1	Does the nandicap principle explain the evolution of dimorphic ornaments:
2	2017-10-31
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Many species are sexually dimorphic, and interestingly, males in some species are dimorphic themselves: some males develop weapons and ornaments, whereas other males express rudimentary ornaments or none at all: horned beetles (Douglas J Emlen, Lavine, & Ewen-Campen, 2007; Moczek & Emlen, 2000), bluegill sunfish (Dominey, 1980; Gross & Charnov, 1980), ruffs (Lank, Smith, Hanotte, Burke, & Cooke, 1995), see for review (Simpson, Sword, & Lo, 2011). Males in some species are so extremely dimorphic that the morphs have been misclassified as different species. The selective maintenance of such male dimorphisms has been difficult to understand (Simpson et al., 2011). Yet, a recent paper by Clifton and colleagues (2016) concluded the evolution of male dimorphisms can be explained solely by the handicap principle (Zahavi, 1975). It is not intuitively obvious how the handicap principle can selectively maintain male dimorphisms, and no verbal explanations were provided. Here, we raise several caveats about this recent study and in particular we show that the findings are not generated by the handicap principle, but by an unrelated assumption of the model. This assumption is not unreasonable, but its stability needs to be examined before concluding that it provides an explanation for the evolution of male dimorphisms.

There are many versions and interpretations of the handicap hypothesis, but it is unclear which version was implemented for the authors' new model. This omission makes it impossible to understand the novelty of the model and how it succeeds in explaining male dimorphisms or why others failed. The authors cite the original handicap hypothesis (Zahavi 1975), and yet this version does not work (reviewed in Kirkpatrick 1986). They also cite evidence consistent with subsequent versions of the handicap hypothesis, but do not acknowledge that there are many models (Hurd, 1995; Lachmann, Számado, & Bergstrom, 2001; S. Számadó, 1999, 2011) and empirical studies (Kotiaho, 2001; Moreno-Rueda, 2007) that do not provide support (Számadó and Penn, 2015). The version that is usually cited as providing theoretical support is the 'strategic handicap' model (Zahavi 1977; (Grafen, 1990).

Grafen (1990) concluded that costly ornaments provide honest indicators of male quality when the fitness costs of signalling are greater for low than high quality individuals. The three main conditions in Grafen's model correspond to the main assumptions of the authors' model: (i) ornament size is an honest signal of health, as it is assumed that optimal ornament size is an increasing function of health; (ii) increasing ornament size is costly; and (iii) healthier individuals can better afford the costs of producing larger ornaments (i.e. differential cost assumption). The authors did not claim to base their model on Grafen's version, and instead used their own particular interpretation of Zahavi's (1975) handicap principle (S. Clifton, person. comm.). This is understandable given the limitations of Grafen's model (Thomas Getty, 1998; T. Getty, 2006; Hurd, 1995; Lachmann et al., 2001; S. Számadó, 1999, 2011; see Szabolcs Számadó & Penn, 2015 for a recent overview and discussion). However, there is a crucial and unstated difference between these models, and particularly the shape of the benefit function used in Grafen's (1990) versus the authors' model. Here we show that the results of the authors' model are due to the shape of the benefit function, which is not part of any versions of the handicap hypothesis to our knowledge. This means that either the results of the authors' new model are not driven the handicap hypothesis, or the authors are proposing a novel version of the handicap hypothesis.

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The critical assumption that drives the results of the authors' model is the shape of the benefits function, and therefore, we examined this assumption (see Box 1 for a description of the main details of the authors' model). For simplicity, we consider the difference between the fitness at the optimal ornament size, given by the "individual reproductive potential" ( $\varphi^{(ind)}$ ) function, and the fitness of the actual ornament size, to be the cost function (c) of signaling, since it provides the cost of deviating from the individual optimum. The study also applies Grafen's condition to this function (i.e., cost and differential cost). We consider the "the social reproductive potential" ( $\varphi^{(soc)}$ ) in the model to be the benefit function (b), since this

function provides the benefit (reproductive success) of the enlarged ornament. The study sets up two conditions (see section (b) *Generality*) for the emergence of two or more morphs: the first condition specifies that "Individual effects dominate reproductive potential for large ornament sizes" ("condition (i)", pp. 5), and the second specifies that "Social effects dominate reproductive potential for at least some range of ornament sizes greater than the population mean" ("condition (ii)", pp. 5). Together, these conditions imply that there must be an *inflection point*, where the function switches from convex to concave, or *vice versa*, in either the cost or in the benefit function. Without an inflection point, either the first or second conditions are satisfied but not both. Yet, neither Grafen's (1990) model, nor any other versions of the handicap hypothesis, include any such inflection point, and therefore cannot explain the results.

The inflection point is introduced in the benefit function of the authors' model, and the numerical example presented in the paper clearly shows that the handicap hypothesis does not explain the results (see Figure 1.a). This inflection point in the benefit function arises entirely from the assumption in the model that the fitness of an individual depends on the population average ("playing-the-field" model, Maynard Smith, 1982, pp. 23), rather than one or a series of individual opponents, as with other ESS models. The bimodal fitness curves, and hence the bimodal distribution of ornament size, are the result of this inflection point. If the benefit function has no inflection point and the cost function – that follows the assumptions of the Zahavi/Grafen handicap hypothesis – is not changed, then there is no such effect. These arguments can be illustrated by numerical examples (see Fig.1). We used the same cost function from the authors' study, but then also introduced a benefit functions that lacks an inflection point, though otherwise behaves exactly as the benefit function in the study (i.e., monotonically increasing with ornament size and a zero value at the population average). We investigate three different general types: a convex, a linear and a concave function. Figure 1

shows the results for different  $gammas(\gamma)$ , which describe the 'social sensitivity' or the strength of sexual selection. It is clear that the new fitness functions have only one optimum, even though the cost function remained unchanged and Grafen's (1990) second and third conditions (cost and differential cost) still hold. We do not assume that the benefit functions used in these three examples are realistic, but they show that Grafen's handicap conditions are not sufficient to explain the observed bimodal fitness curves in this new model. All in all, the playing-the-field assumption in the authors' model is reasonable, but it is not part any version of the handicap hypothesis to our knowledge.

Finally, regardless of the relevance of the handicap hypothesis, it is unclear that the authors' model provides a general explanation for the evolution of dimorphic male ornaments. First, closer examination indicates that the bimodal fitness function is typical only in a narrow range of conditions (what the authors refer to as health, h). Figure 2 shows the fitness as function of ornament size for various health values. It is clear from this figure that bimodality is observed in only a few cases. The effect is more pronounced for  $\gamma$  values <1 (see Figure 2.b  $\gamma$ =0.5), and the effect is almost negligible for  $\gamma$  values larger than one (see Figure 2.c). Figure 2.d shows an enlarged section from Figure 2.c to illustrate the effect more clearly, and that the result holds for only a narrow range of health values ( $\sim$  1.9). Note that the scale on x-axis is not indicated on Figure 2.c or 2.d in the original study (pp. 2).

Second, the evolutionary stability of the signalling equilibrium proposed in this new model was not investigated, but seems doubtful. The paper proposes a novel type of signalling equilibrium, in which signallers of the same type can send more than one signal, and yet the *receiver* response to this signalling strategy was not investigated. It is simply assumed to be evolutionarily stable. However, at any stable evolutionarily equilibrium, the signaller's strategy must be best response to the receiver's strategy – and *vice versa* (C. Bergstrom, Szamado, & Lachmann, 2002). Without this crucial step, signalling models are incomplete at

best and potentially misleading. The approach used in constructing this new model appears to be based on calculating a "signalling equilibrium" by searching only for the optimal signal intensity for signallers and keeping the receivers' evolutionary response fixed. Here we explore why the current shape of the receiver's response may not be the best response to the signaller strategy described in the Clifton et al (2016) model. The authors argue that communication is "mostly honest, at least for large enough variance in health." This conclusion might apply to certain scenarios: (i) the receiver can discriminate all signals, and thus it can effectively assess the quality of the signaller. If so, it should give the same response, as dictated by the receiver's optimum allocation, to the two morphs that belongs to the same health. In turn, this implies that one of these signals is redundant (the costlier one), and thus it will be selected against, hence the scenario is not evolutionarily stable. (ii) The other scenario is that some of the signals cannot be differentiated from signals used by other types. Receivers in such situations are expected to react to the average type expected (C. T. Bergstrom & Lachmann, 1998), and thus they will allocate resources accordingly. If so, the morph with lower signal cost will have higher fitness and the other signal will be selected against, and such scenario is not expected to be evolutionarily stable. Thus, it is unclear that the receiver strategy assumed by the authors is the best response to the signaller strategy obtained in the authors' model, and making conclusions about the evolutionary stability of this model crucially require investigating the co-evolutionary response of receivers.

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In summary, the model proposed by Clifton and colleagues (2016) to explain male dimorphisms is interesting, but there are several caveats that should be considered. First, there are many versions of the handicap hypothesis, but the authors did not clarify which one was the basis of their model – nor acknowledge the limitations of the relevant version that has theoretical support (i.e., the Zahavi-Grafen version). Second, the results of the authors' model do not arise from handicap hypothesis *per se*, but from an inflection in the benefit function

that emerges from the "playing-the-field" assumption. The conclusion of the paper ("Handicap principle implies emergence of dimorphic ornaments") is therefore misleading – or at least it requires a new version or reinterpretation of the handicap hypothesis. Third, the "playing-the-field" assumption is a reasonable, but the generality of the results appear rather limited (since bimodality is generated only in a narrow range of parameters for gamma values >1). Such limitations could be useful if they provided predictions for the conditions in which male dimorphisms are expected evolve (e.g. see D. J. Emlen, Hunt, & Simmons, 2005; Tomkins & Brown, 2004), but we could not detect any such predictions. Also, the conclusions about evolutionary stability of this model are premature until the co-evolution of the receivers' responses are investigated, and the evolutionary stability of the receiver strategy in this model is doubtful. We applaud the authors for the novelty of their approach to address this difficult problem, but this new model is unlikely to provide a general explanation for male dimorphism, at least in its current form. There are other viable hypotheses to explain dimorphic male phenotypes, including 'mimicry, sneaking, and fighting,' as the authors acknowledged, and these deserve more attention.

## Acknowledgements

We thank S. Clifton and colleagues for their courteous replies to our questions, S. Zala, and two anonymous reviewers for their thoughtful comments. Sz.Sz. was supported by OTKA grant K 108974 and by the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No 648693). DP acknowledges support from the Austrian National Science Foundation, FWF P 28141-B25 and FWF P 24711-B21.

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Box. 1 A description of the model by Clifton et al (2016).

Clifton et al (2016) model the change in the distribution of male ornament size due to selection on the differential fitness effect of ornaments with different sizes. The fitness of individuals is influenced by the cost of the ornaments (called 'individual reproductive potential',  $\varphi^{(ind)}$ ) and by the reproductive benefits of the ornament (called 'social reproductive potential',  $\varphi^{(soc)}$ ). The overall fitness is a weighted sum of these two factors:

$$\varphi = s\,\varphi^{(soc)} + (1-s)\varphi^{(ind)} = sa(2\,a_{opt} - a) + (1-s)\operatorname{sgn}(a - \overline{a})|a - \overline{a}|^{\gamma} \quad \text{Eq. 1}$$

Where a denotes ornament size, s is the relative importance of 'social effects' vs. 'individual effects', finally, gamma ( $\gamma$ ) describes the sensitivity of the 'social reproductive potential' to deviations from the population mean. Accordingly, the first part of Eq.1 gives the value of 'social reproductive potential' and the second part of the equation is the 'individual reproductive potential'.

## 232 Figure Legends

233 Figure 1 shows fitness curves with three different benefit functions (concave, linear and 234 convex respectively), while keeping the same cost function from the original paper with 235 Grafen's handicap conditions. Inlets show the benefit functions (the social reproductive potential,  $\varphi^{(\text{soc})}$ ), where: (a)  $\varphi^{(\text{soc})} = 1 - e^{(-a\gamma)} - (1 - e^{(-\bar{a}\gamma)})$ ,  $\bar{a} = 2$ ; (b)  $\varphi^{(\text{soc})} = a\gamma - \bar{a}\gamma$ ,  $\bar{a} = 2$ ; (c)  $\varphi^{(\text{soc})} = e^{(a-\bar{a}\gamma)}$ 236  $\omega^{\gamma} - e^{(\bar{a}-\omega)\gamma}, \omega=5, \bar{a}=2;$ 237 Figure 2 shows (a) the original benefit function (the social reproductive potential,  $\varphi^{(\text{soc})}$ ), and 238 239 the fitness curves for different values of gamma, as a function of ornament size (a), assuming an average ornament size  $\bar{a}$ =2: (b)  $\gamma$ =0.5, (c)  $\gamma$  =1.5, and (d)  $\gamma$  =1.5, enlarged section of (b). 240 241

## 242 Figure 1.



