Study of activation cross sections of deuteron induced reactions on erbium in the 32-50 MeV energy range

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Abstract

Activation cross sections of the $^{nat}Er(d,x)^{163,165,166,167,168,170}Tm$ and $^{nat}Er(d,x)^{171,161}Er$ nuclear reactions have been measured in the 32-50 MeV energy range, above 40 MeV for the first time. The activation method with stacked foil irradiation technique and gamma-ray spectroscopy were used. The experimental cross sections were compared with the theoretical predictions in the TENDL-2015 library.

Keywords: erbium target; deuteron irradiation; cross section; nuclear reaction model code

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1. Introduction

We perform systematic study of excitation functions of light ion induced nuclear reactions on rare earth isotopes, to investigate production routes of diagnostic and therapeutic radioisotopes with potential use in nuclear medicine.

In case of erbium target the activation cross sections of alpha particle induced reactions up to 40 MeV (Király et al., 2007, 2008) and the proton induced reactions up to 70 MeV (Hermanne et al., 2011a; Tarkanyi et al., 2016; Tárkányi et al., 2008, 2009) have already been reported by us. For the activation cross-sections of deuteron induced nuclear reactions on erbium only our experimental data sets exist, published up to 40 MeV (Hermanne et al., 2011b; Tarkanyi et al., 2007b; Tárkányi et al., 2007c; Tárkányi et al., 2007a). In this work we extend the projectiles' energy range up to 50 MeV energy. The measured data are relevant for the general activation database and for further development of theoretical codes. Among the investigated products the ¹⁶⁵Tm \rightarrow ¹⁶⁵Er, ¹⁶⁹Er, ¹⁶⁷Tm, ¹⁷⁰Tm and ¹⁷¹Er \rightarrow ¹⁷¹Tm radio nuclei are of interest in nuclear medicine.

2. Experimental

The excitation functions were measured by the activation method using stacked foil irradiation. The stack was irradiated at an external beam-line of the Cyclone 110 cyclotron of the Université Catholique in Louvain la Neuve (LLN) for 40 min with a 50 MeV, 50 nA deuteron beam. The stack contained a sequence of 10 blocks, each consisting of Al (10 μ m), Sr(NO₃)₂ (3 μ m, sedimented), Al (50 μ m), Er (32 μ m), Al (10 μ m), Ba(NO₂) (2 μ m, sedimented), Al (50 μ m) and Ag (10 μ m) foils. The 10 Er targets covered the 50-32 MeV energy range (up to 40 MeV it was already published by our group). The targets were irradiated in a short Faraday cup. Gamma-ray spectra were measured with HPGe detectors coupled to Canberra multi-channel analyzers equipped with GENIE acquisition software. Four series of gamma-ray spectra were measured to follow the decay, started at different times after the end of bombardment, i.e. 8.9-10.7 h, 53.3-69.6 h, 268.1-313.5 h and 1700.8-1985.0 h, respectively. Gamma-ray spectra were evaluated by the automatic fitting algorithm included in the Genie 2000 package (Canberra, 2000)or in an iterative process using the Forgamma code (Székely, 1985). The decay data were adopted from

NUDAT 2.6 (NuDat, 2014) and the Q values of the contributing reactions from the Q-value calculator (Pritychenko and Sonzogni, 2003) and are shown in Table 1.

The recommended data for simultaneously measured excitation functions of the 27 Al(d,x) 22,24 Na monitor reactions were taken from the IAEA database (Tárkányi et al., 2001)(last updated in 2007). As erbium is not monoisotopic, therefore so called elemental cross-sections were determined. Uncertainty of cross-sections was determined according to the recommendation (International-Bureau-of-Weights-and-Measures, 1993) by taking the sum in quadrature of all individual contributions: beam current (7%), beam-loss corrections (max. 1.5%), target thickness (1%), detector efficiency (5%), photo peak area determination and counting statistics (1-20 %).

The initial beam energies in targets (for stack preparation) were obtained from a degradation calculation based on the incident energy and the Andersen (Andersen and Ziegler, 1977) polynomial approximation of stopping powers. In order to fit with the recommended monitor reactions a correction was applied to the measured collected charge (final) (Tárkányi et al., 1991). Uncertainty of energy was estimated by following the cumulative effects of possible uncertainties (primary energy, target thickness, energy straggling, correction to monitor reaction) during the energy degradation.

				Contributing	Q-value
Nuclide	Half-life	E _γ (keV)	Ι _γ (%)	process	(MeV)
¹⁷⁰ Tm	128.6 d	84.25	2.48	170 Er(d,2n)	-3.32
¹⁶⁸ Tm	93.1 d	198.25	54.49	167 Er(d,n)	3.09
		447.52	23.98	168 Er(d,2n)	-4.69
		631.71	9.26	170 Er(d,4n)	-17.95
		720.39	12.21		
		741.36	12.81		
		816.0	50.95		
		821.16	11.99		
¹⁶⁷ Tm	9.25 d	207.8	42.0	166 Er(d,n)	2.68
				167 Er(d,2n)	-3.76
				168 Er(d,3n)	-11.53
				170 Er(d,5n)	-24.79
¹⁶⁶ Tm	7.70 h	80.59	11.5	166 Er(d,2n)	-6.05
-		691.25	7.5	167 Er(d,3n)	-12.48
-		705.33	11.1	168 Er(d,4n)	-20.25
		778.81	19.1	170 Er(d,6n)	-33.52
		785.90	10.0		
		1176.70	9.6		
¹⁶⁵ Tm	30.06 h	242.92	35.5	164 Er(d,n)	2.05
		297.68	12.7	166 Er(d,3n)	-13.07
				$^{167}{\rm Er}({\rm d},4{\rm n})$	-19.51
				168 Er(d, 5n)	-27.28
				170 Er(d,7n)	-40.54
¹⁶³ Tm	1.810 h	104.32	18.6	162 Er(d, n)	1.46
		241.31	10.9	164 Er(d,3n)	-14.29
				166 Er(d,5n)	-29.42
				¹⁶⁷ Er(d,6n)	-35.85
				168 Er(d,7n)	-43.62
¹⁷¹ Er	7.516 h	111.62	20.5	$^{170}{\rm Er}({\rm d},{\rm p})$	3.46
		308.29	64		
¹⁶¹ Er	3.21 h	211.15	12.2	162 Er(d,p2n)	-11.43
		314.77	2.49	¹⁶¹ Tm decay	-15.51
		826.6	64	2	

Table 1. Decay characteristics of the investigated reaction products

Abundances (%): ¹⁶²Er (0.14), ¹⁶⁴Er (1.61), ¹⁶⁶Er (33.6), ¹⁶⁷Er (22.95), ¹⁶⁸Er (26.8), ¹⁷⁰Er (14.9) Increase the Q-values if compound particles are emitted by: np-d, +2.2 MeV; 2np-t, +8.48 MeV;

n2p-³He, +7.72 MeV; 2n2p- α , +28.30 MeV. The energies in bold are used for evaluation.

3. Results and discussion

3.1 Excitation functions

The measured cross-sections are shown in Figs. 1-8 in comparison with the earlier experimental data and with the theoretical predictions. The numerical data are collected in Tables 2 - 3.

			¹⁷⁰ Tm		¹⁶⁸ Tm		¹⁶⁷ Tm		¹⁶⁶ Tm	
Е	$\Delta \mathbf{E}$	σ	Δσ	σ	Δσ	σ	Δσ	σ	Δσ	
M	MeV				m	b				
49.57	0.20	5.75	3.50	68.32	8.39	204.01	22.90	226.65	26.37	
48.05	0.24	5.62	1.09	66.37	7.77	215.31	24.18	205.21	23.50	
46.49	0.28	7.51	1.11	90.16	10.51	244.48	27.46	196.55	22.63	
44.89	0.32	8.39	2.01	72.70	8.72	253.84	28.50	197.30	22.81	
43.25	0.36	3.51	0.49	81.19	9.40	292.10	32.79	210.80	23.96	
41.56	0.40	5.93	2.29	92.58	11.04	293.99	33.00	236.32	27.15	
39.82	0.44	4.88	1.21	102.86	12.20	287.67	32.30	283.68	32.45	
38.02	0.49	7.38	1.63	101.54	12.20	236.45	26.54	278.06	31.63	
36.16	0.54	10.11	4.85	132.60	15.50	240.90	27.05	355.41	40.53	
34.22	0.58	8.31	3.52	173.69	19.50	243.49	27.33	381.52	43.53	
32.19	0.63	6.29	2.06	211.23	24.07	256.09	28.75	441.26	50.20	

Table 2. Experimental cross-sections for the $^{nat}Er(d,x)^{170,168,167,166}$ Tm reaction

Table 3. Experimental cross-sections for the ${}^{nat}Er(d,x){}^{165,163}Tm$, ${}^{171,161}Er$ reaction reactions

		¹⁶⁵	ſm	163	ſm	171	Er	161	Er	
Е	$\Delta \mathbf{E}$	σ	Δσ	σ	Δσ	σ	Δσ	σ	Δσ	
M	MeV		mb							
49.57	0.20	377.07	42.38	353.80	41.05	3.73	0.49	15.86	2.28	
48.05	0.24	392.09	52.71	311.33	35.70	2.95	0.39	15.86	2.09	
46.49	0.28	407.74	45.88	271.66	30.87	3.85	0.47	12.45	1.64	
44.89	0.32	409.52	46.01	224.00	26.11	3.72	0.47	9.86	1.49	
43.25	0.36	447.23	50.24	176.91	20.58	4.22	0.51	7.52	1.21	
41.56	0.40	432.48	48.61	113.70	14.56	5.07	0.62	3.81	1.14	
39.82	0.44	444.82	50.03	66.35	8.66	4.73	0.58	2.19	0.70	
38.02	0.49	460.97	51.81	43.95	7.56	5.23	0.64			
36.16	0.54	435.69	48.97	31.96	8.33	5.73	0.70			
34.22	0.58	442.00	49.62	25.15	6.77	7.81	0.93			
32.19	0.63	453.67	50.97	35.20	9.24	8.11	0.96			

3.1.1 Production ¹⁷¹Tm ($T_{1/2} = 1.92 y$)

In spite of our efforts, as in our previous works, it was impossible to deduce reliable crosssections for the medically relevant ¹⁷¹Tm produced via the ¹⁷⁰Er(d,n) reaction due to low cross sections and to the very low intensity of the low energy (66.7 keV) gamma-line.

3.1.2 Production of 170 Tm ($T_{1/2} = 128.6 d$)

¹⁷⁰Tm is produced in the ¹⁷⁰Er(d,2n) reaction. The β -decay of ¹⁷⁰Tm is followed by emission of a weak 84.3 keV gamma-line. The overlapping and contamination from the 84.94 keV K_{β 1} X-ray line from gamma-ray excitation of Pb (shielding of the detector) were subtracted, resulting in small residual intensities with large uncertainties. The resulting excitation function is shown in Fig. 1. The comparison with the TENDL-2015 on-line library shows good agreement.

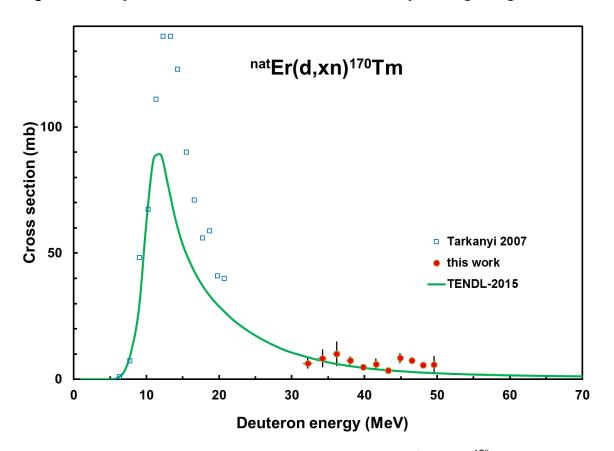


Fig. 1 Experimental and theoretical excitation functions of the ^{nat}Er(d,xn)¹⁷⁰Tm reaction

3.1.3 Production of ¹⁶⁸Tm ($T_{1/2} = 93.1 d$)

The excitation function of ¹⁶⁸Tm is shown in Fig. 2. The agreement with the earlier data is very good in the overlapping energy range. The theory describes well the experimental data, but at higher deuteron energies an obvious energy shift can be observed.

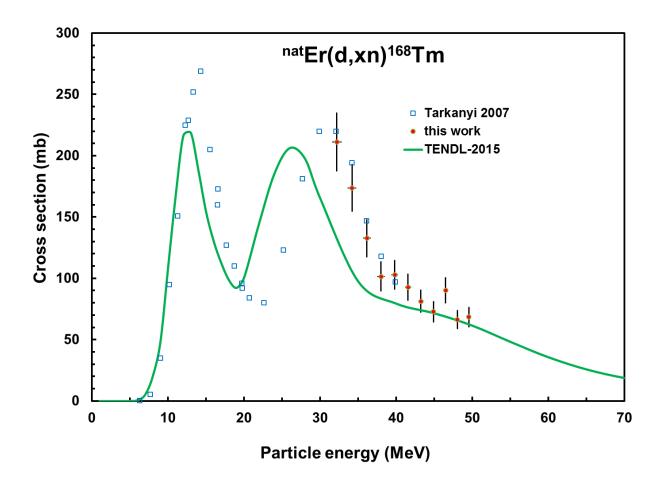


Fig. 2 Experimental and theoretical excitation functions of the $^{nat}Er(d,xn)^{168}Tm$ reaction

3.1.4 Production of 167 Tm ($T_{1/2}$ = 9.25 d)

The excitation function for production of ¹⁶⁷Tm is shown in Fig. 3. The theory underestimates the experiment and again some obvious energy shift is observed at high energies.

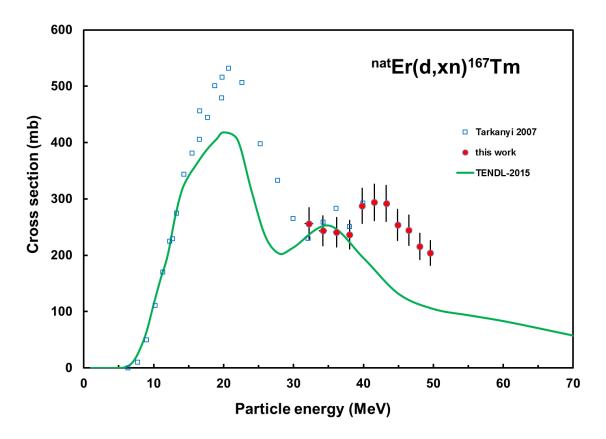


Fig. 3 Experimental and theoretical excitation functions of the $^{nat}Er(d,xn)^{167}Tm$ reaction

3.1.5 Production of ¹⁶⁶Tm ($T_{1/2}$ = 7.70 h)

The cross-sections for production of the ¹⁶⁶Tm radionuclide are shown on Fig 4. The new data are in acceptable agreement with our previous experimental data in the low energy range. The magnitude of the TENDL prediction is acceptable, but an energy shift is also indicated in this case.

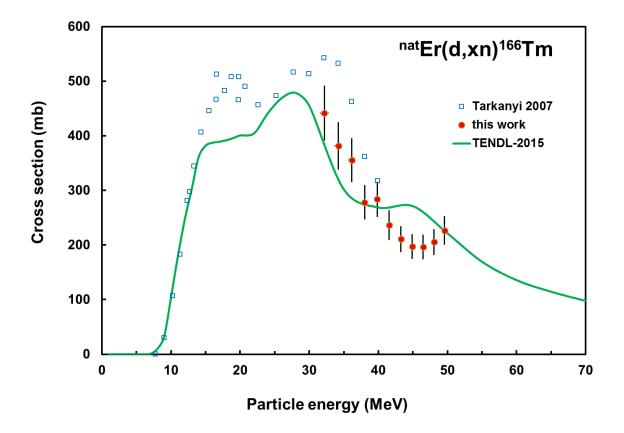


Fig. 4 Experimental and theoretical excitation functions of the $^{nat}Er(d,xn)^{166}Tm$ reaction

3.1.6 Production of 165 Tm ($T_{1/2}$ = 30.06 h)

According to Fig. 5 the new data are lower compared to our previous experimental data in the overlapping energy range, which may be caused by the relatively large uncertainties, but fit rather well with the TENDL-2015 calculations.

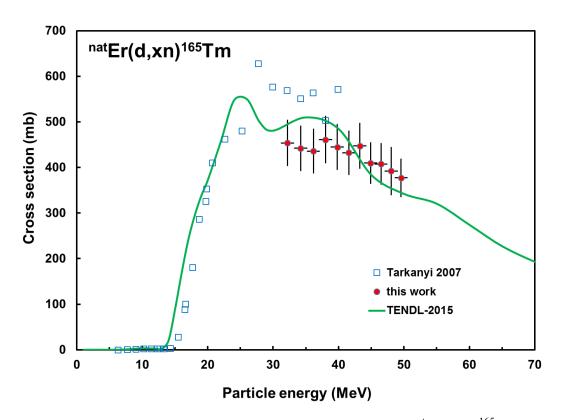


Fig. 5. Experimental and theoretical excitation functions of the ^{nat}Er(d,xn)¹⁶⁵Tm reaction

3.1.7 Production of ¹⁶³Tm ($T_{1/2}$ = 1.810 h)

As obvious from the Fig. 6, a significant energy shift can be observed above 30 MeV between experiment and theory and above 50 MeV the experimental data become significantly higher.

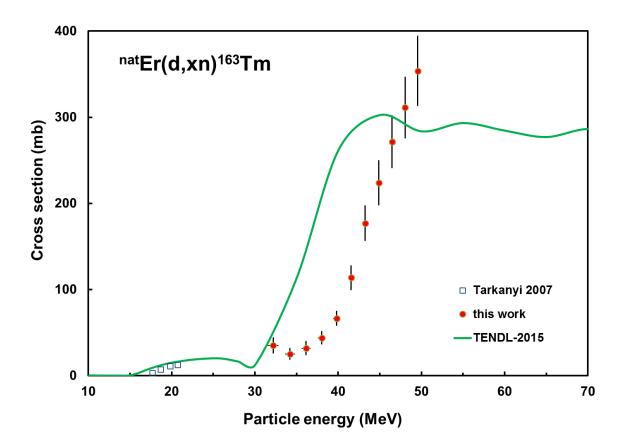


Fig.6 Experimental and theoretical excitation functions of the $^{nat}Er(d,xn)^{163}Tm$ reaction

3.1.8 Production of $^{171}Er(T_{1/2}=7.516 h)$

The prediction systematically underestimates both experimental data sets in the whole energy range (Fig. 7). The reason is the poor modeling of the deuteron breakup, which leads to underestimation of the 170 Er(d,p) reaction by the used model (Khandaker et al., 2015; Khandaker et al., 2014), which is the only contributing reaction to the 171 Er formation.

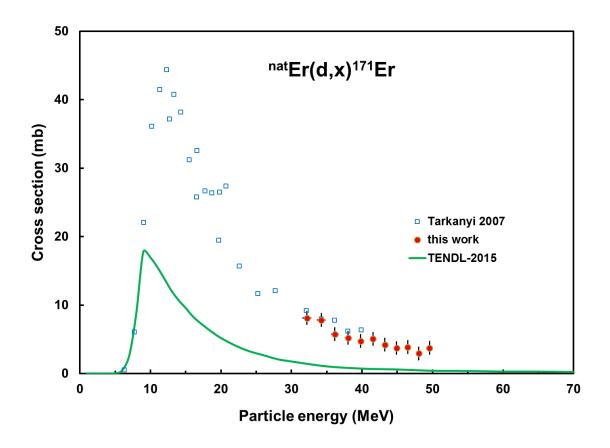


Fig. 7 Experimental and theoretical excitation functions of the $^{nat}Er(d,x)^{171}Er$ reaction

3.1.9 Production of ${}^{161}Er(T_{1/2}=3.21 h)$

For production of ¹⁶¹Er no earlier experimental cross section data were found. It is even not covered by our previous work because of the relatively low half-life and the low expected cross section in the previously measured energy region. The excitation function for cumulative production (from ¹⁶¹Tm, $T_{1/2}$ = 30.2 min, ε =100%) is shown in Fig. 8 where the theory overestimates the experimental values up to 45 MeV, but a good agreement is seen above this value, which can also be the result of an energy shift.

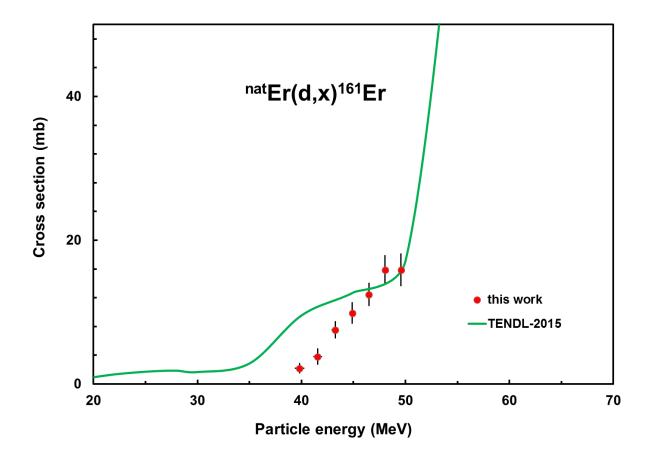


Fig. 8 Experimental and theoretical excitation functions of the $^{nat}Er(d,x)^{161}Er$ reaction

4. Integral yields

Integral yields down to the reaction threshold as a function of the energy were calculated by using fitted curves to experimental cross-section data. The results for physical yields (Bonardi, 1987; Otuka and Takács, 2015) are presented in Fig. 9 in comparison with the experimental yield data in the literature (Dmitriev et al., 1982; Dmitriev et al., 1980). Comparing our new calculated results with the data from the literature the general conclusion is that the previous results of Dmitriev et al. are slightly lower than our new data except in the case of ¹⁶³Tm, but their data are definitely higher at the lower energy region.

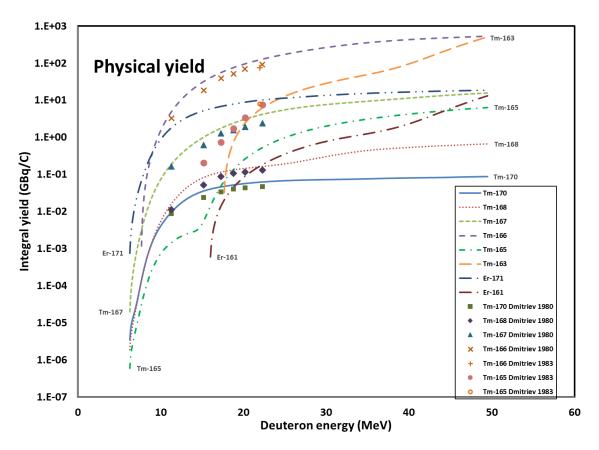


Fig. 9 Integral yields for production of the ^{163,165,166,167,168,170}Tm and ^{171,161}Er nuclear reactions deduced from the excitation functions in comparison with the literature experimental integral yields.

5. Summary and conclusions

Activation cross sections of the ^{nat}Er(d,x)^{163,165,166,167,168,170}Tm and ^{nat}Er(d,x)^{171,161}Er nuclear reactions have been measured experimentally in the 32-50 MeV energy range, above 40 MeV for the first time. The ^{nat}Er(d,x)¹⁶¹Er reaction cross section data are reported here for the first time. The agreement with the earlier experimental data in the overlapping energy range is in most cases is acceptable, and with the theoretical predictions in the TENDL-2015 theoretical library only in several cases is acceptable. The discrepancy by the (d,p) reaction and the observed energy shift at higher energies suggest an improvement in the code. Comparison of charged particle production routes of medically relevant ^{167,170,171}Tm and ^{165,169}Er radioisotopes were discussed in detail in our previous works. By extending the energy range the present work gives important information on cross sections for production of medically relevant ¹⁶¹Er, ¹⁶³Tm, ¹⁶⁷Tm and to test TENDL predictions in broader energy range.

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References

Andersen, H.H., Ziegler, J.F., 1977. Hydrogen stopping powers and ranges in all elements. The stopping and ranges of ions in matter, Volume 3. Pergamon Press, New York.

Bonardi, M., 1987. The contribution to nuclear data for biomedical radioisotope production from the Milan cyclotron facility, in: Okamoto, K. (Ed.), Consultants Meeting on Data Requirements for Medical Radioisotope Production. IAEA, INDC(NDS)-195 (1988), Tokyo, Japan, p. 98.

Canberra, 2000. http://www.canberra.com/products/radiochemistry_lab/genie-2000-software.asp.

Dmitriev, P.P., Molin, G.A., Panarin, M.V., 1980. Yields of Tu-165, Tu-166, Tu-167, Tu-168, and Tu-170 in Reactions with Protons, Deuterons, and Alpha-Particles. At. Energy (N.Y., NY, U.S.) 48, 419-421.

Dmitriev, P.P., Krasnov, N.N., Molin, G.A., 1982. Radioactive nuclide yields for thick target at 22 MeV deuterons energy. Yadernie Konstanti 34, 38.

Hermanne, A., Rebeles, R.A., Tarkanyi, F., Takacs, S., Kiraly, B., Ignatyuk, A.V., 2011a. Cross sections for production of longer lived Tm-170,Tm-168,Tm-167 in 16 MeV proton irradiation of Er-nat. Nucl. Instrum. Methods Phys. Res., Sect. B 269, 695-699.

Hermanne, A., Rebeles, R.A., Tarkanyi, F., Takacs, S., Spahn, I., Ignatyuk, A.V., 2011b. High yield production of the medical radioisotope Tm-167 by the Er-167(d,2n) reaction. Appl. Radiat. Isot. 69, 475-481.

International-Bureau-of-Weights-and-Measures, 1993. Guide to the expression of uncertainty in measurement, 1st ed. International Organization for Standardization, Genève, Switzerland.

Khandaker, M.U., Haba, H., Otuka, N., Usman, A.R., 2014. Investigation of (d,x) nuclear reactions on natural ytterbium up to 24 MeV. Nucl. Instrum. Methods Phys. Res., Sect. B 335, 8-18.

Khandaker, M.U., Haba, H., Murakami, M., Otuka, N., Abu Kassim, H., 2015. Excitation functions of deuteron-induced nuclear reactions on natural platinum up to 24 MeV. Nucl. Instrum. Methods Phys. Res., Sect. B 362, 151-162.

Király, B., Tárkányi, F., Takács, S., Hermanne, A., Kovalev, S.F., Ignatyuk, A.V., 2007. Excitation funcions of alpha-induced nuclear reactions on natural erbium and natural ytterbium targets, in: Bersillon, O., Gunsing, F., Bange, E. (Eds.), International Conference on Nuclear Data for Science and Technology. EDP Sciences Nice, France, p. 1371.

Király, B., Tárkányi, F., Takács, S., Hermanne, A., Kovalev, S.F., Ignatyuk, A.V., 2008. Excitation functions of alpha-induced nuclear reactions on natural erbium. Nucl. Instrum. Methods Phys. Res., Sect. B 266, 549-554.

NuDat, 2014. NuDat2 database (2.6). National Nuclear Data Center, Brookhaven National Laboratory. http://www.nndc.bnl.gov/nudat2/

Otuka, N., Takács, S., 2015. Definitions of radioisotope thick target yields. Radiochim. Acta 103, 1-6.

Pritychenko, B., Sonzogni, A., 2003. Q-value calculator. NNDC, Brookhaven National Laboratory. http://www.nndc.bnl.gov/qcalc.

Székely, G., 1985. Fgm - a flexible gamma-spectrum analysis program for a small computer. Comput. Phys. Commun. 34, 313-324.

Tarkanyi, F., Ditroi, F., Takacs, S., Hermanne, A., Baba, M., 2016. Activation cross sections of proton and deuteron induced nuclear reactions on holmium and erbium, related to the production of Er-161 and Er-160 medical isotopes. Appl. Radiat. Isot. 115, 262-266.

Tárkányi, F., Szelecsényi, F., Takács, S., 1991. Determination of effective bombarding energies and fluxes using improved stacked-foil technique. Acta Radiol., Suppl. 376, 72.

Tárkányi, F., Takács, S., Gul, K., Hermanne, A., Mustafa, M.G., Nortier, M., Oblozinsky, P., Qaim, S.M., Scholten, B., Shubin, Y.N., Youxiang, Z., 2001. Beam monitor reactions (Chapter 4). Charged particle cross-section database for medical radioisotope production: diagnostic radioisotopes and monitor reactions., TECDOC 1211. IAEA, p. 49,<u>http://www.nds.or.at/medical</u>.

Tárkányi, F., Hermanne, A., Takács, S., Ditrói, F., Király, B., Kovalev, S.F., Ignatyuk, A., 2007a. Investigation of new routes for production of the therapeutic radionuclides ¹⁶⁹Yb and ¹⁶⁵Er. Journal of Labelled Compounds and Radiopharmaceuticals. Supplement 50, 99.

Tárkányi, F., Hermanne, A., Király, B., Takács, S., Ditrói, F., Baba, M., Ohtsuki, T., Kovalev, S.F., Ignatyuk, A.V., 2007b. Study of activation cross-sections of deuteron induced reactions on erbium: Production of radioisotopes for practical applications. Nucl. Instrum. Methods Phys. Res., Sect. B 259, 829-835.

Tárkányi, F., Hermanne, A., Takács, S., Ditrói, F., Király, B., Baba, M., Ohtsuki, T., Kovalev, S.F., Ignatyuk, A.V., 2007c. Study of activation cross sections of deuteron-induced reactions on erbium for applications. J. Labelled Compd. Radiopharm. 50, 487-488.

Tárkányi, F., Takács, S., Hermanne, A., Ditrói, F., Király, B., Baba, M., Ohtsuki, T., Kovalev, S.F., Ignatyuk, A.V., 2008. Study of activation cross sections of proton induced reactions on erbium for practical applications. Nucl. Instrum. Methods Phys. Res., Sect. B 266, 4872-4876.

Tárkányi, F., Takács, S., Hermanne, A., Ditrói, F., Király, B., Baba, M., Ohtsuki, T., Kovalev, S.F., Ignatyuk, A.V., 2009. Investigation of production of the therapeutic radioisotope Er-165 by proton induced reactions on erbium in comparison with other production routes. Appl. Radiat. Isot. 67, 243-247.