

Electrostatically confined monolayer graphene quantum dots with orbital and valley splittings

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Abstract

The electrostatic confinement of massless charge carriers is hampered by Klein tunneling. Circumventing this problem in graphene mainly relies on carving out nanostructures or applying electric displacement fields to open a band gap in bilayer graphene. So far, these approaches suffer from edge disorder or insufficiently controlled localization of electrons. Here we realize an alternative strategy in monolayer graphene, by combining a homogeneous magnetic field and electrostatic confinement. Using the tip of a scanning tunneling microscope, we induce a confining potential in the Landau gaps of bulk graphene without the need for physical edges. Gating the localized states towards the Fermi energy leads to regular charging sequences with more than 40 Coulomb peaks exhibiting typical addition energies of 7-20 meV. Orbital splittings of 4-10 meV and a valley splitting of about 3 meV for the first orbital state can be deduced. These experimental observations are quantitatively reproduced by tight binding calculations, which include the interactions of the graphene with the aligned hexagonal boron nitride substrate. The demonstrated confinement approach appears suitable to create quantum dots with well-defined wave function properties beyond the reach of traditional techniques.

The charge carriers in graphene at low energies, described as massless Dirac quasiparticles¹, are expected to feature long spin coherence times²⁻⁵. Exploiting this property requires precise manipulation of individual Dirac electrons. Quantum dots (QDs) present an essential building block, yet providing tailored confinement in graphene has remained challenging. So far, e-beam lithography⁶ and various other techniques⁷⁻¹² have been used to design nanometer sized devices. However, their performance lacks behind, for example, GaAs QDs^{13,14}, as disordered sample edges of patterned graphene result in uncontrolled charge localization and scattering^{6,15-17}. So far, no clear evidence for fourfold degenerate charging sequences has been reported in transport

measurements of tunable QDs. Moreover, failing to controllably lift graphene's valley degeneracy renders spin qubits unfeasible^{2,18,19}.

Bilayer graphene could, in principle, improve the situation, since an electric displacement field opens a band gap at regular AB stacking²⁰. Indeed, electrostatically confined QDs in bilayer graphene exhibit Coulomb blockade²¹⁻²³, yet controlling the spin or valley degree of freedom of an individual state has also not been demonstrated. Moreover, confinement is still prone to parasitic conduction channels due to residual disorder in the band gap or conducting channels along domain walls of AB- and BA-stacked areas²⁴. Another approach exploits whispering gallery modes in electrostatically confined QDs²⁵⁻²⁷, but here the control of the wave functions by gates is difficult and dwell times are extremely short (< 100 fs). On an even more intricate route, the tip of a scanning tunneling microscope (STM) is used to locally stretch a suspended monolayer graphene sheet²⁸. The onset of charge quantization due to induced strain showcases confinement by pseudomagnetic fields. Adding a real magnetic field B leads to charging sequences with regular orbital but no valley splittings²⁸. Creating multiple QDs in this fashion would require independent strain control for every QD on the suspended graphene. Thus such an approach is barely scalable.

Landau quantization helps to overcome Klein tunneling by opening band gaps²¹⁻²³. An elegant method to exploit this by combining a magnetic field and an electrostatic potential has been proposed theoretically²⁹⁻³¹. Indeed, indications of such confinement have been found in metal contact induced pnp junctions³², graphene on SiO₂^{33,34} and a suspended graphene nano-ribbon³⁵. However, in these experiments the confinement potential was not tunable but was generated by electrostatic disorder.

Here, we demonstrate controlled confinement by a combination of magnetic and electrostatic fields. We use the tip-induced electrostatic potential of an STM^{36,37} in a B field perpendicular to the graphene plane (Fig. 1a). Scanning tunneling spectroscopy (STS) reveals sequences of charging peaks by means of Coulomb staircases which appear when these confined states cross the Fermi energy E_F . The peaks systematically group in quadruplets for electrons and holes corresponding to the fourfold (valley and spin) degeneracy in graphene (Fig. 1c,d). Moreover, some quadruplets separate into doublets due to an additional valley splitting induced by the hexagonal boron nitride (BN) substrate. STS as a function of B reveals that the first confined states emerge from Landau levels (LLs) with indices ± 1 . A third-nearest neighbor tight binding (TB) calculation^{38,39} reproduces the onset of charging events as function of tip voltage V_{tip} and B , and the magnitude of orbital and valley splittings.

We now sketch the principle of our experiment. A homogeneous, perpendicular B field condenses the electronic states of graphene into LLs at energies

$$E_N = \text{sgn}(N) \sqrt{2\hbar e \nu_F^2 |BN|}, \quad (1)$$

where ν_F is the Fermi velocity and $N \in \mathbb{Z}$ is the LL index¹. Consequently, energy gaps between the LLs emerge in the electronic spectrum. The smooth electrostatic potential $\Phi_{\text{gr}}^{\text{el}}$ (magenta line in Fig. 1a) induced by the STM tip locally shifts the eigenenergies $\varepsilon_i(\Phi_{\text{gr}}^{\text{el}})$ of charge carriers relative to the bulk LL energy (eq 1). Shifting ε_i into the Landau gaps creates confined states (Fig. 1b)³⁰. The shape of $\Phi_{\text{gr}}^{\text{el}}$ determines the single-particle orbitals and energy levels, as in the case of artificial atoms¹⁴. Orbital splittings Δ_j^{o} separate the energy levels (Fig. 1c), which we deduce experimentally to be $\Delta_j^{\text{o}} = 4 - 10$ meV (see below) and, thus, Δ_j^{o} is small compared

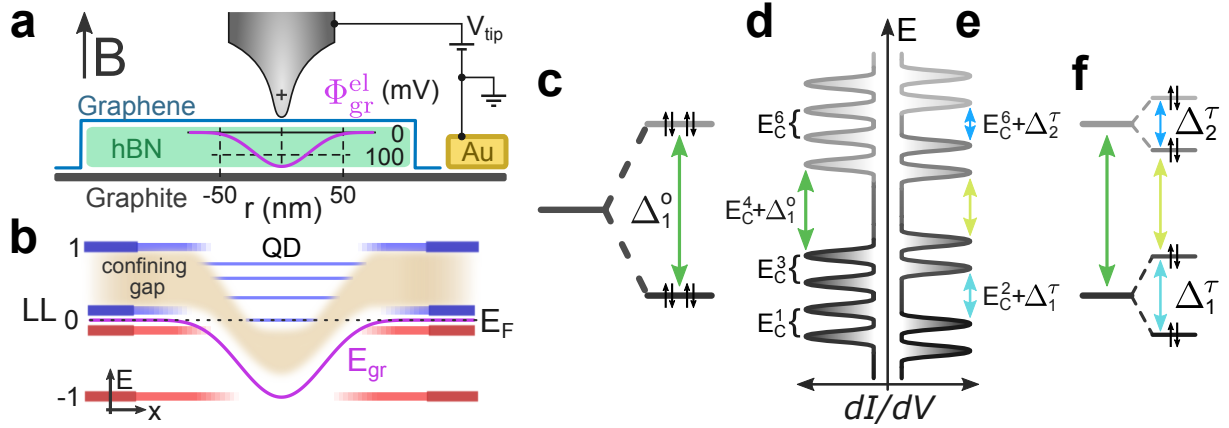


Figure 1: **(a)** Sketch of the experiment. Graphene covers a 30 nm thick hexagonal boron nitride flake on graphite. The magenta line represents the tip-induced confinement potential of graphene $\Phi_{\text{gr}}^{\text{el}}$ for electrons, calculated as the numerical solution of Poisson's equation (Supplement). **(b)** Energy diagram in real space: Fermi energy E_F , black dashed line; local band bending E_{gr} , magenta line; states belonging to electron (hole) LLs, blue (red); bulk LLs, 1, 0, -1. States embedded in the LL_0 - LL_{+1} gap (thin blue lines) are electrostatically confined. **(c)** Energy level diagram for the first two orbital states of a graphene QD exhibiting an orbital splitting Δ_1^o . Both orbitals are fourfold degenerate, as indicated by black arrows representing physical spin. **(d,e)** Charging peak sequence in the differential conductance dI/dV corresponding to the level diagrams in **c** and **f**, respectively. Charging peaks are separated by the addition energy $E_{\text{add}}^i = E_C^i + \Delta_i$, where $E_C^i \approx E_C$ is the charging energy and Δ_i is comprised of Δ_j^o and/or the valley splittings Δ_k^τ . In **d** quadruplet ordering showcases a dominant Δ_1^o , while Δ_k^τ become sizable in **e**, further separating quadruplets into doublets. **(f)** Same as **c**, but including additional Δ_k^τ . The spin splitting Δ^σ is neglected, as $\Delta^\sigma < \Delta_k^\tau, \Delta_j^o, E_C$ in experiment.

to the first LL gap $E_1 - E_0 \approx 100$ meV at 7 T. While pristine graphene exhibits a fourfold degeneracy, varying stacking orders of graphene on top of BN induce an additional valley splitting Δ_k^τ , which turns out to be smaller than Δ_j^o in our experiment. The finite B field creates a small Zeeman splitting estimated as $\Delta^\sigma = g\mu_B B \approx 800$ μ eV at 7 T (g -factor of 2, μ_B : Bohr's magneton). Accordingly, the orbital splittings separate quadruplets of near-degenerate QD states, which exhibit a subtle spin-valley substructure (Fig. 1f).

We use the STM tip not only as source of the electrostatic potential and thus as gate for the QD states but also to sequence the energy level spectrum of the QD as the states cross E_F , that is, as the charge on the QD changes by $\pm e$. This leads to a step in the tunneling current $I(V_{\text{tip}})$ and a corresponding charging peak in the differential conductance dI/dV_{tip} . In addition to the single particle energy spacings, every additional electron on the dot needs to overcome the electrostatic repulsion to the electrons already inside the QD⁴⁰, given by the charging energy E_C^i . Thus, we probe the total energetic separation of charge states i and $i + 1$, given by the addition energy $E_{\text{add}}^i = E_C^i + \Delta_i$, where Δ_i consists of Δ_j^o , Δ_k^τ and/or Δ^σ . As we experimentally find $E_C^i \approx E_C \approx 10$ meV $\gtrsim \Delta_j^o$ (nearly independent of the charge state i , see below), the quadruplet near-degeneracy of the QD states translates to quadruplet ordering of the charging peaks (Fig. 1d). Whenever either Δ_k^τ or Δ^σ significantly exceeds the other and temperature, quadruplets separate into doublets (Fig. 1e).

We prepare our sample (see Fig. 1a and Supplement) by dry-transferring^{41,42} a graphene flake onto BN⁴³⁻⁴⁵. During this step we align both crystal lattices with a precision better than one degree (Supplement). Then we place this graphene/BN stack on a large graphite flake to avoid insulating areas and simplify navigating the STM tip. Any disorder potential present in the sample will limit the confinement as long as it is larger than the Landau level gaps, thus larger gaps (e.g., the $LL_0 - LL_{\pm 1}$ gap) result in improved confinement. Moreover, the induced band bending will only be well-defined if the disorder potential is smaller than the maximum of $\Phi_{\text{gr}}^{\text{el}}$. By using the dry-transfer technique^{41,42} and a graphite/BN substrate we reduce disorder in the graphene significantly⁴⁶⁻⁴⁸.

Probing the sample in our custom-build UHV-STM system⁴⁹ at $T = 8$ K, we observe the superstructure with $a = 13.8$ nm periodicity, which develops due to the small lattice mismatch of 1.8% between graphene and BN⁴⁷. An atomically resolved STM image of this superstructure is presented in Figure 2d. Prior to measuring dI/dV spectra, the tip-sample distance is adjusted at the stabilization voltage V_{stab} and current I_{stab} and then the feedback loop is turned off (Supplement). Figure 2a shows exemplary dI/dV spectra, acquired at $B = 7$ T and adjusted to same vertical scale by dividing dI/dV by the first value I_0 of the respective $I(V)$ curve (Supplement). We observe pronounced, regularly spaced peaks for $V_{\text{tip}} < -170$ mV and $V_{\text{tip}} > 500$ mV. A closer look at the sequences reveals the expected grouping in quadruplets, which can still be distinguished up to the 20th peak. This grouping becomes even more evident by directly comparing the voltage difference between adjacent peaks ΔV in Figure 2b,c: ΔV between quadruplets is up to twice as large as ΔV within the quadruplets indicating $\Delta_j^o \lesssim E_C^i$ while Δ_k^τ and Δ^σ are significantly smaller. To further elucidate grouping patterns, we measure 6400 dI/dV spectra at equidistant positions within a 60 nm \times 60 nm area, thus probing all areas of the superstructure. The median ΔV values (orange circles in Fig. 2b,c) portray the robust ordering into quadruplets on the hole side, implying Δ_j^o generally dominates over Δ_k^τ and Δ^σ . On the electron side of the spectra the sequences are disturbed by a few additional charging peaks of defect states in the BN substrate⁵⁰

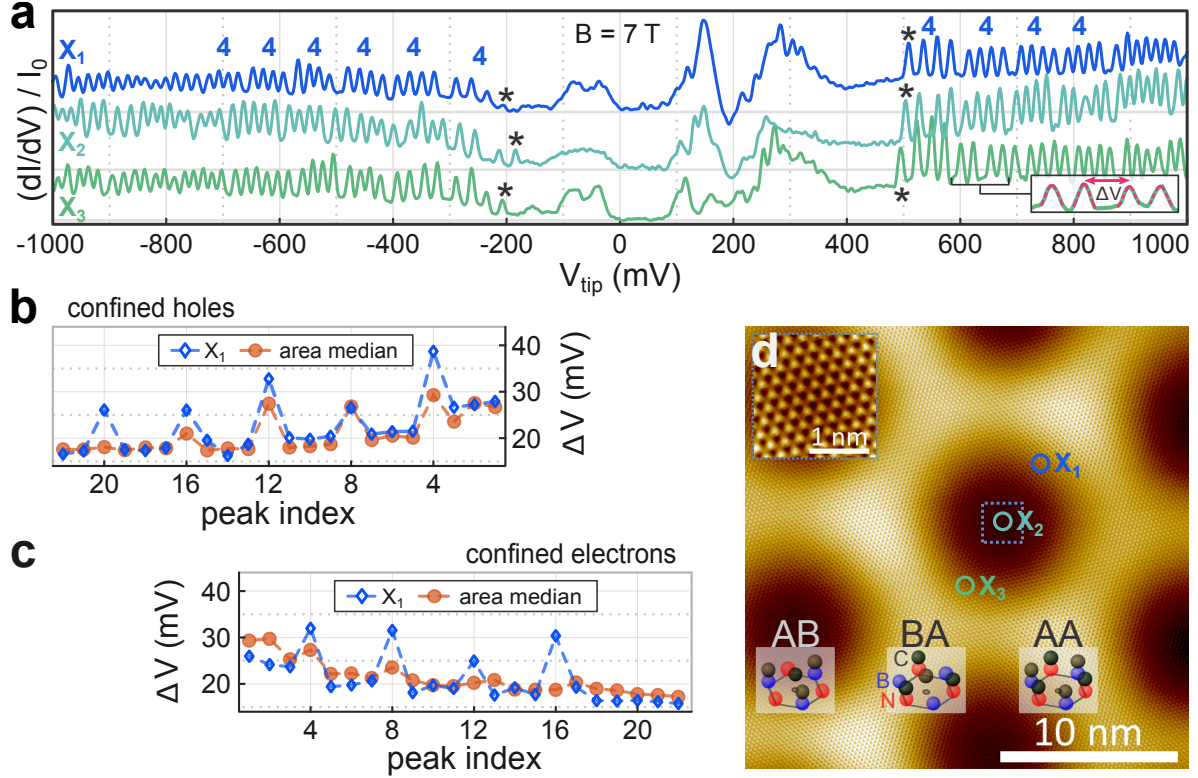


Figure 2: (a) Representative differential conductance spectra $dI/dV(V_{\text{tip}})$, normalized by the first value I_0 of the respective $I(V_{\text{tip}})$ curve (Supplement). Recording positions are: X_1 , between AA and AB; X_2 , on AB; X_3 , between AB and BA (compare d). Spectra on other regions (e.g., AA, BA) look similar. $V_{\text{stab}} = 1$ V, $I_{\text{stab}} = 700$ pA, $V_{\text{mod}} = 4.2$ mV_{rms} and $B = 7$ T. Quadruplets of peaks are marked by “4” and the first charging peak on either V_{tip} side by an asterisk. Curves are offset for clarity, while horizontal gray lines mark $dI/dV = 0$ S. Inset shows a zoom with Gaussian fits (dashed lines) used to extract distances between adjacent peaks ΔV as marked. (b,c) ΔV as function of consecutive peak index, for spectrum X_1 (blue, error bars smaller than symbol size) and the median values for 80×80 spectra recorded on 60×60 nm² (orange). (d) Atomically resolved STM image (raw data) of the aligned graphene on hexagonal boron nitride (BN). $V_{\text{tip}} = 400$ mV, $I = 1$ nA. Differently stacked areas AB, BA and AA marked and sketched by ball models. Inset on the upper left shows a zoom into the AB stacked area, marked by the blue square, exhibiting an obvious sublattice symmetry breaking due to the underlying BN. Positions equivalent to those where spectra in a were recorded are marked by circles labeled X_1, X_2, X_3 .

which are identified by their characteristic spatial development (Supplement). This limits the comparability of the electron and hole sector and hides possible smaller electron-hole asymmetries in the data. The dI/dV features in between the charging peaks most likely capture contributions from multiple orbital states of each LL, which are lifted in degeneracy by the tip-induced potential, but cannot be identified unambiguously (Supplement, Sec. 5).

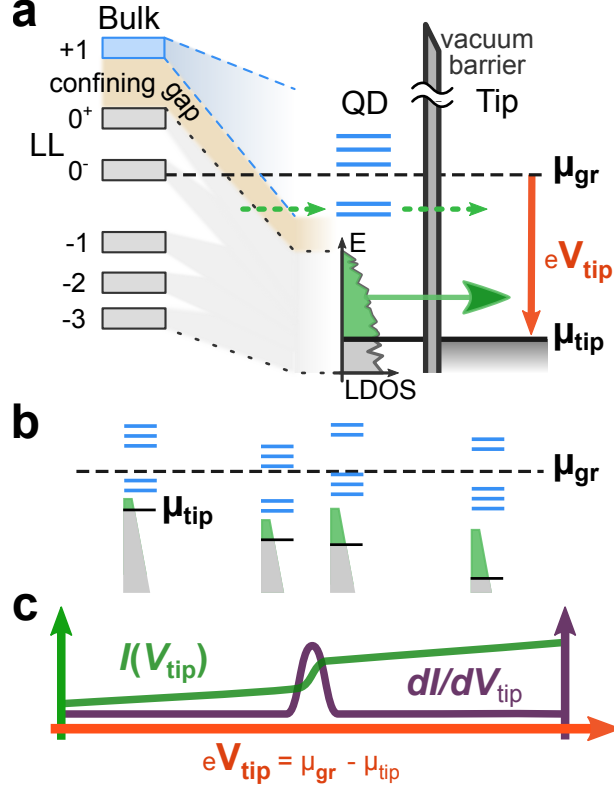


Figure 3: Sketch of the Coulomb staircase. **(a)** The chemical potentials of graphene μ_{gr} (black dashed line) and tip μ_{tip} (black solid line) define the bias window eV_{tip} , within which graphene states tunnel into empty tip states. There are two current paths available: (i) a weak one (green dashed arrow) via quantum dot states (blue lines), (ii) a dominant one (solid green arrow) via states strongly coupled to the graphene bulk (marked LDOS). Left: bulk graphene LLs away from the tip-induced band bending. **(b)** Schematic diagram of change in QD energies (blue lines) and quasi-continuous LDOS underneath the tip (green and gray triangle) for increasing V_{tip} from left to right. Between the second and third frame, the QD changes its charge state shifting the energy of the QD states and the entire LDOS upwards. **(c)** Tunneling current I displaying the staircase (green line) and differential conductance dI/dV (purple line) for increasing V_{tip} (aligned with **b**).

To understand the origin of the charging peaks, we provide a detailed microscopic picture of the tip-induced gating of localized states. We will only discuss the case of positive V_{tip} , that is, electron confinement, since the arguments for negative V_{tip} are analogous. Increasing V_{tip} (orange arrow in Fig. 3) shifts the states underneath the tip energetically down. States originating from LLs with positive index are embedded in the $\text{LL}_0\text{-LL}_{+1}$ gap which provides electrostatic confine-

ment (Fig. 3a, see also Fig. 1b). Within the bias window $eV_{\text{tip}} = \mu_{\text{gr}} - \mu_{\text{tip}}$, electrons tunnel from the sample into unoccupied states of the tip. One current path (dashed green arrow Fig. 3a) passes through states of the QD (blue lines). The other stronger current path (solid green arrow Fig. 3a) originates from the quasi-continuous LDOS at lower energies where energetically overlapping LL states strongly couple to the graphene bulk. Though increasing V_{tip} gates QD states down (Fig. 3b), the Coulomb gap around E_{F} always separates the highest occupied from the lowest unoccupied state, prohibiting continuous charging of confined states. It is only when the next unoccupied level crosses μ_{gr} that the QD is charged by an additional electron. The electrostatic repulsion due to its charge abruptly increases the Hartree energy of all states, thereby shifting additional graphene states from below μ_{tip} into the bias window (Fig. 3b, central transition). Consequently, the tunneling current I increases which translates to a charging peak in dI/dV_{tip} (Fig. 3c). This mechanism is called Coulomb staircase⁴⁰ and has been observed previously, for instance, for charging of clusters within an STM experiment⁵¹. In essence, charging peaks in dI/dV signal the coincidence of a charge level of the QD with μ_{gr} ⁵² and thus provide a clear signature of the addition energy spectrum of the QD.

Since the measurement captures the QD level spacings as charging peak distances ΔV , they need to be converted to E_{add} via the tip lever arm α_{tip} . The latter relates a change of V_{tip} to its induced shift of the QD state energies. The lever arm is determined by the ratio of the capacitance between tip and dot C_{tip} , and the total capacitance of the dot C_{Σ} , thus $\alpha_{\text{tip}} = C_{\text{tip}}/C_{\Sigma}$. C_{Σ} includes C_{tip} , the capacitance between dot and back-gate, and dot and surrounding graphene. We use a Poisson solver to estimate $C_{\Sigma} = 16.5 \pm 3.2$ aF and $C_{\text{tip}} = 8 \pm 1.5$ aF for our QD (Supplement). Hence, we find $E_{\text{C}} = e^2/C_{\Sigma} \approx 10 \pm 2$ meV and $\alpha_{\text{tip}} = 0.51 \pm 0.03$ (close to values reported for a similar system by Jung et al.³³). Consequently charging peaks dominantly separated by E_{C} , that is, $E_{\text{add}}^i \approx E_{\text{C}}^i$ because $\Delta_i \ll E_{\text{C}}^i$, should exhibit $\Delta V = E_{\text{C}}/(e \cdot \alpha_{\text{tip}}) \approx 20$ mV, in close agreement with the values found within quadruplets at higher occupation numbers (Fig. 2b,c). As expected, we also find significantly larger E_{add}^i for every fourth charging peak. In case of clear quadruplet ordering, the orbital splittings for our QD are deduced from $\Delta_j^{\circ} = E_{\text{add}}^{4j} - E_{\text{C}}^{4j} \approx E_{\text{add}}^{4j} - E_{\text{add}}^{4j+1}$ and we find typical values of 4 – 10 meV for the first few orbitals ($\alpha_{\text{tip}} = 0.51$, Fig. 2b,c). For this estimate we neglect the additional Zeeman splitting or an even smaller valley splitting.

We next provide a theoretical framework to elucidate the details of the QD level spectrum. The eigenstates of bulk graphene LLs (eq 1) feature different wave function amplitudes on sublattices¹ A and B,

$$\Psi_N^K = \begin{pmatrix} \Psi_{|N|-1}^A \\ \Psi_{|N|}^B \end{pmatrix} \quad \text{and} \quad \Psi_N^{K'} = \begin{pmatrix} \Psi_{|N|}^A \\ \Psi_{|N|-1}^B \end{pmatrix}, \quad (2)$$

where K and K' denote the two inequivalent K-points of the Brillouin zone associated with the two valleys. For $N \neq 0$ the LL index differs by one for the two sublattices, while for $N = 0$ the part of the wave function with subscript $|N| - 1$ vanishes, resulting in polarized sublattices for each valley. The wave functions of bulk graphene (eq 2) are modified by the tip-induced potential. Assuming a radially symmetric confinement potential, the eigenstates are described by radial and angular momentum quantum numbers (n_r, m) , with $n_r \in \mathbb{N}_0$ and $m \in \mathbb{Z}$. Adiabatically mapping a given LL with index N on to possible combinations of n_r and m yields^{53,54}

$$|N| = n_r + 1/2 \cdot (m + |m|), \quad (3)$$

with $0 \leq n_r \leq |N|$ and $m \leq |N|$.

We calculate eigenstates of a $120 \text{ nm} \times 100 \text{ nm}$ commensurate graphene flake on BN using third-nearest neighbor TB³⁸, where the substrate interaction enters via a periodic superstructure potential and local strain effects³⁹, parametrized from DFT calculations^{55,56}. We approximate the amplitude Φ_0^{el} and shape of $\Phi_{\text{gr}}^{\text{el}}$ by a classic electrostatic solution of Poisson's equation (Fig. 1a, Supplement) with the tip radius r_{tip} as fit parameter. Comparing calculated charging energies to experiment yields a plausible value of $r_{\text{tip}} \approx 120 \text{ nm}$ implying a FWHM of the QD confinement potential of 55 nm at 7 T . We independently determine the initially free parameter E_F from the position of LL_0 in STS as $E_F = -40 \pm 5 \text{ meV}$ (Supplement). Accordingly, the graphene is p-doped. We note that varying E_F within the stated uncertainty range (see blue horizontal bar in Figure 4a) leads to no qualitative changes in the predictions of our model. We use open boundary conditions to simulate the coupling of the flake to the surrounding graphene. Consequently, eigenstates will feature complex eigenvalues $E_l = \varepsilon_l + i\Gamma_l/2$, where the real part ε_l represents the resonant energies and the imaginary part Γ_l the coupling to the delocalized bulk states⁵⁷. Thus we can readily distinguish states that are spread out over the flake (large Γ_l) from those localized near the tip (small Γ_l). We color code Γ_l in Figure 4a for a calculation with the tip-induced potential centered on an AB stacked area.

At $B = 7 \text{ T}$ and vanishing band bending ($\Phi_0^{\text{el}} = 0$), we find only delocalized states whose eigenenergies cluster around the bulk LL energies (eq 1, Fig. 4a). As we increase Φ_0^{el} , states begin to localize at the tip and shift in energy, with smaller Γ_l (darker curves) pointing to stronger localization (see Fig. 4a). Comparing hole states originating from LL_{-1} for negative and positive Φ_0^{el} , we find, as expected, stronger localization in case of negative Φ_0^{el} . The potential is always attractive to one kind of charge carriers which will localize underneath the tip. The other kind is repelled by the induced potential (see also Ref. 31) which results in stronger coupling to the bulk. In order to classify our TB wave functions in terms of the quantum numbers N , n_r and m , we consider sublattice A and B separately. Tracing the states back to their LL of origin reveals N , constraining possible $n_r \leq |N|$. The value of n_r is then determined by counting radial minima in the line cuts of the wave function amplitude for each sublattice (Fig. 4b-d). The distance of the first radial maximum from the center of the wave function is finally sufficient to assign the possible m quantum numbers of the LL (eq 3). Additionally, the (n_r, m) combinations need to be consistent with N differing by one on the two sublattices (eq 2). For instance, the line cuts in Figure 4b portray $(0, 0)$ and $(0, 1)$ on sublattice A and B, respectively. As expected, small angular momentum states are the first ones to localize with increasing Φ_0^{el} , in line with calculations by Giavaras et al.³⁰. Notice that the applied B naturally lifts the orbital degeneracy in QDs⁵⁸. Delocalized states remain at bulk LL energies (red horizontal lines in Fig. 4a).

We distinguish two regimes in the sequence of spin degenerate states crossing E_F for negative Φ_0^{el} . The first regime (Fig. 4e) exhibits $\Delta_k^{\tau} \lesssim \Delta_j^{\circ} \lesssim E_C^i$, while the second at higher Φ_0^{el} is characterized by densely spaced states, thus $\Delta_j^{\circ} \approx \Delta_k^{\tau} \ll E_C^i$. The sequence within the first regime corresponds to about five orbital pairs from valley K and K', in line with about five quadruplets in our experimental spectra (see labels "4" in Fig. 2a and ΔV sequences in Fig. 2b,c). The quite uniform spacing of peaks for larger V_{tip} (Fig. 2a) agrees with the second regime. In order to extract Δ_j° and Δ_k^{τ} within the first regime, we carefully assign the valley index to the states. Using the previously determined n_r and m in eq 3, the first state crossing E_F (Fig. 4b) features LL index $N_A = 0 + 1/2(0 + |0|) = 0$ on sublattice A and $N_B = 1 + 1/2(0 + |0|) = 1$

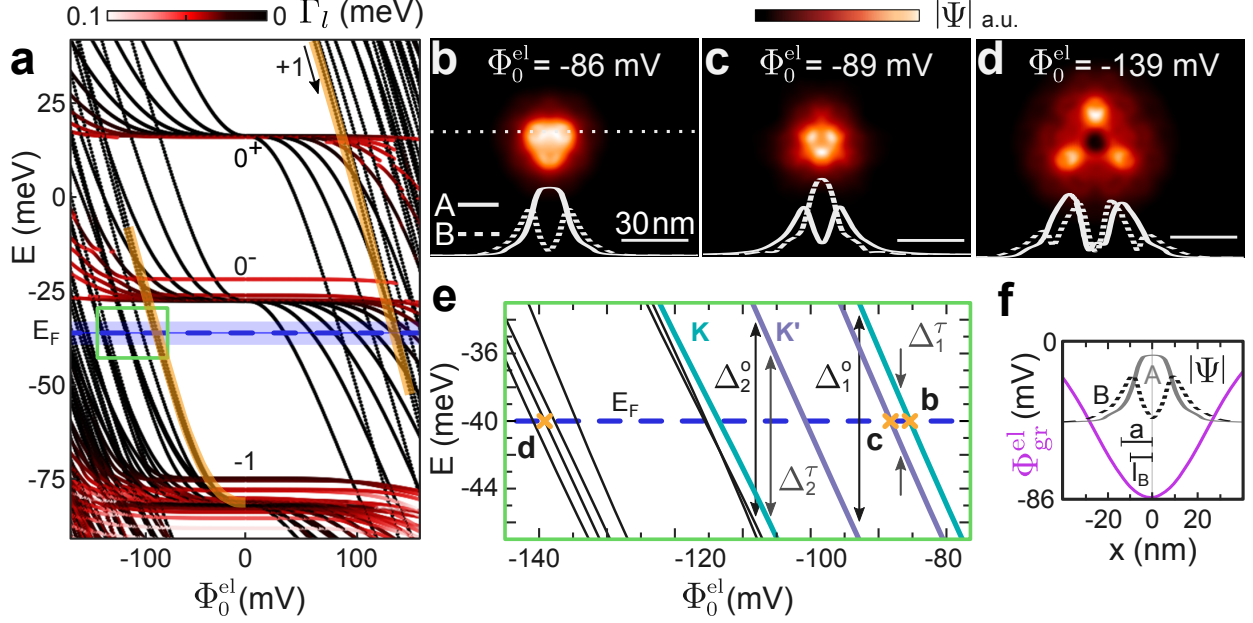


Figure 4: **(a)** Tight binding eigenenergies of a $120 \times 100 \text{ nm}^2$ graphene sample with open boundaries as function of tip-induced potential amplitude Φ_0^{el} at $B = 7 \text{ T}$ with the tip-induced potential centered on an AB area (BA and AA yield very similar behavior, not shown). Line color encodes coupling to the boundary (imaginary part Γ_l of eigenenergies): black (red) indicates strong (weak) localization underneath the tip. States from $\text{LL}_{\pm 1}$ and the split LL_0 are labeled by ± 1 and 0 , respectively. The LL_0 splitting reduces the confining gap to $E_{0^-} - E_{-1} \approx 50 \text{ meV}$. First states crossing E_F from $\text{LL}_{\pm 1}$ are highlighted in orange. Uncertainty in E_F indicated as blue horizontal bar (Supplement). The green rectangle marks the zoom shown in **e**. **(b-d)** Color plot of the wave function amplitude $|\Psi| = \sqrt{|\psi_A|^2 + |\psi_B|^2}$ of states marked by orange crosses in **e**. Φ_0^{el} at the crossing point $\varepsilon_l(\Phi_0^{\text{el}}) = E_F$ is marked. Solid (dashed) white lines are line cuts along the dotted white line in **b** for contributions from sublattice A (B), as marked. All scale bars identical. **(e)** Zoom into area marked by a green box in **a**. Colored lines identify valley K (cyan) and K' (purple). Orange crosses mark crossing of E_F (blue dashed line) of selected states, which are displayed in **b-d**. First two orbital Δ_j^o and valley Δ_k^τ splittings marked by arrows. **(f)** Comparison of length scales: tip-induced potential, magenta; calculated wave function amplitude $|\Psi|$ of first state crossing E_F (same as **b**) for sublattice A (gray line) and B (dashed line); superstructure lattice constant $a = 13.8 \text{ nm}$; magnetic length $l_B(7 \text{ T}) = 9.7 \text{ nm}$.

on sublattice B, as predicted by eq 2 for a $LL_{|1|}$ state in valley K. The role of the sublattices interchanges for the second state crossing E_F (Fig. 4c), placing it in valley K'. Consequently, states with $N_A = N_B - 1$ and $N_B = N_A - 1$ are assigned to valleys K and K', respectively. The calculation therefore predicts a valley splitting of about $\Delta_1^{\uparrow} = 3$ meV on the AB and BA areas (see Fig. 4b,c,e). Δ_2^{\uparrow} is comparatively large (about 12 meV) and the respective orbital splitting Δ_2° is only larger by 1 – 2 meV (see Fig. 4e). Consequently additional electrons may occupy the next orbital state of one valley prior to the same orbital state of the other valley at higher occupation numbers. Hence we limit further comparison to experiment to Δ_1^{\uparrow} . In our TB model, the strength of the valley splitting is dominated by the sublattice symmetry breaking term due to the BN substrate³⁹. The calculations also show that the radial extent of the wave functions grows for the first couple of states crossing E_F , as expected for increasing m (compare Fig. 4b,c to Fig. 4d), explaining the decrease of E_C^i towards higher peak indices at fixed B (see Fig. 2b,c).

Theory and experiment can be directly compared for the B dependence of the onset voltage of charging peaks V^* . Experimentally, V^* shifts towards higher $|V_{\text{tip}}|$ for increasing B (Fig. 5a), thus gating the first state to E_F requires stronger band bending for higher B . Since the curves for $B > 0$ T are offset proportional to \sqrt{B} , the straight line connecting the first charging peaks reveals that the energy distance of the first state to E_F scales with \sqrt{B} . This corresponds to the increase in bulk LL energies for $N \neq 0$ (eq 1), strongly suggesting those LLs as source of the confined states. This analysis is confirmed by our TB calculations, as the first crossing points of $LL_{\pm 1}$ states with the Fermi level Φ_0^* also shift towards higher $|\Phi_0^{\text{el}}|$ with increasing B (Fig. 5b). While the evolution of states with $\Phi_{\text{gr}}^{\text{el}}$ in Figure 4a is (approximately) symmetric with respect to $\Phi_{\text{gr}}^{\text{el}} \rightarrow -\Phi_{\text{gr}}^{\text{el}}$, the previously discussed p-doping induces an asymmetry in Φ_0^* for electrons and holes (see the lines highlighted in orange in Fig. 4a) and thus accounts for the observed asymmetry in V^* . In Figure 5c we compare V^* and Φ_0^* by using the $\Phi_0^{\text{el}}(V_{\text{tip}})$ dependence from the Poisson solver (see inset Fig. 5c, Supplement). Care must be taken to correctly account for the work function difference between the tip and the sample: the tip's work function (4.5 – 4.8 eV^{36,59}) exceeds that of graphene (4.5 eV), placing electric field neutrality in the positive V_{tip} sector. Moreover, it definitely has to lie in between the two charging peak regimes because the QD vanishes without band bending. Using a plausible work function difference of +50 meV in Figure 5c leads to satisfactory agreement between the theoretical predictions for the first state crossings and the experimental V^* .

Our TB simulations predict a strong reduction of Γ_l with increasing magnetic field, corresponding to the suppression of the radial tail of the wave function in Figure 5f and indicating the onset of localization between 1 and 3 T (Fig. 5b). The first appearance of charging peaks in the experiment at around 2 T (Fig. 5a) fits nicely. This finding is further corroborated by comparing the diameter of the LL state $d_n = 2\sqrt{2n+1} \cdot l_B$, being $d_1 = 89$ nm (63 nm) for LL_1 at 1 T (2 T), with the FWHM of the band bending region of 55 nm, providing an independent confirmation of the estimated $\Phi_{\text{gr}}^{\text{el}}$. At higher B , the diameter of the first QD state wave function is dominated by l_B rather than by the width of $\Phi_{\text{gr}}^{\text{el}}$ (Fig. 4f). The compression of the wave function for increasing B (Fig. 5f) also manifests itself as increase in addition energy, for instance, for $E_{\text{add}}^1 = E_C^1 + \Delta^{\sigma}$ in Figure 5d, where the increase in E_{add}^1 with B by about 4 meV cannot be explained by that of Δ^{σ} , being 460 μeV between 3 and 7 T. Consequently, increased Coulomb repulsion between electrons due to stronger compression and thus larger E_C^1 dominates $E_{\text{add}}^1(B)$. We observe a similar monotonic increase for the other E_{add}^i with odd index i , independent of the position of the QD.

Experiment and theory also provide detailed insight into the valley splitting Δ_k^{\uparrow} of the first

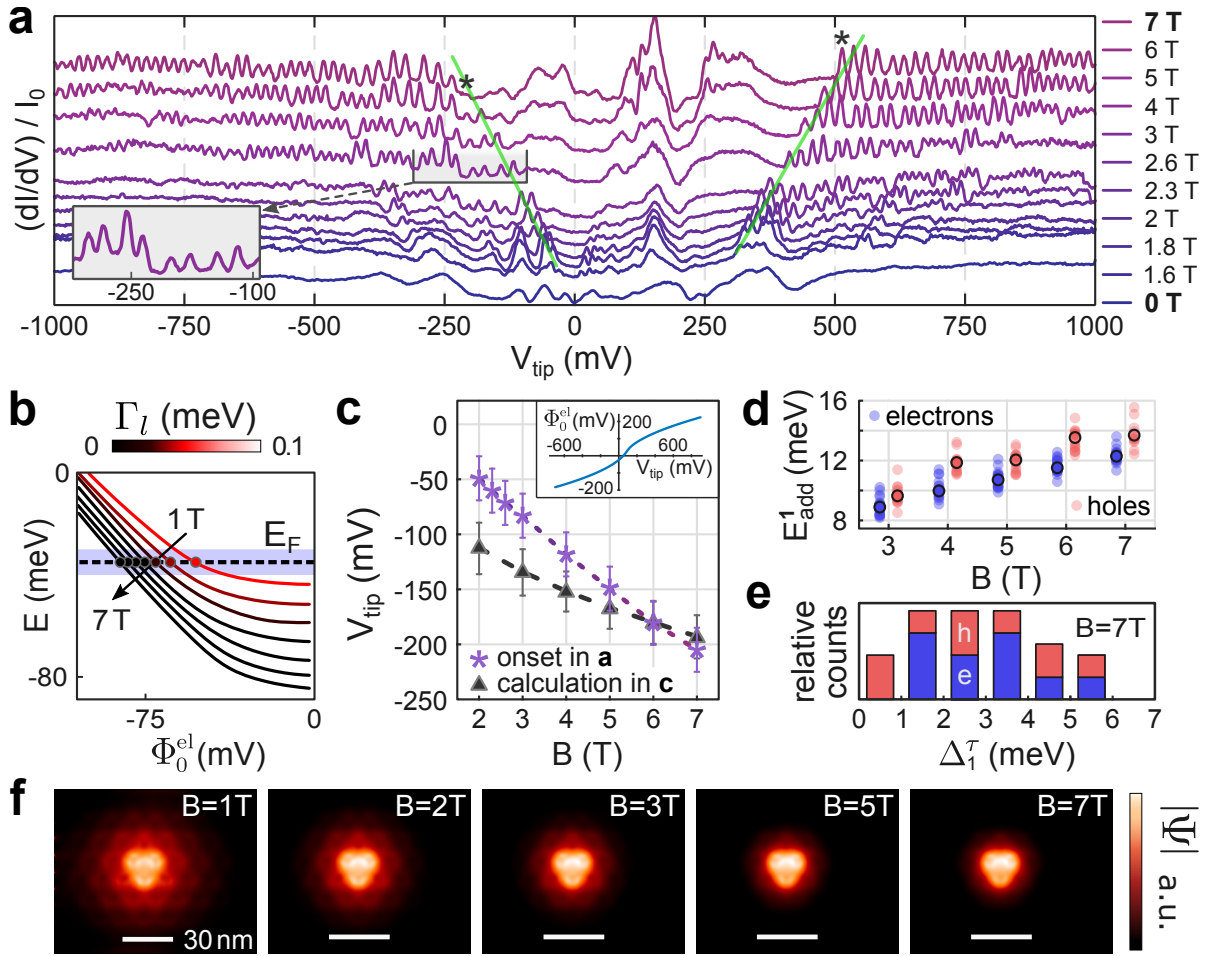


Figure 5: (a) dI/dV spectroscopy in the vicinity of an AA stacked area at varying B , marked on the right. Four spatially adjacent spectra are averaged and the ones for $B > 0$ T are offset by a value proportional to \sqrt{B} . $V_{\text{stab}} = 1000$ mV, $I_{\text{stab}} = 700$ pA, $V_{\text{mod}} = 4.2$ mV_{rms}. Green lines are guides to the eye, marking the onset voltage of charging peaks V^* . At 7 T an asterisk marks the first charging peak on either side. Inset shows zoom onto marked peaks. (b) Energy of first confined hole state as function of induced potential amplitude Φ_0^{el} for different B as marked. At larger B , states cross E_F at larger Φ_0^{el} , shifting V^* to larger negative V_{tip} . Color codes imaginary part of the eigenenergy as in Fig. 4a. (c) Comparison between measured and calculated V^* . Inset shows the required $\Phi_0^{\text{el}}(V_{\text{tip}})$ for conversion, taken from a Poisson-solver (Supplement) and including a reasonable work function difference of $\Delta\Phi = 50$ meV between graphene and tip. Error bars for measured V^* reflect typical variation of V^* on AA areas across a few superstructure unit cells. Error bars for calculation arise from the uncertainty in E_F . (d) Plot of the B dependance of $E_{\text{add}}^1 \approx E_C^1$ of 20 spectra (semitransparent dots) in the vicinity of an AA area. Data points are recorded at integer valued B fields (in Tesla), but displayed slightly shifted to the left (electrons, blue) and to the right (holes, red) for clarity. Median values are encircled in black. (e) Histogram of $\Delta_1^\tau \approx E_{\text{add}}^2 - E_{\text{add}}^3$ (experimental error below 0.2 meV) at $B = 7$ T for the same AA area used in d. Electron (blue bars) and hole (red bars) contributions are colored. (f) Calculated $|\Psi|$ of the first confined hole state (see b) crossing E_F at different B as marked. The state originates from LL_{-1} , i.e., $V_{\text{tip}} < 0$ V when crossing. All scale bars identical.

confined states. The peaks of the first quadruplets in Figure 2a and Figure 5a (see, e.g., inset) often group in doublets, suggesting sizable values of either Δ_k^τ or Δ^σ (Fig. 1e,f). While Δ^σ is expected to be spatially homogeneous and only weakly varying between different quadruplets, the TB calculations predict strongly varying Δ_k^τ for different quadruplets (Fig. 4e), in accordance with our observations in the experimental spectra. For a quantitative comparison we focus on E_{add}^2 , which separates the two doublets within the first quadruplet. In view of the small value of the Zeeman splitting ($\Delta^\sigma \approx 800 \mu\text{eV}$ at 7 T), we approximate E_C^2 by E_{add}^3 to extract the valley splitting $\Delta_1^\tau \approx E_{\text{add}}^2 - E_{\text{add}}^3$. We record 20 spectra in the vicinity of an AA stacked area at $B = 7$ T to obtain a histogram of Δ_1^τ for electrons and holes (Fig. 5e), where Δ_1^τ could be determined with an experimental error smaller than 0.2 meV. The values strikingly group around the predicted $\Delta_1^\tau \approx 3$ meV found in the TB calculations (Fig. 4e), with a probable offset in the QD position relative to the tunneling tip (Supplement, Sec. 5) explaining the QD probing an area adjacent to the tunneling tip. We conclude that sizable Δ_k^τ separate quadruplets into doublets, while the smaller Δ^σ contributes to the odd addition energies within the doublets. Realizing such a controlled lifting of one of the two degeneracies in graphene QDs is a key requirement for 2-qubit gate operation². It enables Pauli blockade in exchange driven qubits as required for scalable quantum computation approaches using graphene². Our observation of valley splittings, so far elusive, provides a stepping stone towards the exploitation of the presumably large coherence time of electron spins in graphene QDs²⁻⁵.

In summary, we have realized graphene quantum dots without physical edges via electrostatic confinement in magnetic field using low disorder graphene crystallographically aligned to a hexagonal boron nitride substrate. We observe more than 40 charging peaks in the hole and electron sector arranged in quadruplets due to orbital splittings. The first few peaks on the hole and electron side show an additional doublet structure traced back to lifting of the valley degeneracy. Note that such a lifting is key for the use of graphene quantum dots as spin qubits². Tight binding calculations quantitatively reproduce the orbital splitting energy of 4 – 10 meV as well as the first orbital’s valley splitting energy of about 3 meV by assuming a tip potential deduced from an electrostatic Poisson calculation. Also the onset of confinement at about 2 T is well reproduced by the calculation. Our results demonstrate a much better controlled confinement by combining magnetic and electrostatic fields than previously found in graphene. Exploiting the present approach in transport merely requires replacing the tip by a conventional electrostatic gate with a diameter of about 100 nm. Moreover, the approach allows for straightforward tuning of (i) orbital splittings by changing the gate geometry and thus the confinement potential, (ii) valley splittings based on substrate interaction, (iii) the Zeeman splitting by altering the magnetic field, and (iv) the coupling of dot states to leads or to other quantum dots by changing the magnetic field or selecting a different quantum dot state. Finally, our novel mobile quantum dot enables a detailed investigation of structural details of graphene stacked on various substrates, by spatially mapping the quantum dot energies.

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