

# **Lift and drag force measurements on basic models of low-speed axial fan blade sections**

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## **ABSTRACT**

This paper presents comparative data on the aerodynamic lift and drag of basic model representations of low-speed axial fan blade sections. Three main types of blades are investigated: flat plate, cambered plate and RAF6-E profiled airfoil. Lift and drag force are measured at three different Reynolds numbers ( $0.6 \cdot 10^5$ ,  $10^5$  and  $1.4 \cdot 10^5$ ) around the threshold value of  $10^5$ . The measurement data is compared to literature data. The aerodynamic force measurements reveal that, for Reynolds numbers below  $10^5$ , cambered plate blade sections can be superior to airfoil profiles in terms of aerodynamic efficiency, especially in the high-load range. The effect of leading edge bluntness is also investigated. Leaving the leading edge of cambered plates blunt, tends to be uncritical for low Reynolds numbers at angles of attack between  $4^\circ$  and  $10^\circ$  but is critical at angles between  $0^\circ$  and  $4^\circ$ .

## **KEYWORDS**

airfoil, cambered plate blade, low-Reynolds-number axial fan, low-speed fan

## **NOMENCLATURE**

$A$	area [mm <sup>2</sup> ]
$c$	chord [mm]
$C_L$	lift coefficient
$C_D$	drag coefficient
$d$	maximum height of the camber line [mm]

$D$  rotor diameter [m]

$F_L$  lift force [N]

$F_D$  drag force [N]

$p_{dyn}$  dynamic pressure [Pa]

$Re$  chord based Reynolds number

$Re_{AMCA, limit}$  diameter based limiting Reynolds number

$Re_{c, limit}$  chord based limiting Reynolds number

$s$  span [mm]

$t$  thickness [mm]

$u_t$  circumferential velocity [m/s]

$U$  absolute uncertainty

$v$  free-stream velocity [m/s]

$\alpha$  angle of attack [°]

### **Abbreviations**

AR aspect ratio =  $s/c$

LDR Lift-to-drag ratio

LE leading edge

max maximum value

OM order of magnitude

TE trailing edge

2D two-dimensional

## 1) INTRODUCTION AND OBJECTIVES

The focus of the current paper is the lift and drag force acting on the blade sections of low-speed axial fans. The blade sections investigated in the present paper are termed herein as “profiles”. ”Low-speed” is defined as being equivalent to the validity of incompressible flow assumption. The low-speed fans operating in the vicinity of humans are often characterized by moderate chord based Reynolds numbers ( $Re \leq 10^5$ ), which is frequently due to small rotor diameter or low rotational speed e.g. computer processor cooling fans [1], cooling fans for electric motors [2][3], or refrigerator fans [4]. These fans often have to fulfil size requirements (only a fixed space is available), while maintaining the prescribed pressure rise, making the investigation of the efficiency of these small fans necessary. Even if the size of the fan is not limited,  $Re \leq 10^5$  may still occur, if the rotor speed of the larger-sized ventilating fan is controlled by means of a frequency converter which reduces the rotation speed. At their nominal speed, these fans usually operate at  $Re > 10^5$ , but by controlling the rotor speed, a speed reduction down to 20% can be reached compared to the nominal value, which provokes an operation of  $Re \leq 10^5$ .

Regulation 327/2011/EU [5] formulates energy efficiency requirements regarding fans in the EU, driven by motors with an electric input power between 125 *W* and 500 *kW*. The regulation only deals with energy efficiency, however noise emission is also linked to aerodynamic losses. This is confirmed by the empirical relations for the noise emission

of fans in [6], which include the fan efficiency as a parameter. Thus the present authors' long-term aim is to reduce the acoustic emission along with the aerodynamic losses. The aerodynamic measurements linked to preliminary acoustic studies [7][8] are presented in this paper.

At the approximate threshold of  $Re = 10^5$ , significant changes are expected in the aerodynamic characteristics of fan blades. The diagrams in [9] indicate that the aerodynamic performance of profiled, i.e. non-plate airfoil sections, deteriorates rapidly below  $Re = 10^5$ . This deterioration in airfoil performance manifests itself in reduced lift, and thus, reduced lift-to-drag ratio (LDR). Such trends were also reported in [10]. On the basis of the aforementioned studies, cambered plate blading may be superior in terms of both aerodynamic performance and efficiency to profiled airfoil blading in the case of low-speed axial fans operating below  $Re = 10^5$ .

The Reynolds numbers below which Reynolds number dependence becomes significant are termed herein "limiting Reynolds numbers". The Reynolds number in the AMCA 211-13 standard [11] is calculated based on the rotor diameter,  $D$  and the circumferential velocity,  $u_t$ :

$$Re_{AMCA,limit} = \frac{Du_t}{\nu} \quad (1)$$

The limiting Reynolds number according to [11] is  $Re_{AMCA,limit} = 0.8 \cdot 10^6$  for propeller fans. In this paper the Reynolds number is defined based on the chord length,  $c$  of the investigated profile and the free-stream velocity,  $v$ :

$$Re_{c,limit} = \frac{cv}{\nu} \quad (2)$$

In accordance with the findings in [9] the chord based Re limit is set to  $Re_{c,limit} = 10^5$  herein. The ratio of the two limiting Reynolds numbers can be calculated:

$$\frac{Re_{AMCA,limit}}{Re_{c,limit}} = \frac{8 \cdot 10^5}{1 \cdot 10^5} = 8 \quad (3)$$

$$\frac{Re_{AMCA,limit}}{Re_{c,limit}} = \frac{D}{c} \frac{u_t}{v} \quad (4)$$

The calculation of limiting Reynolds numbers  $Re_{AMCA,limit}$  and  $Re_{c,limit}$  are self-consistent provided that their ratio Equation (3) is characteristic for the ratio of Equation (4):

$$\frac{D}{c} \frac{u_t}{v} \approx 8 \quad (5)$$

The relation above is valid for axial fans of relatively low-solidity (low chord-to-spacing ratio), high-aspect-ratio blading, i.e. propeller fans. Fitting to the experiments in [9], measurements around the threshold value of  $Re = 10^5$  are presented herein (at  $Re = 0.6 \cdot 10^5$ ,  $10^5$ , and  $1.4 \cdot 10^5$ ) and compared with literature data, in order to offer a comparative investigation in this  $Re$  range.



The cambered plate blading of industrial fans is often manufactured by means of rolling sheet metal segments, produced using methods such as laser cutting, without any additional treatment (rounding or tapering) of leading edge (LE) and trailing edge (TE) geometry. The LE and TE of such blades are therefore blunt. In addition to simplifying the required manufacturing, the literature suggests that the bluntness or sharpness of LE and TE offers a potential for improving the aerodynamic performance at moderate  $Re$ . This trend is supported by the following references [9, 12, 13, 14, 15]. In [12], both blunt LE and TE are found to improve the aerodynamic performance below  $Re = 10^4$ . However, [9] concludes that the TE geometry has a minor effect on the lift and drag characteristics of thin models (less than 6% thick) at low  $Re$ . Therefore, the present investigation focusses on the aerodynamic effect of the LE bluntness. In [9], the Pfenninger airfoil, of thinner and sharper LE than the Eppler 61 airfoil in [13], was found to provide a higher LDR below  $Re = 9 \cdot 10^4$ . In [14][15], a significant increase in lift was found in the case of a reversed NACA profile (facing the sharp TE with the inflow) at  $Re \approx 2.1 \cdot 10^4$ . In the aforementioned cases [9, 12, 14, 15], the present authors presume that the edge-like, high-curvature segments of the blunt LE contour line act as “turbulators” [9]. Such turbulators promote the eddy-induced energy transfer into the boundary layer. Therefore, they can beneficially influence: a) the laminar separation bubble(s) occurring in the vicinity of the LE, and b) the laminar-to-turbulent transition, at low  $Re$ .

This paper presents detailed comparative data on aerodynamic lift and drag of basic model representations of blade sections, obtained from a) historical measurement databases used in design of industrial axial fans [16], b) the basic literature focussing on micro-air vehicle applications [9], and c) own measurements. The aim of the own experiments is to reproduce the measurement layouts realised in [9], as they serve as the main reference for the work presented herein. In accordance with [9], the aerodynamic efficiency is defined in terms of LDR. The angle of attack at which the highest LDR is reached is of great importance from a design point of view. Based on the considerations in [10][16], the maximum LDR represents the optimal operation of the elemental blade section, in terms of moderation of blade friction loss relative to the isentropic total pressure rise. The comparative investigation incorporates data in the extended range of  $0^\circ \leq \alpha \leq 20^\circ$ .

The objective of the present paper is to examine the aerodynamic effect of LE bluntness, low Re and the combination of these two on the lift and drag coefficients of basic model representations of low-speed axial fan blade sections.

## **2) EXPERIMENTAL TECHNIQUE**

The experiments were conducted in the wind tunnel, shown in Figure 1., located in the Department of Fluid Mechanics, Budapest University of Technology and Economics. The detailed characteristics of the wind tunnel are published in [17]. The turbulence intensity at the inlet of the test section is 0.8%. According to [9], turbulence intensity up to about

1% has a negligible influence on the lift and drag characteristics of thin models at low  $Re$ . The test section of the wind tunnel is bounded by a wall on two sides. The walls are perpendicular to the span of the profiles. The width of the test section is 150 mm. The size of the inlet is 150x1000 mm. One of the side walls can be opened in order to change the profiles in the test section. The other, fixed wall, contains the force measurement system of the wind tunnel, with a built-in protractor. The profiles are equipped with a handle, by which they are mounted, and the force acting on them is measured. The wind tunnel serves for both aerodynamic and acoustic [7][8] studies on the profiles under present investigation.

On the basis of [10][16][18], isolated airfoil data can approximately be applied in design of blade cascades if the solidity is below 0.7. Therefore, the results presented herein are relevant for such low-solidity axial fan cascades. The results related to the cambered plate blade can also be utilized in the design of blades of centrifugal fans with cambered plate blades, as long as the fan can be modelled with blade cascade data with low solidity [19]. Similarly the findings can be incorporated into the design of cambered-plate guide vane blades, e.g. subsequently mounted “bolt-on” outlet guide vanes, with low solidity.

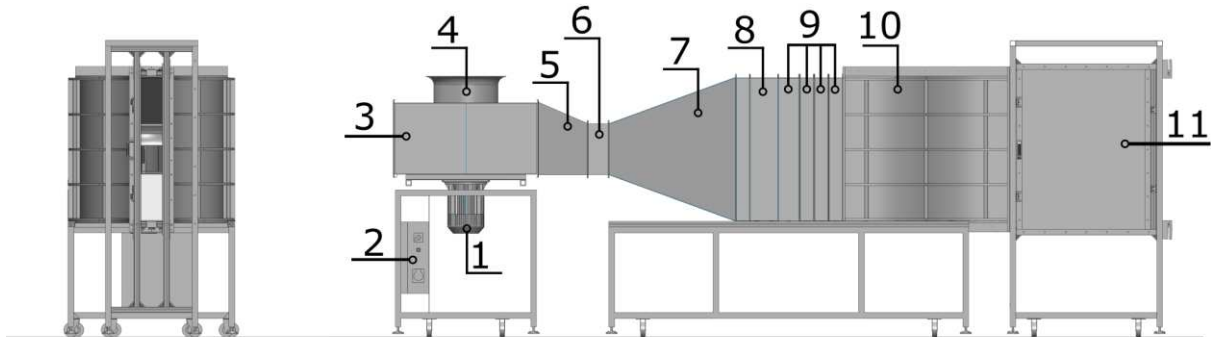


Figure 1. [17] Measurement setup. **1.** Motor **2.** Frequency converter **3.** Radial fan **4.** Inlet bell mouth **5.** Guide vanes **6.** Flexible connector **7.** Split diffuser **8.** Honeycomb **9.** Turbulence reduction screens **10.** Transition element **11.** Closed test section

The dynamic pressure ( $p_{dyn}$ ) was measured using a factory calibrated KIMO Pitot-static tube, with a calibration coefficient of 1.0015 and a pressure transducer of type Setra 239, calibrated to a certified Betz micromanometer.  $F_L$  and  $F_D$  were measured with three load cells (type: Emalog CZL-608), two in the vertical and one in the horizontal directions. The cells were calibrated with weights before the measurements. The signals from the cells were amplified with an Emalog FD-3 load cell amplifier. The pressure and force data were collected using the Pressure & Force measurement software (developed in-house), through an NI BNC-2110 shielded connector block and an NI PCI-6036E data acquisition card. The chord,  $c$ , and span,  $s$ , have been measured using a vernier caliper. A three-hole probe served for determining the inflow direction into the test section. The three-hole probe was preliminarily calibrated in a free jet generated by a calibrator nozzle installed in a calibration wind tunnel. The probe was mounted in the middle of the test

section, in its vertical symmetry plane, i.e. at midspan location of the blade profiles. The angle of attack,  $\alpha$ , has been defined between the aforementioned inflow direction and the chord line. In order to make possible a direct comparison with the results in [9], the method of  $\alpha$ -setting in [9] has been applied herein.  $\alpha$  was aligned manually, with the use of the built-in protractor. The calculation of the reference area,  $A$ , and the lift,  $C_L$ , and drag,  $C_D$ , coefficients are shown in Equations (6) and (7). As  $C_L$  and  $C_D$  are functions of the angle of attack, an uncertainty due to the  $\alpha$  setting was calculated from the derivative of the measured values, and was included in the estimation of overall absolute uncertainty,  $U_{CL}$  and  $U_{CD}$  of the quantities.

$$A = c \cdot s \quad (6)$$

$$C_{L,D} = \frac{F_{L,D}}{p_{dyn} \cdot A} \quad (7)$$

The following main uncertainty sources were identified and quantified: uncertainty in the alignment of  $\alpha$ , force measurement, pressure measurement, and measurement of the geometric dimensions of the profiles.

The maximum uncertainties of the experiment-based quantities were calculated with 95% confidence level. The absolute uncertainties  $U_{CL}$  and  $U_{CD}$  were estimated from the measured values in accordance with the method in [20]. The uncertainty of experimentally determined quantities are presented in Table 1.

Table 1. Estimation of average uncertainties over the full ranges of investigation

Absolute uncertainty	Unit	Magnitude
$U_F^*$	$N$	$\pm 6 \cdot 10^{-3}$
$U_{p_{dyn}}$	$Pa$	$\pm 5 \cdot 10^{-1}$
$U_c$	$m$	$\pm 1 \cdot 10^{-4}$
$U_s$	$m$	$\pm 1 \cdot 10^{-4}$
$U_\alpha$	$deg$	$\pm 5 \cdot 10^{-1}$
$U_{CL}^{**}$	-	$\pm 6 \cdot 10^{-2}$
$U_{CD}^{**}$	-	$\pm 1.5 \cdot 10^{-2}$
$U_{CL}$	-	$\pm 7 \cdot 10^{-2}$
$U_{CD}$	-	$\pm 2 \cdot 10^{-2}$

\* Due to the uncertainty of force measurement

\*\* Due to the uncertainty of  $\alpha$  setting

### 3) INVESTIGATED PROFILES OF THE CASE STUDY

Three basic profiles were selected for investigation: a flat plate, a cambered plate, and a RAF6-E airfoil, which will be termed as “flat”, “cambered” and “airfoil”, respectively. The cross-sections of the profiles are shown in Figure 2. The details of the geometrical data are summarized in Table 2. The experiments carried out by the authors have been designed incorporating profiles of  $s/c = 1.50$ , in order to enable a comparison with detailed aerodynamic data presented in [9].

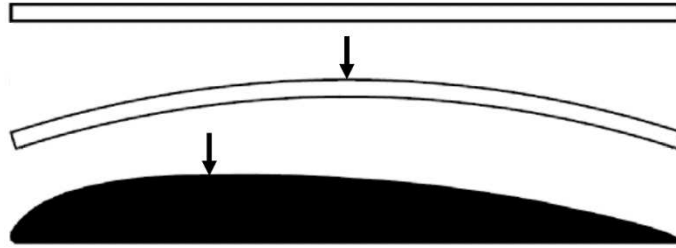


Figure 2. Cross-sections of the profiles [7]. Flat (top), cambered (middle), airfoil (bottom). The arrows indicate the locations of the maximum height of the camber line,  $d$ .

The RAF6-E [16] was chosen for the profiled “airfoil”, as it has been widely used in low-speed axial fan design. Its popularity is due to its plain pressure surface, which allows easy manufacturing. A sheet metal plate, of 8% relative curvature, with a circular-arc camber line, was chosen as “cambered” profile. According to [16], for the “cambered” profile the maximum  $C_L$  is  $\approx 1.6$ , while for the “airfoil” profile the maximum  $C_L$  is approximately 1.4. The maximum achievable lift coefficient using the “cambered” profile exceeds that of the “airfoil”. Therefore, the lift of the “cambered” profile is competitive with that of the “airfoil” in the design of axial fans of increased specific performance, while it offers simplification in manufacturing. The “flat” profile was also investigated in addition to the aforementioned profiles, as it serves as an aerodynamic and aeroacoustic reference case, e.g. [9][16].

The comparative characteristics of the profiles are given in Table 3. For the cases from references [7][9], the aspect ratio (AR) is 1.5. For the cases from [16], the AR can be considered infinite, since the measurement data was corrected to represent an infinite AR.

Table 2. Geometrical data of the profiles

Profile	$c$ [mm]	$s$ [mm]	$t$ [mm]	$d$ [mm]
Flat	100	150	2.5	0
Cambered	100	150	2	8
Airfoil	100	150	10*	5
*maximum thickness				

In order to simplify the description of the measurement cases, the following code system is established. A profile code is introduced, which describes the TE and LE geometry. The code **E** stands for the measurements in [9], since the measured profile had **E**lliptical LE and tapered TE. The code **R** stands for the profiles measured in [16], since those had **R**ounded LE and TE. The code **B** stands for the flat and cambered plates [7] presented herein, since the LE and the TE of these are **B**lunt. The code **A** stands for the **A**irfoil. Since the profile geometry is the same for the current measurements as in the literature, the new measurements are denoted by **A**'. The next parameter considered in the coding system for the profiles is the percent of camber. For the 0% (flat plate), 4% and 8% camber, the following codes are used respectively: C0, C4 and C8. To distinguish between the measurement cases, a code for the chord based  $Re$  is also applied. Measurements carried out at  $Re = x$  times  $10^5$  are indicated with "Rex". For instance the measurement case E\_C4\_Re1.4 stands for a cambered plate from [9], which has an elliptical LE and tapered TE, has 4% camber, and was measured at  $Re = 1.4 \cdot 10^5$ .



Table 3. Geometry of the compared profiles

Code	Profile	Camber	LE geom.	TE geom.	Reference	t/c
E_C0	Flat	0%	Elliptical	Tapered	[9]	0,019
R_C0	Flat	0%	Rounded	Rounded	[16]	0,020
B_C0	Flat	0%	Blunt	Blunt	[7]	0,025
E_C4	Cambered	4%	Elliptical	Tapered	[9]	0,020
R_C4	Cambered	4%	Rounded	Rounded	[16]	0,020
R_C8	Cambered	8%	Rounded	Rounded	[16]	0,020
B_C8	Cambered	8%	Blunt	Blunt	[7]	0,020
A_C0	RAF6-E	n/a	Rounded	Rounded	[16]	0,100*
A'_C0	RAF6-E	n/a	Rounded	Rounded	[7]	0,100*

\* Calculated with maximum thickness

As suggested in [9], the gaps between the two endwalls and the model are to be less than  $0.005 s$ , in order to avoid any significant impact on the measurement results. This requirement is fulfilled in the present measurements, with  $0.5 \text{ mm}$  ( $\approx 0.003 s$ ) gaps being realized. In [9], the case studies on models of  $s/c = 1.50$  equipped with two endplates, were referred to as two-dimensional (2D). This implies that an experiment designed with

$s/c = 1.50$ , two endwalls and the appropriate tip gap, as presented in [9], can be approximated as a 2D aerodynamic case.

The plate blades presented in [9] and [16] have a relative thickness,  $t/c$ , of 0.02. The maximum relative thickness for the plates presented herein is 0.025. Based on [21], 1% change in  $t/c$  causes a change in the lift curve slope in the order of magnitude of  $10^{-3}$ . Consequently, a 5% change in thickness causes a  $5 \cdot 10^{-3}$  change in the lift curve, which is one order of magnitude smaller than the estimated absolute error,  $U_{CL}$ . On this basis, the effect of various relative plate thicknesses in the comparative (both flat and cambered) case studies is neglected herein.

#### **4) RESULTS AND DISCUSSION**

As discussed in [9], the interaction between the boundary layer growing on the endwalls and the flow around the wing tends to reduce the lift and increase the drag, especially at moderate Reynolds numbers. Such effect is termed herein as the “endwall effect”. [16] states that the data in this reference are corrected to infinite AR, thus eliminating the endwall effect. Nevertheless, the endwall effect has been left uncorrected both for the data in [9] and for the own measurements, with the intention of directly presenting the results of the experiments. In order to judge the significance of the endwall effect for the flat plate and the 4% cambered plate cases, the data from [16] is compared to [9]. For the 8% cambered plate and the airfoil cases, the data from [16] is compared to the own measurements. The comparisons focus on whether the lift decreases and / or the drag

increases due to the endwall effect. Such comparisons suggest the following trends. For the flat plate, the endwall effect appears to be insignificant (within the experimental uncertainty) within the low-load range. The endwall effect tends to become more pronounced toward higher camber (flat → 4% cambered → 8% cambered plates) and / or toward higher  $\alpha$  values and always for the airfoil profile. Therefore, the models reported in [9] and in the own experiments can be considered as approximations of 2D flow cases only being aware to the occasionally pronounced endwall effect, in terms of  $C_L$  and / or  $C_D$ .

Figure 3. shows the normalised LDR values for the investigated cases. Each data series is normalised with its maximum value. The aforementioned endwall effect results in a reduction of LDR, seen by comparing the data from [16], [9] and the present measurements. Taking the  $LDR_{max}$  values at  $Re$  closest to  $10^5$  as representative indicators, the following reduction of  $LDR_{max}$  is observed for the own measurements, relative to the data from [16]. "Flat": R\_C0\_Re3,0 ---> B\_C0\_Re1,0: 50% reduction. "Cambered": R\_C8\_Re3,0 ---> B\_C8\_Re1,0: 70% reduction. "Airfoil": A\_Re3,1 ---> A'\_Re1,0: 90% reduction.

For a systematic and comprehensive evaluation of the results, the ranges of incidence angle are uniformly categorised on the basis of Figure 3., and labelled for each presented data curve as follows:

$0^\circ \leq \alpha \leq 4^\circ$ : this range is labelled as the *low-load range*. The upper limit of this range,  $\alpha = 4^\circ$ , is an overall, approximate representation of the state of maximum LDR for each case (literature data as well as own measurements) discussed herein. Therefore, if *high total efficiency* is an aim of the fan design, then the blade sections should be designed to operate near the upper limit of the *low-load range*, corresponding to maximum LDR.

$4^\circ < \alpha \leq 10^\circ$ : this range is labelled as the *high-load range*. The upper limit,  $\alpha = 10^\circ$ , is an overall representation for maximum  $C_L$  for each case discussed herein. Therefore, if *high specific performance* is an aim of the fan blade section design, by utilizing the maximum available lift, the blade sections are to be designed to operate near the upper limit of the *high-load range*.

$10^\circ < \alpha \leq 20^\circ$ : this range is labelled as the *overload range*. This range forms a transition from partly stalled state toward deep stall. Such operational range is undesirable and occurs at highly throttled fan states.

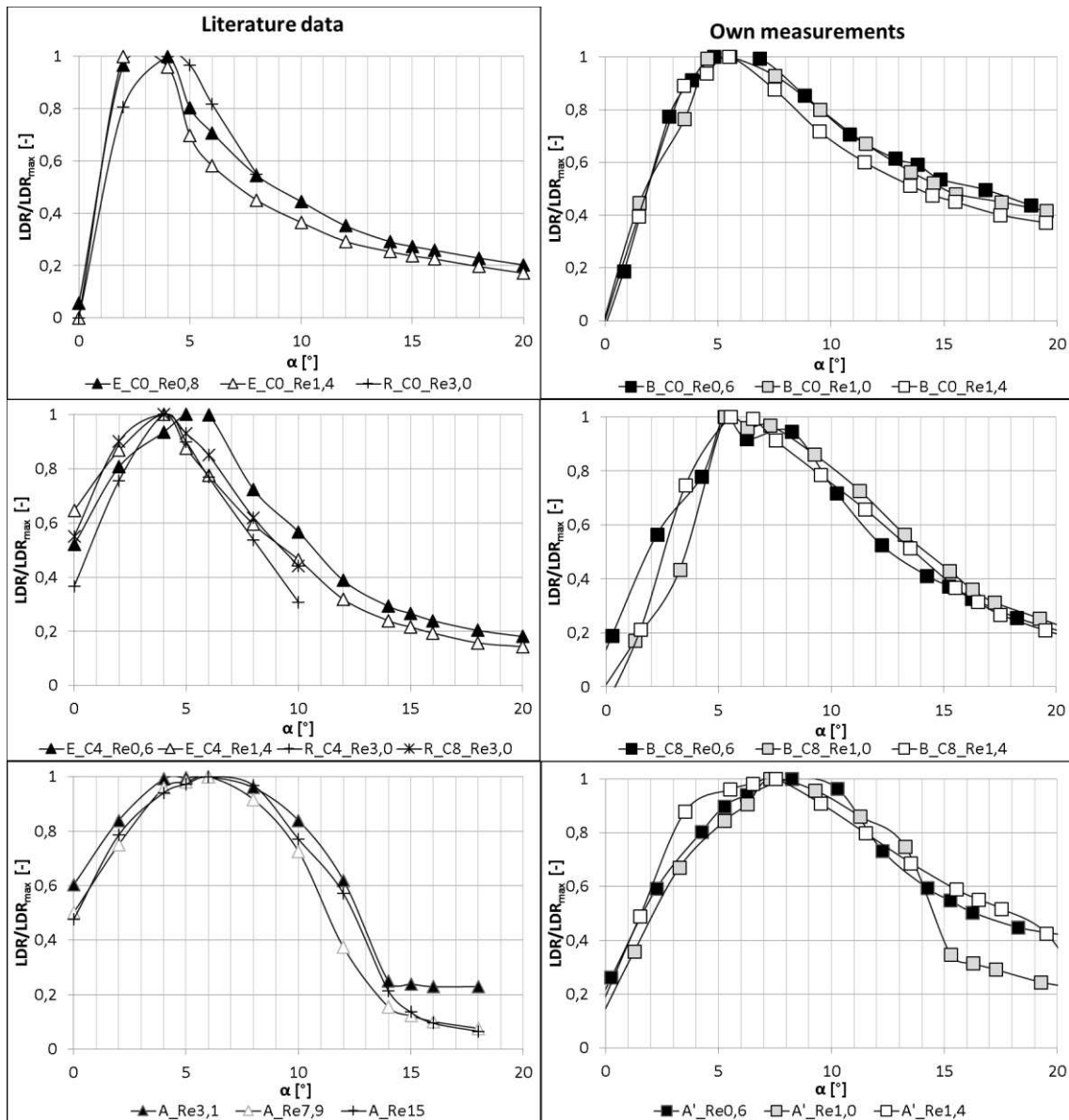


Figure 3. Normalised LDRs as a function of  $\alpha$ .

According to their design relevance, the discussion focusses on the low-load and high-load ranges. The measurement data are also presented and briefly commented on, for the

overload range. In the following section the results of the force measurements are presented for each profile geometry in comparison with literature data.

**Flat plate (Figure 4.)**

**Lift coefficient**

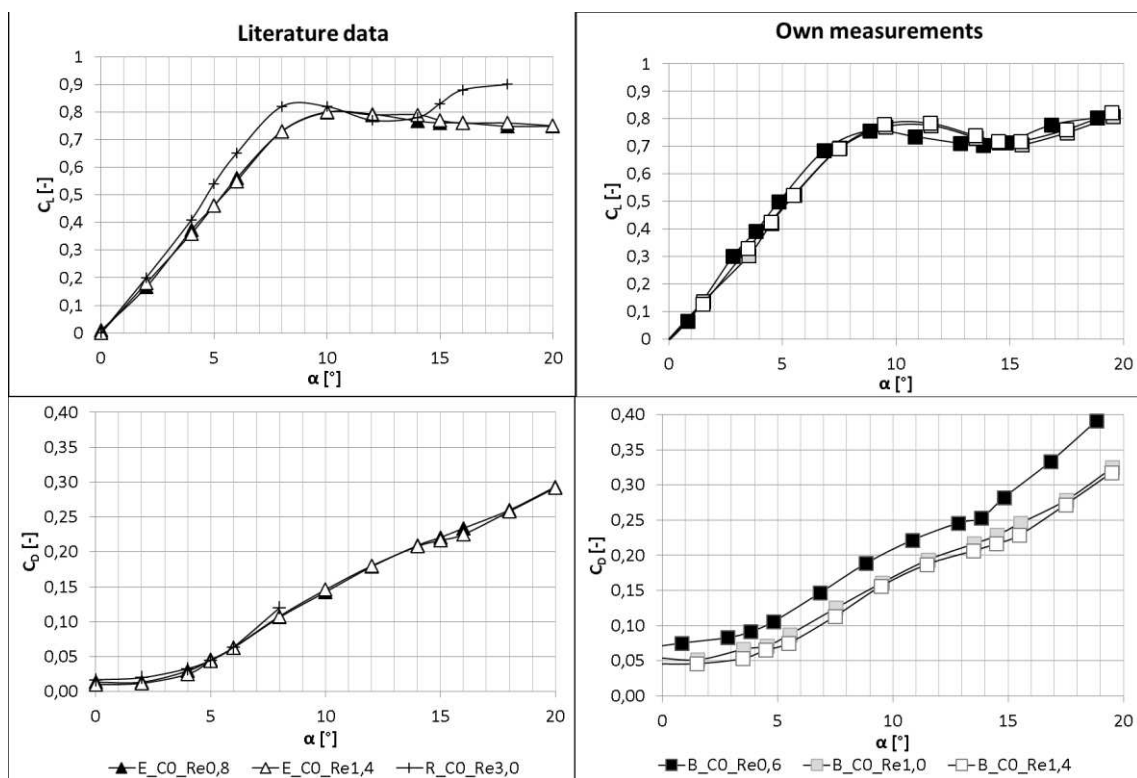


Figure 4. Lift and drag coefficients as a function of  $\alpha$  for the flat plates

For both of the low-load and high-load ranges, the lift curves of the blunt LE cases (B\_C0\_Re0,6; B\_C0\_Re1,0; B\_C0\_Re1,4) agree fairly well with those of the elliptical LE cases (E\_C0\_Re0,8 and E\_C0\_Re1,4). The maximum  $C_L \approx 0.8$  occurs at  $\alpha \approx 10^\circ$  for

each case. Therefore, the bluntness of the LE does not appear to deteriorate the lift on the flat plate.

For the blunt cases no definite trend can be observed for the effect of  $Re$  on  $C_L$ . For both the low-load and high-load ranges, the change in  $C_L$  is confined within the experimental uncertainty for the range of  $Re$  between  $6 \cdot 10^4$  and  $1.4 \cdot 10^5$ . Therefore, the lift appears to be insensitive to the Reynolds number. This observation is in agreement with the flat plate measurements in [9].

### **Drag coefficient**

The bluntness of the LE introduces significant additional drag, especially in the low-load range. At higher Reynolds numbers, this additional drag tends to decrease as  $\alpha$  increases. For the blunt cases  $C_D$  tends to increase as  $Re$  decreases, corresponding to the trend established in [9]. A comparatively large increase in  $C_D$  can be observed when the Reynolds number decreases from  $1 \cdot 10^5$  to  $6 \cdot 10^4$ .

### ***Cambered plate (Figure 5.)***

#### **Lift coefficient**

The lift curve values for the R\_C8\_Re3,0 [16] case are significantly higher than those for the own measurements (B\_C8\_Re0,6; B\_C8\_Re1,0; B\_C8\_Re1,4). The possible reasons include the endwall effect, and/or the effect of LE bluntness. Such effects appear to be pronounced within the low-load range. For example, at  $\alpha = 5^\circ$ ,  $C_L$  for the R\_C8 [16] case

and for the own measurement cases is  $\approx 1.2$  and  $1.0$ , respectively. However, for  $\alpha = 0^\circ$ , these respective values are  $\approx 0.8$  and  $0.2$ .

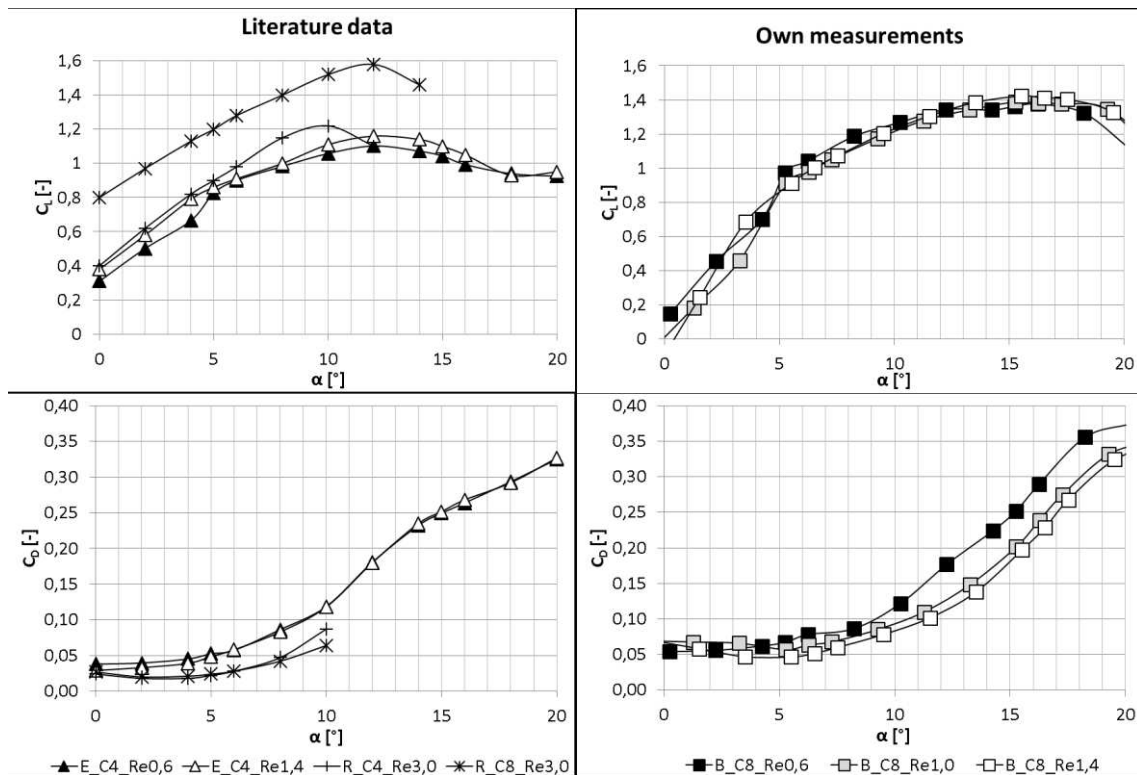


Figure 5. Lift and drag coefficients as a function of  $\alpha$  for the cambered plates

For the elliptical cases the reduction of  $Re$  tends to deteriorate  $C_L$ . Such behaviour is in accordance with the observation in [9]. The deterioration is pronounced within the low-load range. For the blunt cases, such as for the flat plate, no definite trend can be observed for the effect of  $Re$  on  $C_L$ ; the lift tends to be insensitive to the Reynolds number. For the high-load range, the change in  $C_L$  is confined within the experimental uncertainty for the range of  $Re$  between  $6 \cdot 10^4$  and  $1.4 \cdot 10^5$ .



### **Drag coefficient**

Based on [9], it is expected that the increase of camber tends to increase the drag. In comparison of the E\_C4 and the B\_C8 cases, the increase of drag is confined to the low-load range. Such increase of drag can be attributed to the twofold effect of a) increased camber, and b) LE bluntness. The drag-increasing effect of LE bluntness for the low-load range has also been observed for the flat plate case. For higher  $\alpha$  values, the increase of drag due to increased camber and / or LE bluntness is not characteristic.

For the elliptical cases  $C_D$  tends to increase as  $Re$  decreases, corresponding to the trend established in [9]. Such effect appears within the low-load range but is not characteristic for larger angles. For the blunt cases, such as for the flat plate,  $C_D$  tends to increase as  $Re$  decreases, corresponding to the trend established in [9].

### ***Airfoil (Figure 6.)***

#### **Lift coefficient**

In the case of own measurements, within the investigated Reynolds number range, the lift appears to be insensitive to the Reynolds number, such as for the flat plate and cambered plate cases. The lift variation is within the experimental uncertainty for both of the low-load and high-load ranges. The lift increases with the Reynolds number in the overload range only.

## Drag coefficient

In the case of own measurements the reduction of  $Re$  tends to drastically increase  $C_D$ . The increase is especially pronounced when the Reynolds number decreases from  $1 \cdot 10^5$  to  $6 \cdot 10^4$ . At such low Reynolds number, the drag of the airfoil exceeds that of the 8% cambered blade over the entire range of  $0^\circ \leq \alpha \leq 20^\circ$ . This observation is in accordance with [10].

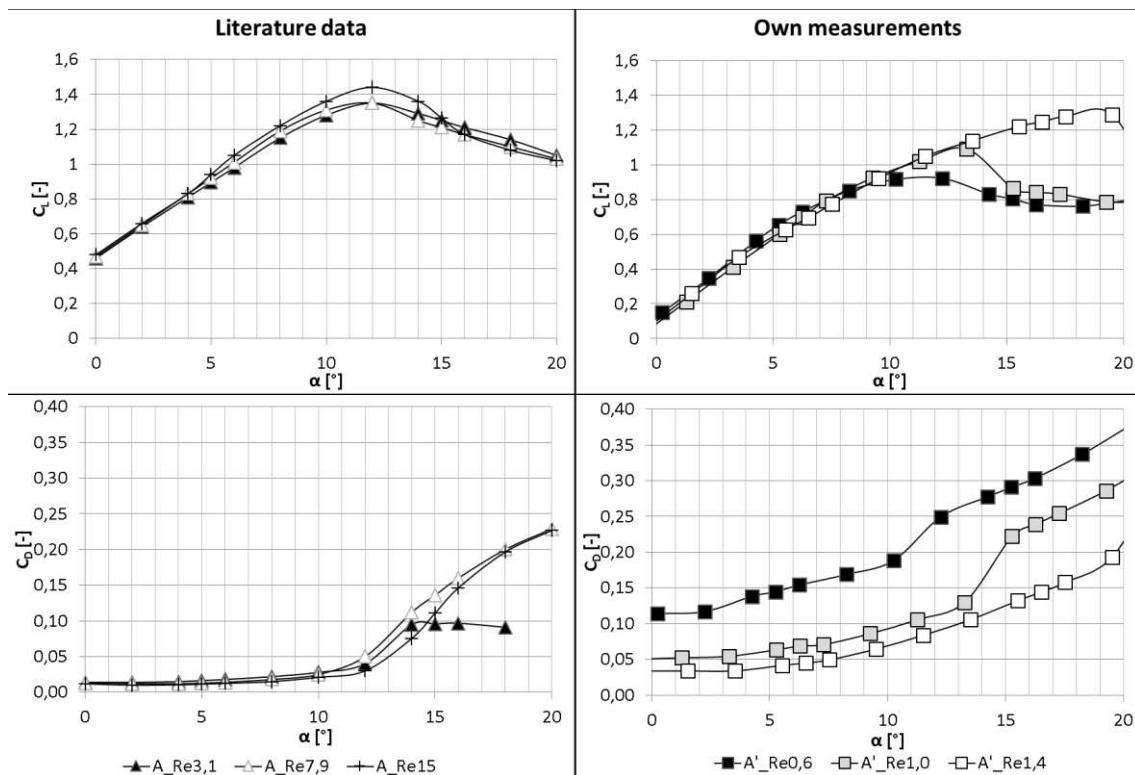


Figure 6. Lift and drag coefficients as a function of  $\alpha$  for the airfoils

## 5) SUMMARY AND FUTURE REMARKS

Based on the results above, the following trends can be stated for each geometry. The results are also summarized in [Table 3](#).

### *Flat plate*

In case of a non-blunt LE, both  $C_L$  and  $C_D$  are found to be insensitive to decreasing the  $Re$  to  $Re < 10^5$ , for both of the low-load ( $0^\circ \leq \alpha \leq 4^\circ$ ) and the high-load ( $4^\circ < \alpha \leq 10^\circ$ ) range. [Comparative cases: E\_C0\_Re1,4  $\rightarrow$  E\_C0\_Re0,10]

At the representative intermediate Reynolds number of  $Re = 10^5$ , blunting the LE was found to leave  $C_L$  practically unchanged, for both the low-load and high-load ranges. Blunting the LE caused an increase in  $C_D$  in the low-load range only. [Comparative cases: E\_C0\_Re1,4 and E\_C0\_Re0,8  $\rightarrow$  B\_C0\_Re1,0]

For the blunt LE case, decreasing the Reynolds number to  $Re < 10^5$  did not significantly affect  $C_L$  but caused a large increase in  $C_D$  for both the low-load and high-load range. [Comparative cases: B\_C0\_Re1,4  $\rightarrow$  B\_C0\_Re1,0  $\rightarrow$  B\_C0\_Re0,8]

### *Cambered plate*

In case of the 4% cambered plate of non-blunt LE, decreasing the Reynolds number to  $Re < 10^5$  caused a deterioration of  $C_L$  and increase of  $C_D$  in the low-load range. However,

insignificant changes were observed for both  $C_L$  and  $C_D$ , due to decreasing  $Re$  for the high-load range. [Comparative cases: E\_C4\_Re1,4  $\rightarrow$  E\_C4\_Re0,8]

For the 8% cambered plate of non-blunt LE, the only reference available in the literature is the R\_C8\_Re3,0 case. The diagrams in [9] suggest that, the Reynolds number effect on  $C_L$  is moderate at  $Re > 1,4 \cdot 10^5$ . Furthermore, as stated before, the endwall effect is pronounced toward higher  $\alpha$  and lower  $Re$  values. The blunt LE cases (B\_C8) show a significant deterioration in  $C_L$  and increase in  $C_D$  for the low-load range. Based on the above, this is attributed to introducing LE bluntness. For the high-load range, the change in  $C_L$  due to blunting the LE appear to be attenuated at higher Reynolds numbers, in comparison to the low-load range: the lift curve slope for the blunt-LE case is similar to that of the non-blunt case. However, the increase of  $C_D$  is observable in the high-load range. [Comparative cases: R\_C8\_Re3,0  $\rightarrow$  B\_C8\_Re1,0]

For the blunt LE case, decreasing the Reynolds number to  $Re < 10^5$  did not characteristically affect  $C_L$ . However, it caused a remarkable increase in  $C_D$ , for the high-load range. [Comparative cases: B\_C8\_Re1,4  $\rightarrow$  B\_C8\_Re1,0  $\rightarrow$  B\_C8\_Re0,8]

### ***Airfoil***

$C_L$  appears to be insensitive to decreasing  $Re$ . However, a large increase is observed in  $C_D$ . Such increase is much more significant for the airfoil than for the cambered plate. [Comparative cases: A\_Re1,4  $\rightarrow$  A\_Re1,0  $\rightarrow$  A\_Re0,8]

**Table 3.** Summary of the trends

<b>FLAT PLATE</b>		<b>Low-load range</b> $0^\circ \leq \alpha \leq 4^\circ$		<b>High-load range</b> $4^\circ < \alpha \leq 10^\circ$	
<b>LE + its modification</b>	<b>Re + its modification</b>	$C_L$	$C_D$	$C_L$	$C_D$
Non-blunt LE	Decreasing $Re$ : $Re < 10^5$	—	—	—	—
Blunting the LE	@ $Re = 10^5$	—	↑	—	—
	Decreasing $Re$ : $Re < 10^5$	—	↑	—	↑

<b>CAMBERED PLATES</b>		<b>Low-load range</b> $0^\circ \leq \alpha \leq 4^\circ$		<b>High-load range</b> $4^\circ < \alpha \leq 10^\circ$	
<b>LE + its modification</b>	<b>Re + its modification</b>	$C_L$	$C_D$	$C_L$	$C_D$
Non-blunt LE	Decreasing $Re$ : $Re < 10^5$	↓	↑	—	—
Blunting the LE	@ $Re = 10^5$	↓	↑	—	↑
	Decreasing $Re$ : $Re < 10^5$	—	—	—	↑

AIRFOIL		Low-load range $0^\circ \leq \alpha \leq 4^\circ$		High-load range $4^\circ < \alpha \leq 10^\circ$	
LE	<i>Re</i> + its modification	$C_L$	$C_D$	$C_L$	$C_D$
Non-blunt LE	Decreasing <i>Re</i> : $Re < 10^5$	—	↑	—	↑

**Key:**

— Insensitive

↑ Increase

↓ Decrease

The trends discussed above allow for the following qualitative guidelines in preliminary design of axial fan blades.

- For  $Re < 10^5$  applications, cambered plate profiles can be superior to airfoil profiles in terms of aerodynamic efficiency, especially in the high-load range. The reason is that the increase of drag, due to decreasing *Re*, is moderate for cambered plate profiles, in comparison to airfoil profiles, without a significant deterioration of lift.
- For low-*Re* applications, leaving the LE of cambered plates blunt tends to be uncritical in the high-load range but is critical in the low-load range.

## **CONFLICT OF INTEREST**

The Authors declare that there is no conflict of interest.

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