

Article

Signatures of Gate-Driven Out-of-Equilibrium Superconductivity in Ta/InAs Nanowires

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controlled supercurrent (GCS) in superconducting nanobridges is crucial for engineering superconducting switches suitable for a variety of electronic applications. The origin of GCS is controversial, and various mechanisms have been proposed to explain it. In this work, we have investigated the GCS in a Ta layer deposited on the surface of InAs nanowires. Comparison between switching current distributions at opposite gate polarities and between the gate dependence of two opposite side gates with different nanowire−gate spacings shows that

the GCS is determined by the power dissipated by the gate leakage. We also found a substantial difference between the influence of the gate and elevated bath temperature on the magnetic field dependence of the supercurrent. Detailed analysis of the switching dynamics at high gate voltages shows that the device is driven into the multiple phase slips regime by highenergy fluctuations arising from the leakage current.

KEYWORDS: *field effect, nanowire, gate-controlled supercurrent, hot electron injection, phonons, phase slips*

Since superconducting circuits have the potential to realize electronics with short switching time and ultralow power consumption, various architectures have been developed for integrating semiconductor technology with sup electronics with short switching time and ultralow power consumption, various architectures have been developed devices to reduce the high power consumption required for cooling the high-density semiconductor-based microchips.^{1-[3](#page-6-0)} The cryotron, 4 Josephson cryotron, 5 rapid single flux quantum $(RSFQ)$ device,^{[6](#page-6-0)} and nanocryotron $(nTron)^{1}$ $(nTron)^{1}$ $(nTron)^{1}$ were all developed as building blocks for superconducting switches; however, their scalability or even the difficulty of interfacing with CMOS electronics limited their applications. In recent years, suppression of supercurrent by applying a voltage to a gate electrode in the vicinity of a superconducting metallic nanowire has attracted much attention as a promising building block for
highly scalable superconducting switches.^{7−[16](#page-7-0),16−[28](#page-7-0)} In some works, the effect is attributed to the large electric field (10^8 V/m) at the superconducting surface,^{[7](#page-6-0)-[16,16](#page-7-0)-[21](#page-7-0)} which distorts the superconducting state and leads to the quenching of the superconductivity.^{29−[33](#page-7-0)} Other studies^{22−[28](#page-7-0)} reported a correlation between the gate-controlled supercurrent (GCS) and the leakage current flowing between the gate and the superconducting device. Some of these studies suggest that the GCS results from ballistic injection of high-energy quasiparticles.^{24−[26](#page-7-0)} In another work, the quenching of the supercurrent was attributed to the absorption of phonons emitted in the relaxation process of high-energy electrons injected from the gate electrode.^{[28](#page-7-0)} In order to engineer efficient superconducting

switches for future electronic applications, it is important to understand the dominant mechanism behind the GCS effect.

In this work, we have studied the GCS in a superconducting Ta shell deposited on the surface of InAs nanowires.^{[34](#page-7-0)} We chose Ta because of its strong spin–orbit interaction,^{[35,36](#page-7-0)} so it is expected that the electric field has a strong influence on the superconducting state. We investigated the influence of the distance between the gate and the nanowire on the suppression of the supercurrent for the fabricated devices. Also, the magnetic field dependence of the supercurrent under the influence of the gate voltage and elevated temperatures was investigated. In addition, the switching current distribution at opposite gate polarities and at different current ramp speeds was studied. Furthermore, we give a detailed analysis for the switching dynamics at high gate voltages. Our findings contradict the proposed theoretical explanations based on electric fields or ballistic injection of high-energy electrons, and they are consistent with the nonequilibrium phonon picture as the origin of the GCS effect.

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Figure 1. Device geometry and gate dependence characterization (device A). (a) A false-colored SEM image and (b) schematic of the side view of the nanowire device. (c) *I*−*V* characteristics of the device measured at 35 mK. Asthe bias currentrampsfrom negative to positive values (blue arrow), the device switches to a finite-resistance state at the switching current $I_{SW} = 1.17 \mu A$. If the current ramps in the opposite direction (gray arrow), the device switches back to the superconducting state at two successive retrapping current values at $\simeq 0.61 \mu A$ and $\simeq 0.4 \mu A$. (d) *I_{SW}* as a function of *V*sg (at magnetic field *B* = 0.1 T) applied to SG1 (orange curve) and SG2 (light blue curve) with nanowire−gate spacings of ≃65 and ≃115 nm, respectively. (e) The leakage current as a function of *V*_{sg} for both gates.

Figure 2. Magnetic field dependence and comparison between the GCS effect and effect of bath temperature (device B, *d* = 35 nm). (a) *I*−*V* curve as a function of out-of-plane magnetic field *B* up to ± 2 T. (b) I_SW as a function of V_sg at various values of B-field up to 2 T. (c) I_SW as a function of the B-field at various elevated temperatures and (d) at various values of *V*sg. (e) Magnification of the curves surrounded by the red rectangle in (c) and (d). (f) Comparison between the SCDs measured at *T* = 600 mK (blue) and *V*sg = 3 V (green).

Figure 3. SCD measurements and schematics for different proposed mechanisms of the GCS effect (device C, $d = 30$ nm). (a) SCDs measured at positive (orange) and negative (blue) gate polarity and paired at the same **|***V*sg**|**. The SCDs are normalized to their maximum counts and shifted on the *y*-axis for clarity. The inset shows I_{SW} as a function of V_{sg} for the investigated device measured at 0.1 T. (b) SCDs measured at positive (orange) and negative (blue) gate polarity and paired at approximately the same P_G . The inset shows the mean value of $\langle I_{SW} \rangle$ of SCDs measured at both gate polarities as a function of *P*G. (c) Schematic diagram of the electric field *E* applied from the metallic gate N to the superconducting nanowire SC at positive gate polarity. The colored/uncolored parts represent occupied/unoccupied states. (d) Schematic diagram of the ballistic electron injection from the gate to the nanowire at negative gate polarity. The high-energy electron (red circle) tunnels through the potential barrier of the substrate S and relaxes to the lowest unoccupied state (close to the superconducting gap edge), releasing heat on the SC side. (e) Schematic diagram of relaxation of high-energy electrons in the substrate when injected from the SC/N side to N/SC at positive/ negative gate polarity in the left/right panels. In the case of positive gate polarity, the electrons relax close to the SC side (superconducting nanowire) so that it is heated more than in the case of negative gate polarity at the same P_G .

RESULTS AND DISCUSSION

In our device configuration, we used InAs nanowires with a 20 nm-thick Ta shell layer deposited on only three facets of the nanowire.^{[34](#page-7-0)} In order to investigate the impact of the gate on the supercurrent flowing in the Ta layer, four-terminal nanowirebased devices were fabricated with the configuration shown in [Figure](#page-1-0) 1a,b. The Ta/InAs nanowires (green/brown) were deposited on a doped Si wafer with a 290-nm-thick oxide layer. Four Ti/Al contacts (blue) with a thickness of 10/80 nm were fabricated on the top of the nanowire with a distance of 1 *μ*m for quasi-four-terminal measurements. Two metallic Ti/Au side gates, SG1 (orange) and SG2 (light blue), with a thickness of 7/ 33 nm were placed with unequal spacings and on opposite sides of the nanowire. This provides a possibility to study the GCS effect for the device with gates at different spacings. The results presented in this paper are based on measurements performed on three different devices, A, B, and C, with the same device geometry, but with different values of nanowire−gate spacing *d* in the range from 30 to 120 nm. The results in [Figure](#page-1-0) 1 were measured on device A and in [Figure](#page-1-0) 2 on device B, while the results in Figure 3 and their analysis in [Figure](#page-3-0) 4 were performed on device C.

The current−voltage (*I*−*V*) characteristics measured at 35 mK show a clear switching from the superconducting state to the normal state at the switching current $I_{SW} \simeq 1.17 \mu A$ (see blue curve in [Figure](#page-1-0) 1c). When the measurements are carried out in the opposite sweep direction (gray curve), the device shows a hysteretic behavior and switches back to the superconducting state at two successive retrapping current values at ≃0.61 *μ*A and 0.4 *μ*A. This hysteretic behavior can be attributed to large Joule heating dissipated in the resistive state.^{[37](#page-7-0)} The GCS is

investigated by measuring the dependence of I_{SW} under the influence of gates SG1 (orange) and SG2 (light blue) with *d* of ≃65 and ≃115 nm, respectively. [Figure](#page-1-0) 1d shows *I*_{SW} as a function of V_{sg} for both gates, where each of the plotted curves has the same color as the corresponding gate in [Figure](#page-1-0) 1a. The plot reveals that both gates completely switch the device to the normal state at almost the same critical gate voltage, $V_{sg,C} \simeq \pm 13$ V. Even though the nanowire−gate spacing for SG1 is about half that for SG2, SG2 still suppresses I_{SW} at lower threshold gate voltage V_{th} than SG1. Importantly, at V_{th} a correspondingly large increase in the gate leakage current Ileak is observed for each of the gates (see [Figure](#page-1-0) 1e), which has also been reported elsewhere.^{[22,23](#page-7-0),[25](#page-7-0),[26,28](#page-7-0)}

The dependence of the supercurrent in our device on the outof-plane magnetic field *B* is shown in [Figure](#page-1-0) 2a, where the *I*−*V* curves are measured as a function of the *B*-field up to ± 2 T. The white region represents the zero-resistance state, with a transition to and from the normal state (red and blue regions) at the switching and retrapping current values in the positive and negative bias current values, respectively. The magnitude of I_{SW} shows a rapid suppression with increasing *B*-field below 100 mT and then slowly decreases with further increasing the magnetic field up to 2 T. The sharp decrease in the critical current below 100 mT coincides with the B_C of the Al electrodes contacting the nanowire; 23 therefore we believe that this decrease is a result of the Al contacts switching to normal state. Although the maximum *B*-field in our setup (2 T) does not allow full suppression of the superconducting state in the Ta shell, based on the measured trend, B_C is expected to be about 3.5 T, which is consistent with earlier findings on identical Ta/InAs nano-wires.^{[38](#page-7-0)}

Figure 4. Analysis of the switching dynamics under the influence of *V*_{sg} (device C, $d = 30$ nm). (a) Standard deviation σ and mean value $\langle I_{SW} \rangle$ as a function of $|V_{sg}|$ for all SCDs measured at negative gate polarity in the blue and green curves, respectively. (b) The calculated skewness as a function of $|V_{sg}|$ for SCDs measured with a step of 0.1 V in the interval [−3.5, −2.7 V] (surrounded by the vertical gray dotted lines in panel a) where a corresponding increase in I_{leak} is observed. (c) Logarithm of escape rate Γ as a function of I_{SW} (colored curves) for different values of *V*_{sg} from −3.5 V (orange curve) up to −2.7 V (purple curve) with a step of 0.1 V. The colored solid lines represent the fitting of different portions of these curves with an exponential of higher orders n of the slope α . The inset shows the variation of the slope α with increasing V_{sg} (red curve) and the corresponding I_{leak} as a function of V_{sg} (gray curve).

The gate dependence of I_{SW} under the influence of the B-field is shown in [Figure](#page-1-0) 2b. I_{SW} is plotted as a function of V_{sg} at different values of magnetic field up to 2 T. No significant change in $V_{\text{sg},\text{C}}$ with increasing *B*-field was observed, which is in contrast to the dependence observed for Ti and Al nanostructures.^{[7](#page-6-0),[23](#page-7-0)} [Figure](#page-1-0) 2c and d show the dependence of I_{SW} on *B*-field under influence of temperature *T* and V_{sv} respectively. In the former case, I_{SW} decreases with increasing T , as expected, accompanied by a suppression of B_C , giving $B_C = 2$ T at 800 mK and $B_C = 1.5$ T at 900 mK. In the case of the gate control, I_{SW} also decreases with increasing V_{sg} , but surprisingly, *no change in* B_C *was observed*. For a better comparison, [Figure](#page-1-0) 2e shows a zoom-in of the curves in both dependencies marked by the red rectangle and having almost the same magnitude of I_{SW} (at $B = 0$ T). It can be clearly seen that the B_C dependence behaves differently under the influence of temperature and gate voltage. While from 900 mK to 950 mK B_C further decreases from 1.5 to 1 T, I_{SW} does not seem to be suppressed by the magnetic field in the case of the gate (see also the [Supporting](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf) [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)), in strong contradiction to other works in which a significant change of B_C with gate voltage was observed.^{[10](#page-6-0)[,16,23](#page-7-0)}

Another noticeable difference between temperature and gate dependence is that *I_{SW}* exhibits large fluctuations at finite gate voltages (see green curves in [Figure](#page-1-0) 2e). In order to investigate

this effect, the switching current distribution (SCD) at finite temperatures and gate voltages is measured by ramping the current at constant speed from 0 to 3 *μ*A for 10,000 times and recording the corresponding I_SW value every time (see [Methods](#page-5-0)). A comparison between the SCDs obtained at 600 mK and 3 V is shown in [Figure](#page-1-0) 2f. Despite the fact that both histograms have almost the same mean value $\langle I_{SW} \rangle$, the width of the histogram obtained under influence of the gate voltage is an order of magnitude larger than that obtained at elevated bath temperature. The large gate-induced broadening is consistent with refs [14](#page-6-0), [19](#page-7-0), [22,](#page-7-0) [26,](#page-7-0) and [28](#page-7-0) and shows that the gate voltage induces an out-of-equilibrium state in the superconducting nanowire, which cannot be described with an effective temperature.

In the following, we will compare the SCDs measured at positive and negative gate polarity, as they are expected to behave differently for different microscopic origins of the GCS. The dependence of I_{SW} on V_{sg} of the device is shown in the inset of [Figure](#page-2-0) 3a, where the positive and negative gate polarities are represented by the orange and blue curves, respectively. [Figure](#page-2-0) [3](#page-2-0)a shows the SCDs measured at the same $|V_{\text{se}}|$ but with opposite polarities are paired and shifted along the *y*-axis for clarity. For simplicity, we made the measurements with the Al leads in the normal state, at $B = 100$ mT.^{[23](#page-7-0)} There is a clear difference in the shape and $\langle I_{SW} \rangle$ of SCDs paired at equal $|V_{sg}|$. In addition, we also paired SCDs for opposite gate polarities and with approximately the same power dissipated at the gate $P_G = I_{leak}$. *V*sg as shown in [Figure](#page-2-0) 3b. Comparing [Figure](#page-2-0) 3a and b, one can conclude that the pairing at the same power gives a better match between SCDs with opposite polarities. We also found that the SCDs measured at positive polarity have a slightly smaller $\langle I_{SW} \rangle$ than those measured at negative polarity at the same $P_{\rm G}$ (see inset in [Figure](#page-2-0) 3b).

Assuming that the electric field *E* applied by the gate [\(Figure](#page-2-0) [3](#page-2-0)c) is responsible for the suppression of I_{SW}^{29-33} I_{SW}^{29-33} I_{SW}^{29-33} I_{SW}^{29-33} I_{SW}^{29-33} its effect should not depend on the sign of *E*. Therefore, we expect the SCD obtained at a given voltage V_{sg} to be identical to the SCD obtained at the same gate voltage with the opposite sign, $-V_{sg}$. Since the measured SCDs do not match at opposite polarities (see [Figure](#page-2-0) 3a), our results contradict the electric field-based explanation. Another possible microscopic picture is that the CGS is caused by ballistic injection of high-energy quasiparticles, as shown in [Figure](#page-2-0) 3d. After injection of these electrons, their energy is released by relaxation, heating the side on which they end up. Therefore, for negative gate polarity [\(Figure](#page-2-0) 3d), they heat the superconducting bridge, while for positive polarity they heat the gate electrode instead. Thus, a stronger suppression of superconductivity is expected for negative polarity. Therefore, at the same P_G value, the mean value of the distribution is expected to be significantly smaller for negative polarity than for positive polarity. Comparing this prediction with the measured results in [Figure](#page-2-0) 3b, one can conclude that the experimental findings are just opposite, so that ballistic injection of electrons can also be excluded.

The most likely explanation for our results is the generation of phonons by a series of relaxation events of the high-energy electrons in the substrate.²⁸ The small shift between the $\langle I_{SW} \rangle$ measured for the two polarities (see [Figure](#page-2-0) 3b) can be attributed to the short energy relaxation length of electrons in $SiO₂$ (\leq 3 nm) at high electric fields compared to nanowire−gate spacing $(d = 30 \text{ nm})$.^{[39](#page-7-0)–[42](#page-7-0)} Thus, at positive gate polarity, it is expected that the high-energy electrons will relax close to the nanowire ([Figure](#page-2-0) 3e, left panel), and the generated phonons can heat the

superconducting nanowire more than at negative gate polarity ([Figure](#page-2-0) 3e, right panel).

The standard deviation *σ* of SCDs measured under the influence of the gate is represented by the blue curve in [Figure](#page-3-0) [4](#page-3-0)a. For small values of |*V*sg|, where *I*leak is negligible, *σ* is independent of $|V_{\text{se}}|$ and no significant change in the $\langle I_{\text{SW}} \rangle$ of SCDs (green curve) was observed. Beyond V_{th} at $|V_{sg}| = 2.7$ V, σ increases with $|V_{\text{se}}|$ because the fluctuations assisted by I_{leak} become stronger and more frequent. This increases the probability of nanowire switching at small I_{SW} values with a corresponding suppression in the $\langle I_{SW} \rangle$ of the SCD. This increase in the width of the SCDs is analogous to the typical temperature dependence (see the [Supporting](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf) Informa tion tion tion ^{[14](#page-6-0),[19](#page-7-0),[43](#page-7-0)} associated with thermally activated phase slips.^{[44](#page-7-0),[45](#page-7-0)} However, the large width of the SCDs obtained under the influence of the gate indicates that the system is driven to a nonequilibrium state where the fluctuations are an order of magnitude larger than expected from the bath temperature. With further increasing $|V_{\text{so}}|$, σ decreases and the SCDs become more symmetric, as shown by their calculated skewness in [Figure](#page-3-0) [4](#page-3-0)b. This is analogous with the picture that the switching of the system is due to multiple phase slips (MPS) found at finite temperatures.^{[43](#page-7-0)}

Interestingly, the SCD in [Figure](#page-2-0) 3a at $V_{sg} = 2.8 \text{ V}$ (orange curve) shows two peaks, a sharp one at 1.57 *μ*A and a broad one around 1.5 *μ*A. This distribution looks like the sum of two overlapping probability distributions, similar to distributions shown in refs [14](#page-6-0) and [22](#page-7-0). Since the probability distribution in this transition region depends strongly on the ramp speed of the bias current ν_{I} (see the Supporting [Information\)](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf), we could completely switch between the two distributions when the ramp speed was changed from 300 (at which the SCDs in [Figure](#page-2-0) [3](#page-2-0) are measured) to 9.375 μ A/s. For a more accurate evaluation, it is better to transform the measured probability distributions into the speed-independent escape rate $\Gamma(I, T)$ (see the Supporting [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)) by the direct Kurkijärvi-Fulton-Dunkleberger (KFD) transformation:[45](#page-7-0)[−][47](#page-7-0)

$$
\Gamma(I_{N}, T) = \frac{P(I_{N}, T)\nu_{I}}{1 - w \sum_{k=0}^{N} P(I_{k}, T)}
$$
\n(1)

where w is the bin size in the current axis of the measured probability distribution $P(I, T)$, and $P(I_k, T)$ is the switching probability in the bias current interval $[kw, (k + 1)w]$ with $k \in$ [0, *N*]. $\Gamma(I_N, T)$ represents the rate at which the superconducting order parameter reaches zero under the influence of external fluctuations. [Figure](#page-3-0) 4c shows the logarithm of the calculated $\Gamma(I_N, T)$ as a function of current for SCDs measured under the influence of V_{sg} in the interval $[-3.5, -2.7 \text{ V}]$. As long as V_{sg} is small, the SCDs have a sharp peak around $I_{\text{SW}} = 1.57 \ \mu\text{A}$, resulting in a large escape rate around this value, which represents the escape rate due to quantum tunneling or thermal escape Γ_{T} . As the influence of the gate voltage sets in (see, e.g., purple curve), a finite escape rate appears at lower *I*_{SW} values, corresponding to the gate-assisted escape rate Γ_{L} . The latter contribution becomes the dominant escape rate at higher gate voltages (see, e.g., green curve).

For V_{sg} > −3 V, where I_{leak} is negligible (the first three curves from the right), $\Gamma_{\rm L}$ can be well fitted with an exponential curve (black solid line) given by

$$
\Gamma_{\rm L}(I_{\rm SW}) = A e^{n\alpha I_{\rm sw}} \tag{2}
$$

with $n = 1$ and using α and A as fitting parameters. The switching dynamics in this region have been extensively studied in detail in ref [22.](#page-7-0) In this regime, the fluctuation events triggered by the gate were assumed to be rare and independent, and the dependence of the escape rate on the current is fitted by a single exponential. For $V_{\text{sg}} \leq -3$ V, Γ_{L} deviates from the single-exponential dependence described by eq 2. For example, the light green curve measured at −3.2 V can be fitted at large current values using eq 2 with $n = 1$ (see black solid lines). Interestingly, the measured curve for I_{SW} < 0.9 μ A can be well fitted by adding extra higher order terms with $n = 2, 3, ...$, keeping the same values of the fitting parameters. Further increasing V_{sg} (I_{leak}) requires more higher order terms to fit the escape rate dependence (e.g., orange curve).^{[43](#page-7-0)} The value of α required to fit the escape rate dependence decreases sharply as V_{sg} increases, and saturates at large values of V_{sg} (I_{leak}) as shown in the red curve in the inset of [Figure](#page-3-0) 4c, while the corresponding I_{leak} is shown in the gray curve.

The deviation of the escape rate dependence with current from a pure exponential at higher gate voltages is similar to elevated temperatures in ref [43.](#page-7-0) This can be attributed to the reduced impact for a single fluctuation event triggered by the leakage current, since the dissipation during the induced phase slip event is smaller at lower values of $I_{SW}^{(43,45)}$ $I_{SW}^{(43,45)}$ $I_{SW}^{(43,45)}$ Thus, several coincident fluctuation events with corresponding induced MPS are required to trigger the switching of the nanowire to the normal state.^{43,[48,49](#page-7-0)} In this regime, at large bias current values, the dissipation of a single MPS event $(n = 1)$ is sufficient to switch the nanowire into the resistive state. On the other hand, at lower current values, the dissipation of a single MPS event is reduced and higher orders $(n = 2, 3, ...)$ of the MPS event are required to trigger the resistive switching of the nanowire.^{[43](#page-7-0)}

In the following, we will compare our experimental results with the possible microscopic pictures. Starting from the two gates [\(Figure](#page-1-0) 1d,e), despite SG2 having almost twice the nanowire−gate spacing of SG1, it suppresses the *I*_{SW} at lower *V*_{th} than SG1. This contradicts the electric field picture as a possible explanation for the origin of the GCS. On the other hand, I_{SW} starts to be suppressed with the onset of leakage current between the nanowire and each of the gates (see the [Supporting](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf) [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)). In another cool-down, the influence of the two gates for the same device shows an opposite situation, as SG1 shows a stronger influence on *I*_{SW} than SG2 (see the [Supporting](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf) [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)). This excludes any concerns arising from the quite large dielectric constant of the InAs nanowire between SG2 and the Ta shell (see [Figure](#page-1-0) 1a), which may lead to a larger influence of SG2 on I_{SW} than SG1. Interestingly, we found that the influence of the two gates on I_{SW} gives better matching with P_G in the two cool-downs (see the Supporting [Information\)](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf).

Accepting that the leakage current plays a key role in the GCS, a simple explanation arises: that the leaking electrons increase the temperature of the superconducting nanowire. We have investigated the *B*-field dependence of a superconducting nanowire with normal contacts, which allows efficient cooling of the superconducting nanowire. The *B*-field dependence at finite *T* and finite gate voltage was strictly different, indicating that the effect of leakage current cannot be described by a simple hot electron regime induced by elevated bath temperature. The highly nonequilibrium state of the superconductor at finite gate voltage is further supported by the broad SCDs in our work and in previous results.^{[14](#page-6-0),[19,22](#page-7-0),[26](#page-7-0),[28](#page-7-0)} Our detailed comparison of the SCDs for different gate polarities ([Figure](#page-2-0) 3) provided another important finding which is inconsistent with electric-fieldinduced suppression of superconductivity. Pairing of SCDs measured at opposite gate polarities at the same leakage current dissipation, P_G , provided a better matching than at the same $|V_{se}|$ ([Figure](#page-2-0) 3a,b). This reveals that the suppression of I_{SW} depends not only on the energy of the injected electrons (eV_{sg}) or the rate of their injection (*I*leak/e) but on the power dissipated at the gate, P_{G} . Based on the $\langle I_{\text{SW}} \rangle$ of the SCDs for the two polarities, the ballistic injection of electrons from the gate into the superconducting nanowire can be discarded. We conclude that the phonon-mediated excitation of the superconductor remains a microscopic picture consistent with the measured results.

Furthermore, we also noticed that the power dissipation at the gate required to fully suppress I_{SW} , $P_{G,C}$, is comparable to the power dissipation that occurs when the device switches to the resistive state, $P_n = I_{SW}^2 \cdot R_n$. For example, for device A, in the case of SG1 (the closer to the Ta shell), $P_{\text{G,C}} \simeq 1.5 \text{ nW}$ (see the Supporting [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)), while $P_n \simeq 1$ nW (using $R_n = 780$ Ω and $I_{SW} \simeq 1.17 \mu A$).

Finally, a very large leakage current was required to quench I_{SW} when we investigated the GCS in similar Ta/InAs devices fabricated on a sapphire substrate (see the [Supporting](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf) [Information](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)). These results indicate that the GCS depends mainly on the properties of the substrate and the leakage pathway between the gate and nanowire.

CONCLUSIONS

We investigated the origin of GCS in the Ta half-shell layer deposited on InAs nanowires by various measurements. Devices with small nanowire−gate spacing (specifically devices B and C) fully switch to the normal state below $V_{sg} = \pm 5$ V, which makes them promising for integration into classical electronic circuits. When the wire is connected by electrodes in the normal state, the critical magnetic field B_C is not suppressed under the influence of the gate as for elevated temperatures. Moreover, the comparison of the switching current distributions at opposite gate polarities, as well as the gate dependence of two opposite side gates at different nanowire−gate spacings, shows that the power dissipated at the gate (P_G) is the relevant parameter for this effect. Analysis of the switching dynamics under strong gate influence shows a deviation in the escape rate dependence with the bias current from a pure exponential. This indicates that the device is driven into the MPS regime by the high-energy fluctuations originating from the leakage current. The measurements on our devices are consistent with the nonequilibrium superconducting state resulting from the absorption of phonons generated by the leakage current and contradict the microscopic pictures proposing electric fields or ballistic injection of highenergy electrons as the origin of the GCS effect. GCS is a robust effect; it has been reported so far in very different circumstances: using various substrates and superconductors, different geometries, and even in suspended nanobridges 13 or ionic gating. 21 Since many of these measurements were done under very different experimental conditions, it is hard to make a direct comparison between the experiments. Furthermore, it is not obvious that a single mechanism should be expected to be responsible for all the measurements in the literature. Therefore, further investigations are required to reach a solid understanding of the contribution of different microscopic processes, which is essential to the use of GCS in future applications.

METHODS

InAs nanowires were grown by the VLS mechanism using molecular beam epitaxy and the Ta shell was deposited in situ under UHV using electron beam evaporation at a substrate temperature of about 25 °C. Based on the TEM characterization, the morphology of the Ta shells was continuous but granular on the InAs nanowires and was found to be noncrystalline.[38](#page-7-0)

Table 1. Dimensions of the Investigated Nanowire Devices

device	$L_{NW}(\mu m)$	d_1 (nm)	d_2 (nm)
A		65	115
B		35	115
€		30	120

The Ta/InAs nanowires with a total diameter of ≃100 nm were deposited on the top of a doped Si wafer with a 290-nm-thick $SiO₂$ layer by means of a hydraulic micromanipulator along with a highmagnification optical microscope. The nanowire device was fabricated in two separate electron beam lithography (EBL) steps. In the first step, four Ti/Al contacts with a thickness of 10/80 nm were fabricated. Prior to the metal evaporation, Ta/InAs nanowires were exposed to Ar-ion plasma milling for 8 min at 50 W to remove any oxides on the top of the Ta shell. In the second step, two metallic gates of Ti/Au layers with a thickness of 7/33 nm were fabricated with unequal spacing and on opposite sides of the nanowire. The metallic gates were fabricated in a separate lithography step, since a thin resist is used for precise alignment of the gates from the nanowire. Table 1 shows the dimensions of the investigated nanowire devices where L_{NW} is the nanowire segment length and *d*₁ and *d*₂ are the nanowire−gate spacings of gates SG1 and SG2, respectively.

The *I*−*V* characteristics of the device were measured by a pure DC measurement using a quasi-four-probe method in which the current was injected through the nanowire via a pair of Al contacts by using a standard voltage source (Basel DAC SP 927) with a series resistor of 1 MΩ, while the voltage was measured across the other pair with a differential voltage amplifier and a digital multimeter (Keithley 2001). The leakage current was recorded by measuring the voltage across a 10 MΩ preresistor connected to the gate and corrected according to the method reported in ref [23](#page-7-0).

The SCD was measured using an NI-DAQ card (USB-6341), where a periodic current wave signal was engineered. This signal is composed of a positive linear ramp with an amplitude of 3 *μ*A and a slope in the range from 9.375 to 300 μA/s followed by a 2.5 ms zero-current plateau for cooling down the superconducting device. This signal is repeated 10,000 times, and I_{SW} is extracted each time. All SCDs are measured at 0.1 T to switch the Al leads to the normal state. The skewness is calculated from the measured SCDs as

Skewness =
$$
\frac{1}{N} \sum_{k=1}^{N} \frac{(I_{SW,k} - \langle I_{SW} \rangle)^3}{\sigma^3}
$$
 (3)

where $\langle I_{SW} \rangle$ and σ are the mean value and standard deviation of the SCD. All measurements were carried out in a Leiden Cryogenics CF-400 top-loading cryo-free dilution refrigerator system with a base temperature of 30 mK.

ASSOCIATED CONTENT

\bullet Supporting Information

The Supporting Information is available free of charge at [https://pubs.acs.org/doi/10.1021/acsnano.2c10877](https://pubs.acs.org/doi/10.1021/acsnano.2c10877?goto=supporting-info).

> Gate dependence of the supercurrent for devices B and C, magnetic field dependence under the influence of the gate, temperature dependence of SCD, dependence of SCD and escape rate on the current ramp speed, comparison between the influence of two opposite side gates for device A, investigation of device A in another

cool-down, dual-gate measurement, and measurements on different substrates ([PDF\)](https://pubs.acs.org/doi/suppl/10.1021/acsnano.2c10877/suppl_file/nn2c10877_si_002.pdf)

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Author Contributions

T.E. and M.B. fabricated the devices, and T.E., M.B., M.K., G.F., and Z.S. performed the measurements and did the data analysis. T.K. and J.N. developed the nanowires. All authors discussed the results and worked on the manuscript. P.M. and S.C. guided the project.

Notes

The authors declare no competing financial interest.

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