

Maximal gene number maintainable by stochastic correction – The second error threshold

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Abstract

There is still no general solution to Eigen's Paradox, the chicken-or-egg problem of the origin of life: neither accurate copying, nor long genomes could have evolved without one another being established beforehand. But an array of small, individually replicating genes might offer a workaround, provided that multilevel selection assists the survival of the ensemble. There are two key difficulties that such a system has to overcome: the non-synchronous replication of genes, and their random assortment into daughter cells (the units

25 of higher-level selection) upon fission. Here we find, using the Stochastic Corrector Model
26 framework, that a large number ($\tau \geq 90$) of genes can coexist. Furthermore, the system can
27 tolerate about 10% of replication rate asymmetry (competition) among the genes. On this
28 basis, we put forward a plausible (and testable!) scenario for how novel genes could have
29 been incorporated into early evolving systems: a route to complex metabolism.

30 **Highlights**

- 31 • We find that the non-synchronous replication of genes and their random assortment
32 into daughter cells result in a threshold-like drop in the maintainable number of
33 individually replicating genes. We term this phenomena the second error threshold in
34 reference to the first error limit caused by mutations (cf. Eigen's Paradox)
- 35 • Multilevel selection can supports no less than a 100 genes: the larger the cells are, the
36 more genes they can uphold
- 37 • This system can mitigate a limited amount of competition asymmetry, further aiding the
38 coexistence of genes

39 **1. Introduction**

40 It has been forty years since Manfred Eigen proposed the theory that mutations in
41 molecular replication, a phenomenon considered conducive to the adaptation and speciation
42 of the extant biota, could have posed a fundamental obstacle to the spontaneous formation of
43 life (Eigen, 1971). The idea can be presented simply: early living systems lacking proof-
44 reading processes had to tolerate a high rate of mutation; such mutation pressure precludes
45 sustaining information in long chromosomes; but shorter genomes are unable to store proof-
46 reading enzymes. For example, in the RNA world scenario “one cannot have accurate
47 replication without a length of RNA, say, 2000 or more base pairs, and one cannot have that

48 much RNA without accurate replication” (Maynard Smith, 1979). This is Eigen’s Paradox
49 which still troubles origin of life research: maintenance of information is a central topic of this
50 field (Kun et al., 2015).

51 The notion of the error threshold was put forward with DNA genomes and peptide
52 enzymes in mind. The 2000 base long RNA in Maynard Smith’s example would code for an
53 enzyme of length 600+. A quick look at UNIPROT yields DNA-dependent DNA polymerases
54 (E.C. 2.7.7.7) that are smaller than this, albeit mostly DNA polymerase IV, which is quite
55 error prone. On the other hand, reliable information replication evolved during the RNA
56 world (Joyce, 2002; Kun et al., 2015; Yarus, 2011). The RNA world is the era in the history
57 of Earth during which information was stored in RNA and catalysis was mostly done by RNA
58 enzymes (ribozymes). At the moment there is no known general RNA-based RNA
59 polymerase ribozyme. There is a ribozyme which can catalyse the template based
60 polymerization of up to 98 nucleotides (Wochner et al., 2011), and given a very specific
61 template a ribozyme can copy longer strands as well (Attwater et al., 2013) on par with its
62 size of roughly 200 nucleotides. Still 200 nucleotides is a long sequence when we take
63 prebiotic replication fidelity into account (<99%, (Orgel, 1992)).

64 The error threshold, in the simplified treatment of John Maynard Smith (1983), is:
65 $L < \ln s / \mu$, meaning that the maximum sustainable genome size (L) is less than the quotient
66 of the natural logarithm of the selective superiority (s) of the sequence to be copied
67 (‘master’) and the error rate (μ). Selective superiority is the ratio of the average Malthusian
68 growth rates of selected sequences (here, only the master) versus the rest (here, its mutants).
69 Let us say that the error rate is $\mu = 0.01$ (Orgel, 1992). Based on the above inequality, this
70 only allows the sustainment of sequences shorter than $L < 100$ monomers (with the standard
71 assumption that $\ln s \approx 1$). Thus the putative replicase ribozyme of 200 bases length (Wochner
72 et al., 2011) seems to be too long.

73 Recent advances paint a brighter picture. An order of magnitude longer functional
74 ribozymes can be maintained (with the error rate being equal) if the structure of the
75 ribozymes, and the neutral mutations it allows, are taken into account (Kun et al., 2005;
76 Szilágyi et al., 2014; Takeuchi et al., 2005). Second, it seems that intragenomic recombination
77 may have shifted the threshold by about 30% (Santos et al., 2004). Third, the processivity of
78 replication (i.e. the constraint that during template-based replication, nucleotides have to be
79 inserted one by one into the growing copy) may have somewhat filtered against errors,
80 provided erroneous insertions had slowed down replication (Huang et al., 1992; Mendelman
81 et al., 1990; Perrino and Loeb, 1989): erroneous copies would have thus suffered from an
82 inherent fitness disadvantage (Leu et al., 2012; Rajamani et al., 2010). It may also have
83 alleviated the error threshold by about another 30%.

84 While such a relaxed error threshold seems less problematic, the replication of whole
85 genomes that could run a primitive metabolism is still out of reach. Ribocells (cells whose
86 metabolism is run by RNA enzymes) require at least one ribozymes of each of the essential
87 enzymatic functionalities to be considered viable: they can produce the biomass component
88 necessary for growth and reproduction. Cells lacking even one of the functions cannot
89 reproduce. Thus all information needs to be replicated, which can only be done if all
90 ribozymes replicate individually. Individual known ribozymes are short enough to be
91 faithfully copied (Szilágyi et al., 2014). However, if individual genes are replicated, they have
92 individual growth rates inside the cell. Sequences having the highest growth rates will
93 dominate the ribozyme population, and other genes will be lost (cf. the Spiegelman
94 experiment (Kacian et al., 1972)). Thus while the error catastrophe can be overcome by
95 replicating the whole set of genes required for the cell as individual replicators, it creates
96 another problem, that of non-synchronous replication. How much information can be

97 integrated via the compartmentalization of individually replicating ribozymes? Is such a
98 system complex enough to overcome the error catastrophe?

99 The Stochastic Corrector Model (SCM) is a group selection / package model framework; it
100 was developed to investigate the above compartmentalized system, which has the potential to
101 solve the problem of information integration. Szathmáry and Demeter (1987) have shown that
102 given a low number of replicators inside a cell having a far from optimal copy number
103 distribution (the goal distribution can be arbitrary), stochastic separation of the genes into the
104 daughter cells can ameliorate the copy number distribution of the parent cells. Previous works
105 on the SCM have focused on cells with only two (Grey et al., 1995; Zintzaras et al., 2010) or
106 three genes (Zintzaras et al., 2002). A few enzymes can coexist without a problem even
107 without full compartmentalization, i.e. on surfaces (Boerlijst, 2000; Czárán and Szathmáry,
108 2000; Hogeweg and Takeuchi, 2003; Könnyű and Czárán, 2013; Takeuchi and Hogeweg,
109 2009). And in vesicle models the coexistence of a few enzymes was demonstrated (Hogeweg
110 and Takeuchi, 2003; Takeuchi and Hogeweg, 2009). But, the maximal number of coexisting
111 genes was not investigated except by Fontanari *et al.* (2006), who have shown that arbitrary
112 number of genes can coexist, if their replication rates are the same and the population size is
113 infinitely large. However, neither of these assumptions is realistic—and as we will show—both
114 of them critically affect the outcome.

115 Here we investigate how many independently replicating genes can coexist in a cell,
116 despite the potential for information loss due to random assortment to daughter cells and non-
117 synchronous replication. Information loss due to mutations in individual ribozymes is not
118 investigated here. We already know that the error threshold limit the amount of information
119 that can be maintained, and including it now would hamper our ability to assess how many
120 genes can coexist despite different replication rates and random assortment into daughter
121 cells? We show that these also limit the sustainable length of information. To distinguish

122 these two sources of limitation, we term Eigen's limitation 'first error threshold' and the
123 limitation investigated here 'second error threshold'.

124 **2. Methods**

125 We follow the dynamics of a population (N) of ribocells. The biomass of the cells is
126 produced by an abstract metabolism requiring τ different enzymatic functions. Ribozymes
127 (catalysts) replicate individually and there could be more than one ribozyme of each type in
128 the cell. The internal composition of the cell, i.e. the number of ribozymes and their
129 distribution among the metabolic functions, determines the metabolic activity (R_i), which in
130 turn affects the growth and replication of the cell. Accordingly, a cell i containing
131 $v_i \in [1, v_{\max}]$ independently replicating ribozymes distributed among the τ different genes

132 each having $v_{i,j}$ copies ($v_i = \sum_{j=1}^{\tau} v_{i,j}$) has a metabolic activity $R_i = \prod_{j=1}^{\tau} \left(\frac{\tau \cdot v_j}{v_i} \right)^{\varepsilon} \cdot \frac{v_i}{v_{\max}}$. Thus we

133 assume that each gene catalyses an essential reaction in the metabolic pathway, producing
134 intermediers (e.g. monomers) for the replication of the ribozymes. We further assume that
135 there is an optimal distribution in the copy number of the different ribozymes, which
136 corresponds to the highest metabolic activity inside the cell. We arbitrarily assign this
137 optimum to the most even distribution, where every different ribozyme (gene) is present with
138 an identical number of copies. We also presume that the greater the size of the cell, i.e. the
139 number of ribozymes it harbours, the faster its metabolic activity will be. An arbitrary
140 exponent (ε) weights these two components (evenness of distribution and ribozyme number).
141 In pilot studies, we found that a selection focusing on the inner distribution is beneficial for
142 the sustainability of the genome. In the studies to be presented we used $\varepsilon = 0.3$.

143 The population dynamics is the following: a cell is chosen randomly, in proportion to its
144 metabolic activity (R_i); this cell gains one new ribozyme. Next, a ribozyme (j) is chosen

145 randomly from the ribozymes in the selected cell, proportionately to its replicase affinity (a_j
146); this ribozyme is copied. The new ribozyme belongs to the same type and has the same
147 replicase affinity as its parent.

148 If the number of ribozymes inside a cell reaches a maximal number (v_{\max}), then the cell
149 splits into two. The ribozymes get into one of the daughter cells independently and randomly.
150 The two new cells take the place of the parent cell and another one, which will perish, chosen
151 randomly (with uniform probability): the population dynamics is a Moran process. Thus we
152 assume constant population size, and fitness independent death-rate.

153 Pilot studies have shown that 50 “generations”, i.e. $50N$ cell divisions, are enough for the
154 system to reach equilibrium.

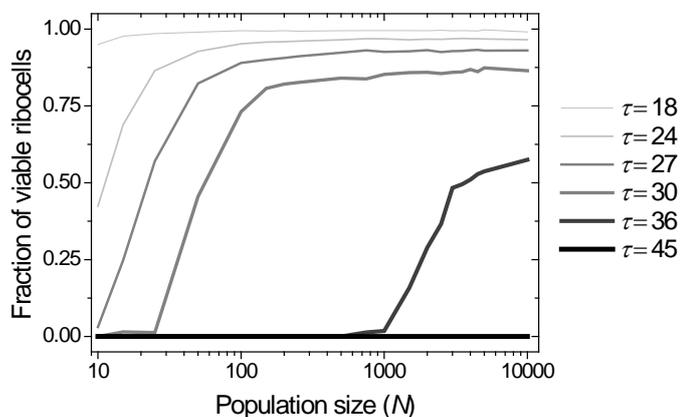
155 The initial cells start with cell $v_{\max}/2$ ribozymes, with each function (gene) represented
156 evenly.

157 **3. Results**

158 Genes can coexist in the SCM, and the parameter range in which coexistence is possible
159 increases with population size (N) (Fig. 1) and gene redundancy within the cell (Fig. 2),
160 furthermore, the more equal the replication rates of the individually replicating genes, the
161 more genes can coexist (Fig. 3).

162 A larger population size allows more genes (functionally different ribozymes) to coexist
163 (Fig. 1). This is not surprising, given the fact that an infinite population size guarantees
164 coexistence (Fontanari et al., 2006). However, it is also important to know how infinity is
165 approached. It seems that for most of the parameter space, an increase in population size has a
166 meagre effect on cell viability. Thus, while it is possible to increase population size to achieve
167 the coexistence of any number of genes, the additional population size required for it can be
168 unrealistically large; e.g. nearly two magnitudes of increase in population size do not raise the

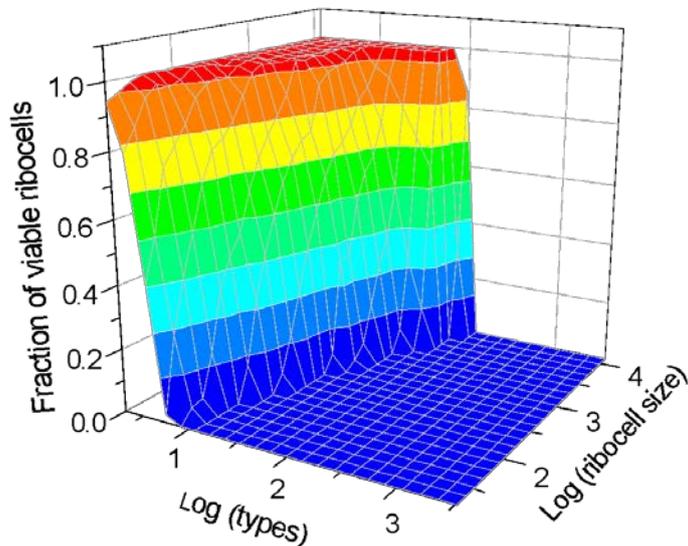
169 fraction of viable cell when $\tau > 45$. Because of computational limits, we did most of our
170 simulations with $N = 1000$. Thus our estimates are conservative, as increasing population
171 size would allow for a slightly greater coexistence of replicators.



172
173 **Figure 1. Fraction of viable cells increases with population size.** Darker and wider lines
174 represent systems with more required functions (τ). In all cases there are $v_{\max} = 2160$
175 ribozymes in the cells. All cells are viable if $\tau < 18$, and none is viable if $\tau > 45$.
176

177 Given a number of genes that need to coexist there exists a redundancy (maximum ribocell
178 size, which translates to more ribozymes of each type) that allows it. The transition between
179 the ribocell size that precludes coexistence and which ensures a viable population is
180 threshold-like (Fig. 2). Increasing the maximum number of ribozymes inside the cells, and
181 with it the achievable redundancy for each gene, increases the fraction of viable ribocells. The
182 increase is sigmoid in shape with a very steep increase at certain point. This point is the
183 second error threshold, i.e. the redundancy below which given number of genes cannot
184 coexist. Thus at any given ribozyme abundance, there is a maximum to how many genes can
185 coexist. Reaching a higher maintainable ribozyme diversity requires an increase in the number
186 of ribozymes a cell can harbour. As a good rule of thumb, the maintainable genetic diversity
187 (number of genes) is equal to the square root of the maximum number of ribozymes. At
188 $N = 1000$ about a 100 different ribozymes can coexist if a cell can house 10,000 ribozymes

189 per cell. Once a population passes the error threshold and becomes viable, further increase in
190 gene redundancy has negligible effect.



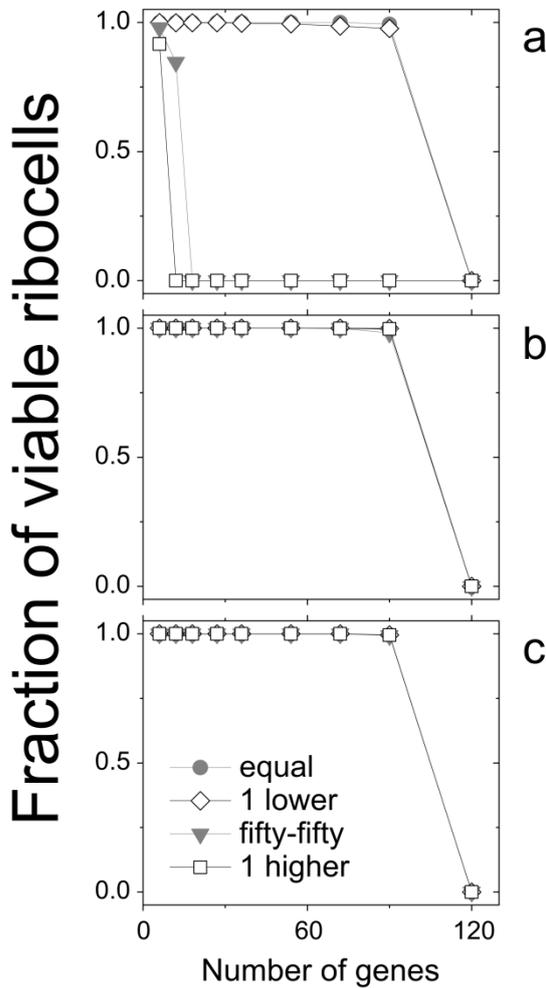
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192 **Figure 2. Maximum gene diversity.** The fraction of viable ribocells is displayed as
193 function of the number of types (τ) and the number of ribozymes per ribocell (ribocell
194 size, ν). Please note that the logarithm of the number of types and ribocell size is on the X
195 and Y axes, respectively.

196

197 The above investigations assume that each functionally different ribozyme (different
198 genes) has the same affinity to the replicase, thus there is no competition asymmetry in the
199 system. Three different scenarios are compared with the above results: (1) all affinities are the
200 same, except for the affinity of one of the ribozymes, which is higher; (2) all affinities are the
201 same, except for one, which is lower; and (3) affinities have two values, low and high, and the
202 ribozymes of half (or about half in the cases of an odd number of genes) the genes have low,
203 the other half have high affinity. Competition asymmetry causes the competitive exclusion of
204 some of the genes, and consequently the loss of viability of the cells. When affinities differ as
205 much as 10%, then in the case of a single competitively superior gene, coexistence is already
206 lost at $\tau = 12$ (Fig.3a). In the case when there is a single competitively inferior gene, a
207 considerable number of genes can coexist. In this case, the results are only different from the

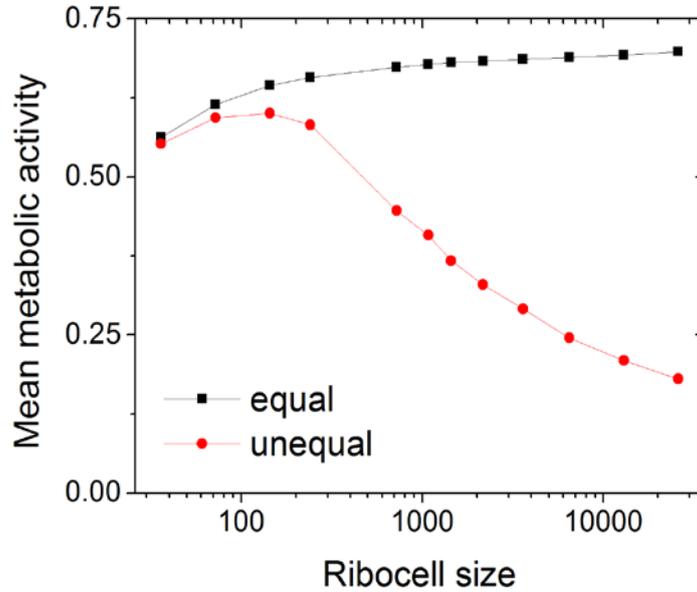
208 equal affinities scenario if $\tau \geq 96$ (Fig.3a). The stochastic corrector can tolerate all of these
 209 scenarios when the difference in the affinities is even lower, i.e. 1% (Fig.3b) or 0.1% (Fig.3c).
 210



211
 212 **Figure 3. Mean fraction of viable cells with non-equal affinities to the replicase.**
 213 "Equal" (solid square) $a_{1..\tau} = 1$; "One lower" (open upward triangle) $a_{1..(\tau-1)} = 1$ and $a_{\tau} = \alpha$
 214); "1:1" (solid circle) $a_{1..(\tau/2)} = 1$ and $a_{(\tau/2)+1..\tau} = \alpha$; and "one higher" (open downward
 215 triangle) $a_1 = 1$ and $a_{2..\tau} = \alpha$. (a) $\alpha = 0.9$, (b) $\alpha = 0.99$, (c) $\alpha = 0.999$. Symbols represent
 216 means from 10 iterations. Other parameters $g = 100000$; $v_{\max} = 25920$; $\varepsilon = 0.3$.

217
 218 We found that the relationship between the effect of asynchronous replication and the
 219 genetic composition of the ribocell (cf. metabolic activity) depends on the maximal cell size
 220 (Fig. 4). While a larger ribocell promotes a more even composition for equal replicase

221 affinities, for an unequal distribution ($\alpha = 0.9$) this leads to a more adverse composition
222 instead. There seems to be an optimal protocell size for asynchronous replication where
223 despite the differences in replicase affinity a mostly even composition is sustained.



224
225 Figure 4. The effect of redundancy on asynchronous replication. In this minimal system of
226 two genes ($\tau = 2$) we compared replicase affinities of equal distribution ($a_1 = a_2 = 1$) with
227 those of an unequal distribution ($a_1 = 0.9, a_2 = 1$). The two lines show a divergent trend with
228 the growth of protocell size. Note the logarithmic scale. Parameters $g = 100000$; $N = 1000$, $t =$
229 2 , $\varepsilon = 0.3$.

230 4. Discussion

231 Non-synchronous replication and random assortment leads to a threshold-like decrease in
232 the viability of ribocells as the number of type increases. Thus there is a limit to the enzymatic
233 diversity that can be maintained in an ancient cell. We term this limit the second error
234 threshold. Despite the second error threshold a sizable number of genes can coexist. Here we
235 have shown that as many as 100 different genes (types) can coexist if internal copy number is
236 moderately high and affinities do not differ by more than 1%.

237 **4.1 Assumptions of the model**

238 The computational analysis presented in this paper focuses on the phenomena we call the
239 second error threshold. For this reason, we have excluded mutations from our current model.
240 We understand that excluding possible mutations in the enzymatic activities can affect our
241 results. Increasing mutational rate can push the population over the error threshold (Kun et al.,
242 2015; Takeuchi and Hogeweg, 2012). Here we show that assortment load also leads to a
243 threshold-like change in the viability of the population, independently of the first error
244 threshold. Mutations can also produce parasites, sequences that do not contribute to biomass
245 production, but which contribute to cell size. Thus cells might divide harbouring few enzymes
246 and many parasites, leading to deficient daughter cells with a higher probability. On the other
247 hand, such cells have a severe selective disadvantage, and they would divide at a slower rate
248 compared to cell having few parasites. Efficient information integration despite the presence
249 of parasites were demonstrated in the stochastic corrector model framework (e.g. (Zintzaras et
250 al., 2002)), albeit for only 3 genes. The interplay of the two error thresholds will be revisited
251 in a future study.

252 We assume that the limiting factor in the metabolism of the cells is the number of enzymes
253 present. Food scarcity is irrelevant, as it does not differentiate between the ribocells, thus
254 would not affect selection.

255 The employed fitness function assumes that an uniform distribution of every different
256 ribozyme has the highest replication rate. It can be understood as either a linear (serial) set of
257 all-essential reactions (for example, a chain of reactions that transform food molecule to
258 monomers), or parallel pathways with equally important end-products (for example, the
259 parallel production of all NTPs). In essence an arbitrary metabolic network can be employed,
260 and the metabolic flux through the network can be used as a proxy for fitness (as used in
261 (Szilágyi et al., 2012)). The added complexity of flux calculation can pose a technical

262 difficulty, as the computational requirement is already quite high, and would necessitate other
263 simplifying assumptions.

264 **4.1. Minimal gene number of a ribo-organism**

265 Minimal genome sizes found in contemporary organism can be as low as 112 kbases:
266 *Nasuia deltocephalinicola* (112 kbases) (Bennett and Moran, 2013), *Tremblaya princeps* (139
267 kbases) (McCutcheon and von Dohlen, 2011), *Hodgkinia cicadicola* (144 kbases) (McCutcheon
268 et al., 2009), *Sulcia muelleri* (146 kbases) (Chang et al., 2015; McCutcheon and Moran, 2007;
269 McCutcheon and Moran, 2010; Woyke et al., 2010; Wu et al., 2006), *Carsonella ruddii* (160
270 kbases) (Tamames et al., 2007), *Zinderia insecticola* (208 kbases) (McCutcheon and Moran,
271 2010). However, these symbionts of insects are barely alive in the sense that they lack genes
272 for membrane and cell wall synthesis, lack transporters, most of carbon metabolism
273 (McCutcheon and Moran, 2010) and some even lack some genes for DNA replication and
274 translation. Other symbionts and intracellular parasites have genomes of around 600 kbases
275 (*Mycoplasma genitalium*, *Buchnera* sp. (Islas et al., 2004)) and these minimalistic cells
276 contain around 500-600 genes. However, the smallest possible genome size could have been
277 even less (Luisi et al., 2006; Szathmáry, 2005): around 200 (Gil et al., 2004) (Table 1). These
278 estimates pertain to cells having a DNA genome and peptide enzymes. A minimal ribo-
279 organism can do with less. Jeffares *et al.* (1998) suggested that the last ribo-organism had a
280 genome of 10,000-15,000 base pairs. This estimate includes ribozymes involved in translation
281 and RNA replication, but it lacks enzymes for the control of cell division and the estimates for
282 intermediate metabolism is rather arbitrary. The last ribo-organism most probably had
283 translation, but we are more interested in the first cells, and not in the ones just on the verge to
284 switch to DNA genomes.

285 A ribocell requires enzymes for the replication of its genetic material, chaperons for its
286 ribozymes, maybe some enzymes that alters ribozymes much like post-translational

287 modification alters peptide enzymes. Cellular processes, such as transport, also need some
 288 RNA enzymes. Moreover, the NTPs (both as monomers for RNA synthesis and as energy
 289 molecules), coenzymes and lipids need to be produced. A good estimate for the minimal
 290 intermediate metabolism covering said functionalities is given by Moya and co-workers
 291 (Gabaldón et al., 2007), who suggested 50 enzymes to be the minimum. We have to note that
 292 this set also included enzymes for dNTP production, which a ribo-organism did not need. A
 293 conservative estimate of 88 ribozymes is afforded by this back of the envelope calculation
 294 (Table 1). Most probably even fewer ribozymes would be enough, as this set of 88 contains
 295 multi-subunit enzymes as well (Gil et al., 2004). We have estimated 60 to be a minimum
 296 (Szilágyi et al., 2012), a more detailed analysis of the minimal set of genes required for a
 297 ribocell will be proposed later (Kun *et al. in prep*).

298 It is clear that even with 0.99 replication fidelity, a chromosome packed with 60 genes
 299 cannot be maintained due to the first error threshold. Sixty or even a hundred individually
 300 replicating genes can be maintained in randomly assorting ribocells. We thus conclude that
 301 the information required for a minimal ribocell can be propagated despite the second error
 302 threshold.

303 **Table 1. Estimate of a minimal gene set for a ribo-organism**

| Function | Number of gene in a DNA-peptide organism | Number of gene in a ribo-organism | Notes |
|--|--|-----------------------------------|-----------------------------|
| Replication of the genetic information | 16 | 16 | |
| translation | 106 | 0 | |
| Enzyme folding, modification and translocation | 15 | 15 | |
| Cellular processes | 5 | 5 | |
| Energetic and intermediary metabolism | 56 | 52 | no need for dNTP production |
| Total | 198 | 88 | |

304 **4.3 Possible evolutionary route to complex metabolism**

305 Metabolisms having hundreds of enzymes and molecules do not appear at once. Most
306 probably enzymes, and thus functions, were added one at a time (Szathmáry, 2007). A few
307 enzyme can coexist on surfaces (Boerlijst, 2000; Czárán and Szathmáry, 2000; Hogeweg and
308 Takeuchi, 2003; Könnnyű and Czárán, 2013; Takeuchi and Hogeweg, 2009) as well as in
309 vesicles (Hogeweg and Takeuchi, 2003; Szathmáry and Demeter, 1987; Takeuchi and
310 Hogeweg, 2009; Zintzaras et al., 2002). How can we get from a few enzymes to nearly a
311 hundred? The enhancement of metabolic capabilities afforded by more enzymes is surely
312 selectively advantageous. On the other hand if the new enzyme cannot establish or coexist
313 with the “old” ones, then this evolutionary step cannot be taken. Based on our results we can
314 propose a possible evolutionary route to increasing metabolic complexity, i.e. more genes.

315 Equal affinities to the replicator ensure that no replicator outcompete the others. Thus the
316 process could have started by a few (even two) ribozymes with equal replication rates. Now
317 let us assume that any novel enzyme has a lower affinity to the replicase than the already
318 established ones, then this enzyme can establish in the system, even if its affinity to the
319 replicase is lower by as much as 10% compared to the rest of the enzymes (cf. Fig. 3a).
320 Difference in affinities could not be very high: 60% difference is too much for the
321 maintenance of a mere 10 enzymes, which is still too few for a metabolism. However, new
322 enzymes probably evolved from established ones, and thus probably had tag sequences
323 compatible with the replicase. The system then can evolve to equalize all affinities (Kun
324 unpublished results), in this case to increase the affinity of the new enzyme. The simultaneous
325 addition of more enzymes drive the system to extinction, but the addition of a single one
326 seems to be feasible. Thus enzymes can be added one after the other with the requirement of
327 only slight difference in affinities to the replicator.

328 The proposed evolutionary scenario of gradual increase in metabolic complexity can
329 progress till the coexistence is no longer possible due to internal redundancy (Fig. 2), which
330 can be alleviated by increasing the cell's size at division. Cell sizes do not need to increase to
331 infinity or even to very high number: at a certain metabolic complexity replication efficiency
332 and fidelity could increase to a level at which a chromosome can be replicated. Then
333 integration of the genetic information a chromosome can evolve (Maynard Smith and
334 Szathmáry, 1993). The chromosome, a major evolutionary transition (Maynard Smith and
335 Szathmáry, 1995; Szathmáry, 2015; Szathmáry and Maynard Smith, 1995), is made possible
336 by overcoming the first error threshold. An intermediate solution to the first error threshold is
337 the individual replication of ribozymes, which introduces the second error threshold. The
338 second error threshold is alleviated by controlling the distribution of chromosome to the
339 daughter cells.

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