Comparison of protocol based cancer therapies and discrete controller based treatments in the case of endostatin administration

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Abstract — In the medical practice, there are several methods to administer anti-cancer drugs. A commonly used method is the intermittent bolus doses (BD) administration when the patient receives drug on given days and the therapy has rest periods between the injections. The amount of bolus doses can be the maximum tolerated dose (MTD) or less. Anti-cancer drug can be administered in low doses over prolonged periods without extended rest periods which is called as low-dose metronomic therapy (LDM). In addition, continuous infusion therapy is applicable within clinical environment, not yet as a portable device. The major disadvantage of these methods is the empiricism associated with determining the optimal biologic dose (OBD). In order to solve the problem, we have designed discrete-time controllers which realize automated optimal treatments.

Keywords — cancer therapy, protocol, discrete-time controller, endostatin, bolus doses, maximum tolerated dose, low-dose metronomic therapy, state feedback, setpoint control, actual state observer, load estimation

I. INTRODUCTION

Newest research studies on cancer treatments show the importance of specific cancer therapies. The group of Targeted Molecular Therapies (TMTs) [1, 2] contains several different therapeutic methods; however what they have in common is the aim to fight directly against specific, identified cancer mechanisms. Antiangiogenic therapy [3] is a type of TMT, which acts by inhibiting tumor vascularization. Ceasing the process of angiogenesis (new blood vessel formation), tumor growth is limited.

There are several types of antiangiogenic drugs (also known as angiogenic inhibitors) like bevacizumab [4], angiostatin [5] and endostatin [6]. Delivery of an antiangiogenic drug is not a trivial problem since the biological effectiveness of the treatment highly depends on the applied dosage. Using an empirical method to achieve the biological effective dosage, it is not guaranteed that the optimal therapy will be found; however, using closed-loop control, optimal solution can be realized [7, 8].

In this paper, we discuss the possible delivery methods in cancer therapies which use endostatin. Endostatin is able to target neovascular endothelial cells (ECs) and has the potential for antiangiogenic and antitumor activities [9]. However, it has to be taken into account that endostatin has a short half-time [10].

The paper is organized as follows. In Section II, we present the nonlinear model of tumor growth under angiogenic inhibition. Section III discusses first the cancer protocols in the light of the dosage problem, and then it presents the simulation results of the protocol based cancer therapies. In Section IV, first the design aspects of the discrete time controller with state feedback, setpoint control, actual state observer and load estimation are summarized, and then the simulation results of the discrete-time controller based treatments are evaluated. The paper ends with the results and discussion in Section V.

II. THE APPLIED MODEL OF TUMOR GROWTH

P. Hahnfeldt et al. created a dynamic model for tumor growth under antiangiogenic therapy [11]. In a simplified version of this model, continuous infusion therapy is taken into account [12], where the input (the inhibitor administration rate) is equal to the concentration of administered inhibitor (serum level of inhibitor) and the system is described by the equations:

\[
\begin{align*}
\dot{x}_1 &= -\lambda_1 \ln \left( \frac{x_1}{x_2} \right) \\
\dot{x}_2 &= b n_1 - d x_1^{1/3} - x_2 - c x_1 g \\
y &= x_1
\end{align*}
\]

where \(x_1\) is the tumor volume (\(\text{mm}^3\)), \(x_2\) is the endothelial/vascular volume (\(\text{mm}^3\)) and \(g\) is the concentration of the administered inhibitor (\(\text{mg} / \text{kg}\)). The model contains the following parameters: \(\lambda_1\) is the tumor growth rate (1/day), \(b\) is the stimulatory capacity of the tumor to the vasculature (1/day), \(d\) is the endogenous inhibition of previously generated vasculature (1/(day \(\text{mm}^2\))), \(c\) is the antiangiogenic effect of the administered inhibitor on the tumor vasculature (kg/(day mg)).

Parameter values for the considered Lewis lung carcinoma and the mice used in the experiment are [11]: \(\lambda_1 = 0.192\) 1/day, \(b = 5.85\) 1/day, \(d = 0.00873\) 1/day \(\text{mm}^2\). The experiment has shown that the most effective inhibitor was endostatin; therefore, we have applied this...
antiangiogenic drug in controller design (the value of parameter $e$ for endostatin is $e_{\text{endostatin}} = 0.66$ kg/(day·mg)).

III. PROTOCOL BASED CANCER THERAPIES

A. Cancer protocols in the light of the dosage problem

Methods of drug administration fall into four categories: a) bolus doses (BD), b) bolus doses with maximum tolerated dose (BD MTD), c) low-dose metronomic (LDM) regimen, and d) continuous infusion therapy. In this subsection, we draw a distinction between these treatments; in addition, we lay emphasis on the possible delivery doses in the case of endostatin treatment.

Using intermittent bolus doses administration, the patient receives drug on given days and the therapy has rest periods between the injections. The injected amount of bolus can be the maximum tolerated dose (MTD) or lower dose. The length of the rest periods depends on the amount of boluses (e.g. after MTD a longer rest period is required). The disadvantage of this method is that it involves regrowth of tumor cells, and in several cases the growth of selected clones will be resistant to the therapy.

To avoid the adverse events of bolus doses, anti-cancer drug can be administered in low doses over prolonged periods without extended rest periods which is called as low-dose metronomic therapy [14]. Advantages of LDM are its antitumor efficacy and reduced acute toxicities; however the major disadvantage is the empiricism associated with determining the optimal biologic dose (OBID) [15]. This is the most important problem oncologists are faced with when they are trying to translate LDM into the clinical application; however, according to our previous research, this can be solved by a closed-loop control [16].

Low-dose daily administration of antiangiogenic drugs was found to be more effective than high-doses with rest periods. In [16], the effect of low-dose bevacizumab treatment on mice and human adenocarcinoma was examined. Article [17] makes a case for low-dose endostatin treatment on human lung cancer. In this experiment, 3 mg/kg endostatin was administered intravenously daily for 10 days. The results lend support to the view that endostatin normalizes the structure and function of tumor vasculature. The importance of tumor vasculature normalization lies on the further delivery of chemotherapeutic drugs. Low-dose antiangiogenic therapy creates the possibility of further efficient therapeutic agent use (if any) or assists the more effective direct antitumor effect of the angiogenic inhibitor [18].

Finally, continuous infusion therapy is applicable within clinical environment, but not yet as a portable device. However, prolonged delivery of antiangiogenic drugs may be carried out by mini-osmotic pumps or cell encapsulation systems [9, 19]. In the study [20], endostatin was microencapsulated into poly(lactic-co-glycolic acid) (PLGA) microspheres to treat Lewis lung cancer. They found that in vivo releasing endostatin was biologically active and significantly inhibited the migration of endothelial cells.

Several studies examined the antitumor effect of endostatin as a function of delivery (for instance in the case of pancreatic cancer [10, 21]). Continuous administration (using micro-osmotic pumps) was found to be more effective (97% inhibition of tumor growth) than daily bolus doses (66% inhibition of tumor growth), using the same dosage (20mg/kg/day).

To sum up, there is a lot of supporting evidence from the medical experiments showing that low-dose administration of antiangiogenic drugs is more effective than high-dose delivery. Continuous drug administration may have even better efficacy; however, long-term continuous therapy raises technical questions which are not solved yet. Therefore we draw attention to the discrete-time control as an alternative and promising solution for antiangiogenic drug delivery.

B. Simulation results of the protocol based cancer therapies

We simulated the effect of the different medical protocols on the tumor growth model described by (1)-(3). The therapies were designed to be comparable; therefore the total administered inhibitor concentration was 300 mg/kg in all cases. Treatment period was 15 days in every case.

In the case of bolus doses with maximum tolerated dose (BD MTD), 100 mg/kg bolus was administered once a day in the 1st, 6th and 12th days of the treatment (3 times). The length of the drug infusion was chosen to be one hour. The rest periods were 5 days. When bolus doses (BD) were used in lower dosage, 20 mg/kg bolus was delivered once a day every day of the treatment (15 times). The length of the drug infusion was chosen to be one hour, similarly to the BD MTD therapy. Consequently, the rest periods were 23 hours.

Using low-dose metronomic regimen (LDM), 2.5 mg/kg infusion was delivered for one day in the 1st, 4th, 7th, 10th and 13th days of the treatment (5 times). The rest periods were 2 days.

In the case of continuous infusion therapy, 0.8335 mg/kg/h continuous infusion was used during the whole treatment, without rest periods.

Fig. 1 shows the results of the simulations. The less effective treatment was BD MTD, since this therapy reduced the tumor volume in the least amount (steady state tumor volume is 16330 mm³). This is consistent with the above mentioned clinical experimental results. In addition, maximum tolerated doses are not just therapeutically ineffective, but may cause serious adverse events for the patient, and therefore erode the quality of life.

The effectiveness of BD and LDM therapies was similar. Using daily bolus doses, the steady state tumor volume is 15580 mm³, while low-dose metronomic therapy resulted in 15660 mm³ steady state tumor volume. Despite the similar results relating to steady state tumor volume, the aspect of physiological load has to be taken into account as well. For a long-term treatment, low-dose metronomic regimen can be more tolerable, and as it can be seen from Fig. 1, due to the smaller drug dosage, vascular volume changes more slowly and to a lesser extent in LDM therapy in contrast to BD treatment.

The simulation results of continuous infusion therapy (marked as “cont” in Fig. 1) lend support to the clinical experimental results, since the lowest steady state tumor volume (15360 mm³) was achieved using this treatment. Other advantages of this method are the smooth change...
of vascular volume during the treatment on the one hand, and minimal or no side effects on the other hand. However, we would like to emphasize once more that continuous long-term therapy is not yet available nowadays.

IV. DISCRETE TIME CONTROLLER BASED TREATMENTS

A. Discrete time controller with state feedback, setpoint control, actual state observer and load estimation

Detailed description of the discrete-time controller design can be found in [7]. Here we give a concise summary of the design aspects of the discrete time controller with state feedback, setpoint control, actual state observer and load estimation.

Taking into account that state feedback control design requires linear model, we applied operating point linearization in the go = 0 working point. The matrices of the linear model with system matrix $A$, input matrix $B$ (i.e. the right-hand side of its differential equation is $\dot{x} = Ax + Bu$), and output defined as $y = Cx + Du$ are

$$A = \begin{bmatrix} -\lambda_1 \log \frac{x_1}{x_2} & -\lambda_2 \frac{x_2}{x_3} \\ -\lambda_3 \frac{x_3}{x_4} & -\lambda_4 \frac{x_4}{x_5} \\ h - \frac{d}{x_1} & 0 & 0 & 0 & 0 \\ 0 & 0 & a & b & c \\ 0 & 0 & 0 & d & 0 \end{bmatrix}$$

(4)

$$B = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

(5)

$$C = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

(6)

$$D = \begin{bmatrix} 0 \end{bmatrix}$$

(7)

The whole controller structure was designed for the linearized and discretized tumor growth model; however the simulations were carried out on the original nonlinear continuous model.

Sampling time was chosen to fulfill the conditions of Shannon theorem for every signal of the accelerated (closed-loop) system. The continuous-time linear model was transformed to a discretized model that has equivalent step response in the sampling times, thus the difference equation of the discrete-time model is
We investigated the observability and controllability of the linearized discrete model, and we found that the matrices are full rank for every nonzero operating point, thus the system is controllable and observable.

The feedback matrix $K$ was determined by the Ackermann’s formula, i.e.

$$K_{ij} = \psi^T M_i^{-1} (A_i B_j) \psi_{\text{closed}}(A_i),$$

where $\psi_i$ is the $i$th unit vector, and $\psi_{\text{closed}}(A_i)$ is the characteristic polynomial of the closed loop evaluated at the matrix $A_i$ and $M_i$ is the controllability matrix evaluated as

$$M_i(A_i, B_j) = \{B_j, A_i B_j , \ldots , A_i^{m-1} B_j \},$$

where $m$ denotes the order of the system.

The feedback matrix $K$ was also calculated for the discrete time LQ problem using the formula

$$K_{ij} = (R + B_j^T P B_j)^{-1} B_j^T P A_i,$$

where $P$ is the solution of the Discrete-time Algebraic Riccati Equation (DARE)

$$P = A_i^T P A_i - A_i^T P B_j (R + B_j^T P B_j)^{-1} B_j^T P A_i + Q$$

where $Q = C^T C$.

For setpoint control, two matrices ($N_i$ and $N_s$) are needed to extend the control structure (provided that the reference signal is piecewise continuous):

$$
\begin{pmatrix}
N_s \\
N_i
\end{pmatrix}
= 
\begin{bmatrix}
A_i - I & B_j \\
C & 0
\end{bmatrix}
\begin{bmatrix}
0_{nxm} \\
I_n
\end{bmatrix}$$

Actual state observer was designed to estimate the non-measurable state variables. It is described by the difference equation

$$\dot{\hat{x}}_i = F \tilde{x}_{i-1} + G \hat{y}_i + H u_{i-1},$$

where

$$F = A_i - G C A_i,$$

$$H = B_i - G C B_i,$$

$$G = \phi(A_i) = \text{rref}(A_i - C^T P^{-1} C A_i F'),$$

where $\phi(A_i)$ refers to the characteristic polynomial of the matrix $F$ evaluated at the matrix $A_i$.

We also designed load estimation; we assumed that the disturbance is reduced to the input of the system (load change) and it is piecewise constant, so the discrete-time model was extended by the load modeled as a constant state-variable that adds up to the input of the original model.

The state feedback and the setpoint control was designed for the original system; however, the actual state observer was designed for the extended system, whose difference equation is

$$\begin{pmatrix}
\dot{\hat{x}}_i \\
\hat{y}_i \\
\dot{\hat{w}}_i
\end{pmatrix}
= 
\begin{bmatrix}
F \hat{x}_{i-1} + G \hat{y}_i + H u_{i-1} \\
0_n \\
0_n
\end{bmatrix}$$

Fig. 2 shows the whole closed-loop control system containing the controller and the nonlinear system. We placed saturation between the tumor model and the controller; in addition, control input has a lower and an upper limit due to physiological considerations.

### Simulation results of the discrete-time controller based treatments

Discrete controller based therapies are automatic treatments which can contain bolus doses and metronomic periods as inputs. The whole treatment periods are the same as in protocol based cancer therapies, i.e. 15 days. Each discrete controller has the following parameters (which were chosen according to [7]). The operating point, where the original nonlinear system was linearized, is 10 mm$^3$. Controllers use LQ optimal control as a state feedback method. The value of $R$ weighting matrix is 1.

The reference signal is 13000 mm$^3$ to get steady state tumor volume results close to the protocol based cancer therapies’ values. The disturbance was chosen to be 0%, since protocol based cancer therapies do not have disturbance either in the simulations. The controllers differ only in the chosen saturation level.

Fig. 3 shows the results of the simulations. Using the maximum tolerated dose as the saturation level (100 mg/kg, note that this is the same value as it was at the protocol based therapies’ BD MTD case), there are more than one rest periods, and these periods are not located at equal intervals. The therapy begins with a maximum bolus dose, and after that, a half day rest period follows. The next phase takes 3 days, during this period, maximum bolus doses follow each other in about 5-10 hours. After that an approximately 6.5-day rest period follows. This
V. RESULTS AND DISCUSSION

Comparison of the therapies as a function of total inhibitor concentration and steady state tumor volume can be seen in Fig. 4.

Since the protocol based therapies were designed to be comparable (the total administered inhibitor concentration was 300 mg/kg in all cases), the efficacy order can be easily set up. Bolus doses therapy with maximum tolerated dose (BD MTD) is the less effective in terms of tumor volume reduction. Bolus doses therapy with lower dose (BD) and low-dose metronomic regimen (LDM) has similar results, and continuous infusion therapy reduces the tumor volume in the greatest extent.

However, it is trivial from Fig. 4, that even the best protocol based therapy cannot approach the effectiveness of discrete controller based therapies, since these
automated treatments achieve considerably lower steady state tumor volumes while using less than half total inhibitor concentration. The choice between the automated treatments depends on the current therapeutic goal. If the goal is to reduce the tumor volume as fast as possible, and the patient tolerates MTD boluses, the 100 mg/kg saturation is the most appropriate way. The 20 mg/kg saturation level is a trade-off choice: the physiological load of the patient is less; however, the gained steady state tumor volume is higher compared to the BD MTD therapy. Taking into account the above mentioned vasculature normalization aspect and the minimal side effects, 2.5 mg/kg saturation seems to be the best therapeutic choice in most cases.

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