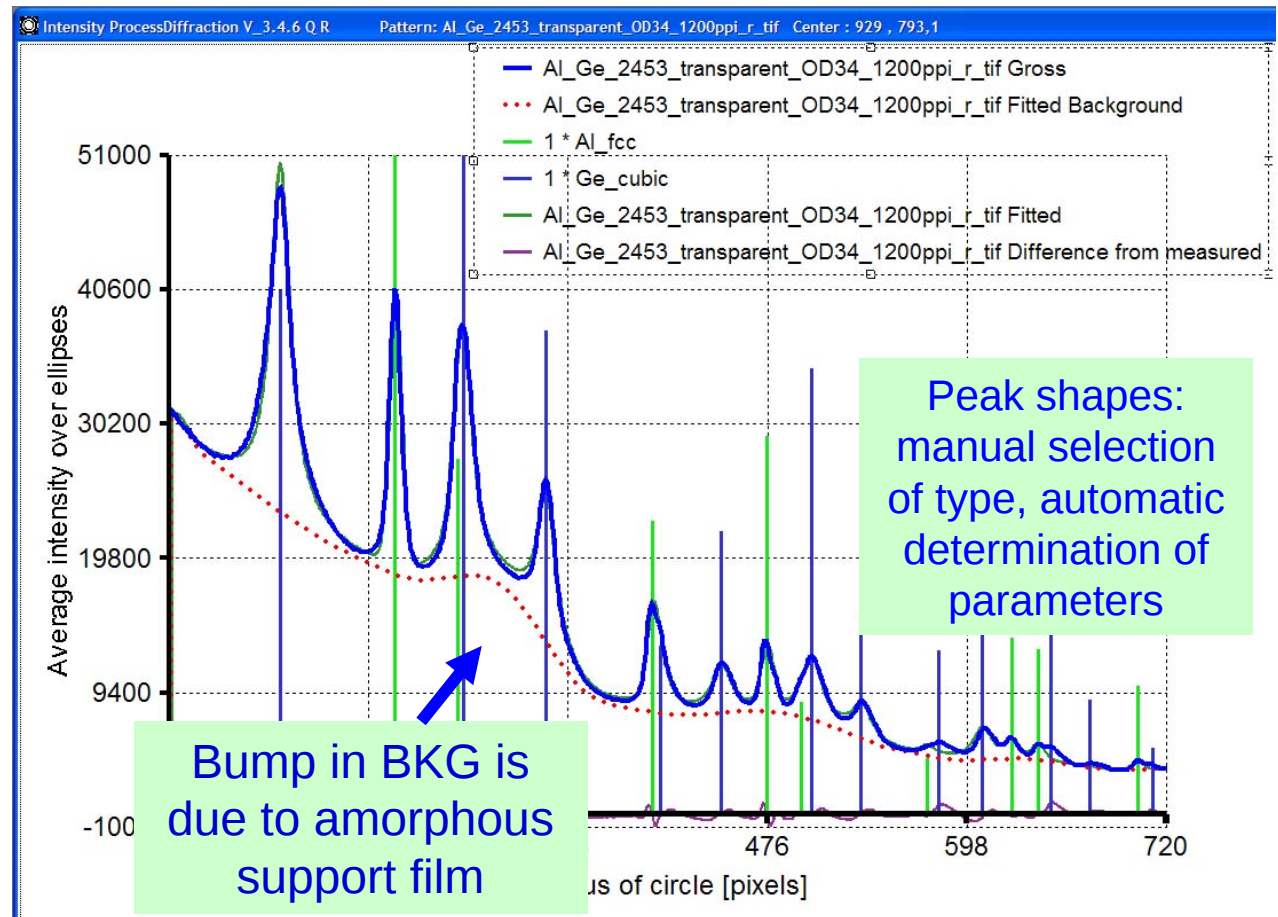
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# Modeling / fitting the measured intensity distribution

- Background
  - Normal, log-Normal
  - Polynomial, Spline
- Peak shapes
  - Gaussian, Lorentzian
  - Pseudo-Voigt
- Global minimum
  - Downhill SIMPLEX
  - Manual control

⇒ **parameters** (camera length, peak-width, Gaussian-fraction, ...)
- **Example:** Al + Ge: SAED on C-film
  - Large crystal Al: Gaussian
  - Small crystal Ge: Lorentzian



***Different peak-shapes are observed for the two phases of the same sample***

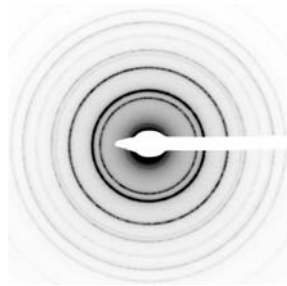
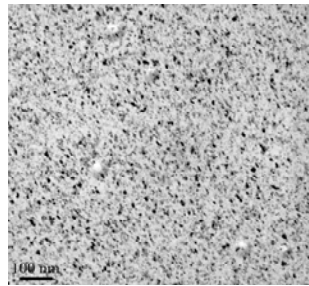


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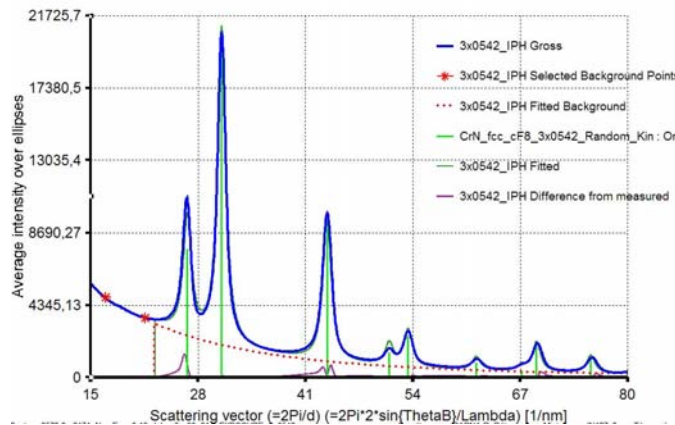


# Example: Measuring change in lattice parameter

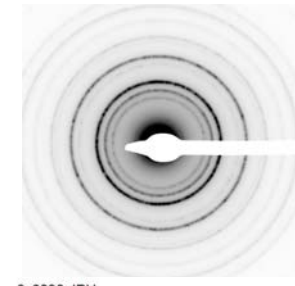
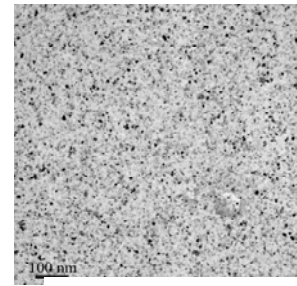
Camera length can be reproduced with 0.3% precision with our **experimental protocol**. Absolute changes in lattice parameter can only be determined if they significantly exceed this level. Smaller relative change can be determined in comparison to an other (unchanged) phase of the same sample.



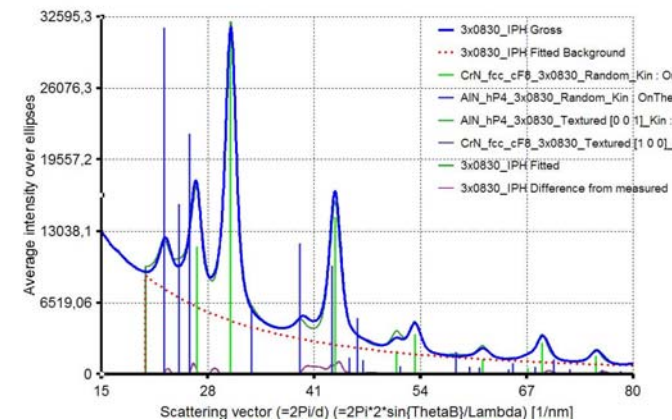
3x0542\_IPH



fcc-CrN with 70% AlN dissolved  
( $a=4.14 \Rightarrow 4.07\text{\AA}$ ).



3x0830\_IPH



hP4-AlN with dissolved 25% fcc-CrN  
( $a=3.11 \Rightarrow 3.20\text{\AA}$ ;  $c=4.98 \Rightarrow 5.13\text{\AA}$ ).



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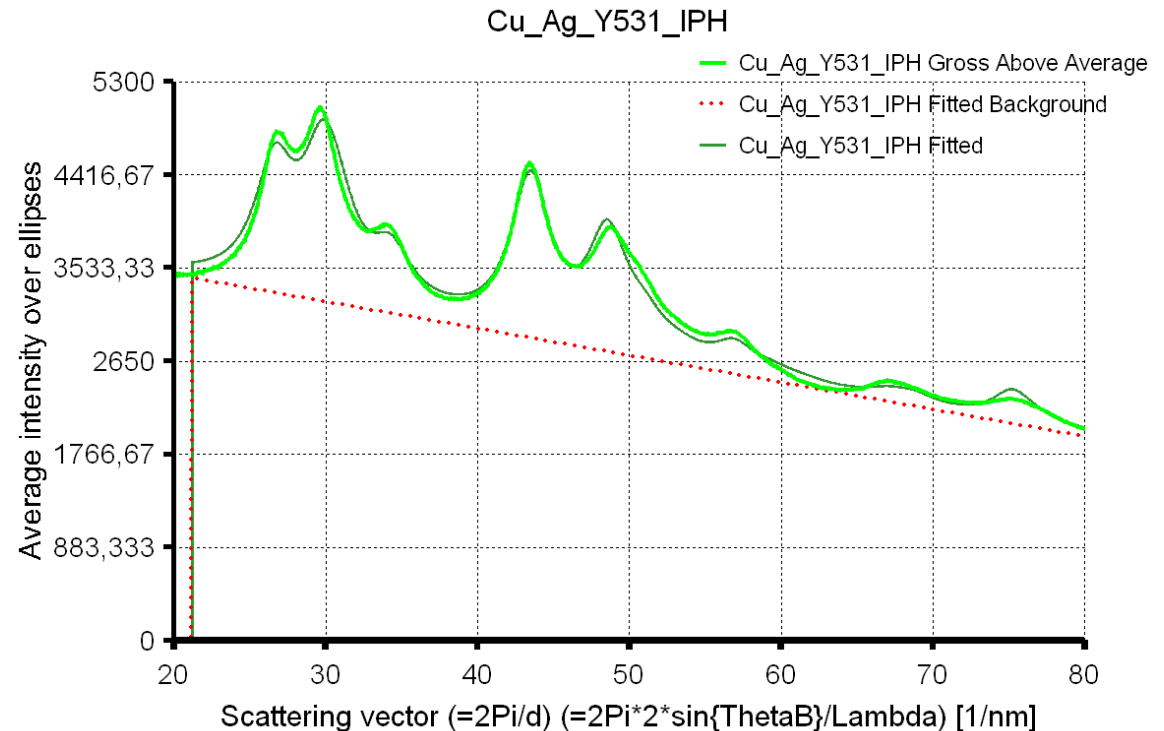
# Example: phase and texture analysis for very small grains $\Rightarrow$ Kinematic

Simultaneously evaporated Cu and Ag.

EDS:        34 Vol % Ag  
              66 Vol % Cu

Measured relative amount of the phases:

Ag\_fcc\_Random :            3.9 Vol %  
Ag\_fcc\_**Textured** [1 1 1]: 28.7 Vol %  
**Total Ag:**                **32.6 Vol %**  
Cu\_fcc\_Random :            10.6 Vol %  
Cu\_fcc\_**Textured** [1 1 1]: 56.7 Vol %  
**Total Cu:**                **67.3 Vol %**



**Agreement with EDS is good in spite of the presence of high background and broad peaks.**



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# Determination of the Short Range Order in **amorphous** samples

|          |               |                |               |                     |               |                                  |
|----------|---------------|----------------|---------------|---------------------|---------------|----------------------------------|
| $I(Q)$   | $\Rightarrow$ | $Q \cdot I(Q)$ | $\Rightarrow$ | $G(r)$              | $\Rightarrow$ | $g(r)$ [RDF(r), $\rho(r)$ , ...] |
| Measured |               | Normalized     |               | Fourier-transformed |               |                                  |

## Assumptions:

- Homogeneous, isotropic material
- Elastic scattering only
- Single (kinematic) scattering
- Composition of the sample is known
- Illumination is parallel

## Empirical corrections are needed because of:

- Inelastic scattering
- Multiple scattering
- Black level from stray radiation, noise, etc.



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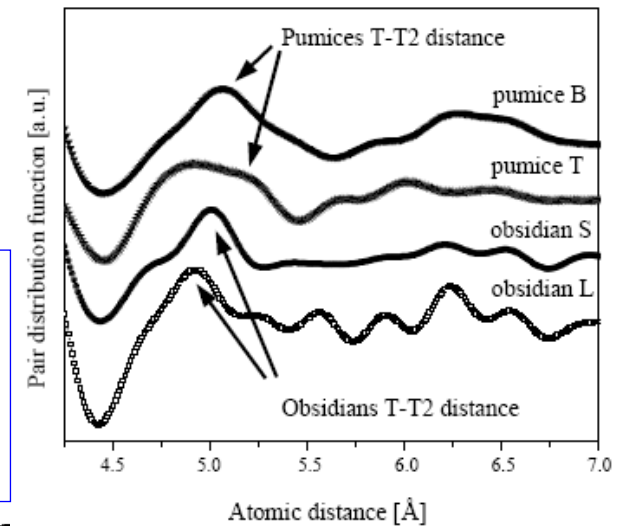
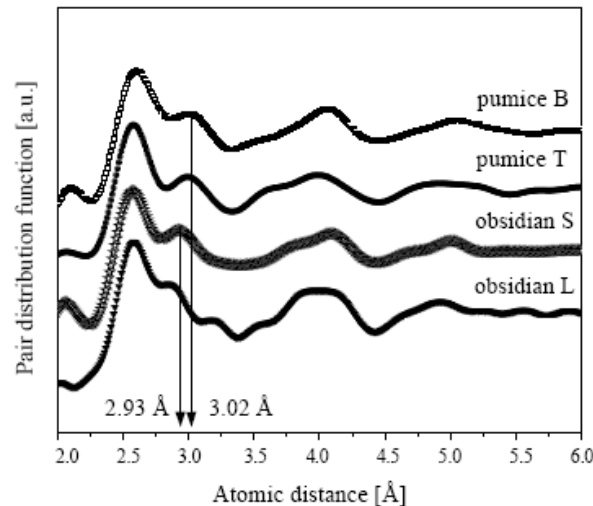


# Determination of the SRO of amorphous samples: examples

## Amorphous $\text{SiO}_2$ minerals

- obsidian
- pumice

- Building block:  $\text{SiO}_4$  tetrahedron
- The ordering of the  $\text{SiO}_4$  tetrahedra is different in the two amorphous minerals
- Structure in both amorphous materials already resembles the SRO in the respective crystalline forms



V Kovács Kis, I  
Dódon, JL Lábár,  
Eur. J. Miner. 18.  
745-752. (2006)

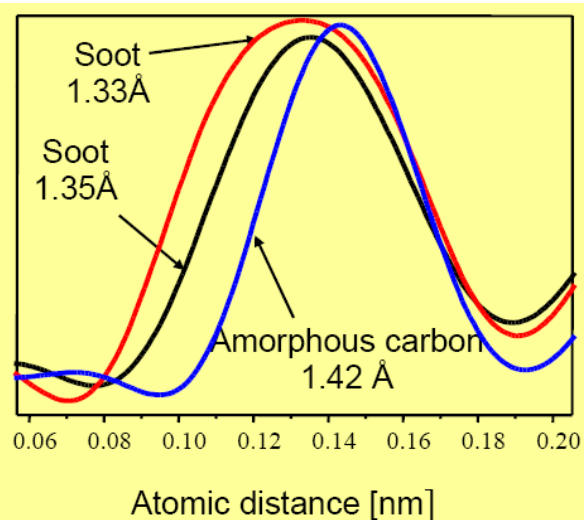


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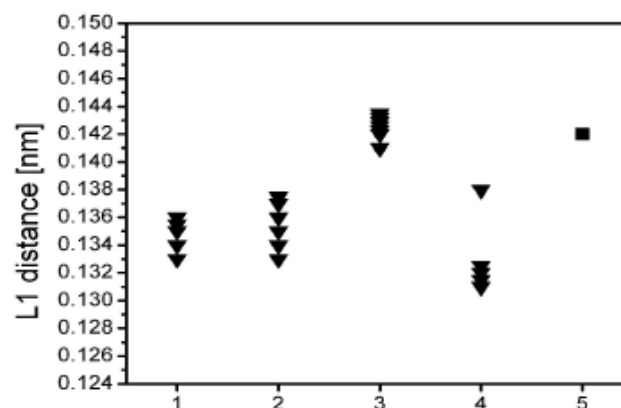


# Determination of the SRO of amorphous samples: examples

## Structure of soot from aerosols



## First nearest neighbour atomic distances in carbonaceous materials



- 1 – soot 1 from Central Europe
- 2 – soot 2 from South Africa
- 3 – magnetron sputtered amorphous carbon (H/C = 0)
- 4 – kerogen with 95 at% total carbon (H/C = 0.61)
- 5 – graphite (not measured)

## Conclusions:

1. Atomic distances are similar in soot both from Central European Troposphere and a savanna fire in South Africa
2. First peaks in PDF results from the superposition of C-C and C-H distances
3. H/C ratio is lower in soot than in kerogen (0.61)

V Kovács Kis, M Pósfai,  
JL Lábár  
Atmospheric Environment  
40 (2006) 5533–5542



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# Thank you for your attention

## Further reading:

- JL Lábár, *Ultramicroscopy*, **103** (2005) 237-249
- JL Lábár, *Microsc. Microanal.* **14** (2008) 287-295
- JL Lábár, *Microsc. Microanal.* **15** (2009) 20-29
- JL Lábár et al., *Microsc. Microanal.* **18** (2012) 406-420

The ProcessDiffraction program can be downloaded free from

<http://www.mfa.kfki.hu/~labar/ProcDif.htm>



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