

Combustion Kinetics of Biomass Materials in the Kinetic Regime

Energy Fuels, **2012**, 26, 1323-1335. doi: [10.1021/ef201497k](https://doi.org/10.1021/ef201497k)

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Keywords: Wheat straw, willow; wood; sewage sludge; thermogravimetry; distributed activation energy model; combustion; char burn-off; pyrolysis; kinetic regime.

Scope of this document: The kinetic evaluation was illustrated by two experiments for each sample in the figures of our article. **Figures S1 - S6** of the present *Supporting Information* show series of 10 experiments that were evaluated simultaneously. Besides, details are given on the autocatalytic (self-accelerating) kinetics of the oxidative decomposition of the cellulose in the wood sample of the study in **Figure S7** and **Table S1**.

Textual information in Figures S1 - S6: The first row below each figure contains the name of the sample and a brief description of the experimental conditions. The second row lists the fit quality for the given experiment (*fit*₁) and for the whole series (*fit*₁₀). The further rows display parameters for the partial processes.

Colors and line types in Figures S1 - S6:

- oooo DTG curves normalized by the initial sample mass
- normalized mass loss rate curves calculated from the model ($-dm^{\text{calc}}/dt$)
- rate of the biomass devolatilization ($-dm_{\text{ur}}/dt$ or $c_{\text{other}} d\alpha_{\text{other}}/dt$)
- - - - rate of the cellulose devolatilization (when present in the model, $c_{\text{cell}} d\alpha_{\text{cell}}/dt$)
- rate of the char formation and/or char burn-off ($-dm_{\text{char}}/dt$ or $c_{\text{char}} d\alpha_{\text{char}}/dt$)
- xxxxx ash formation rate

The last figure (**Figure S7**) displays $f(\alpha_{\text{cell}})$ functions, where α_{cell} is the reacted fraction of the cellulose in the wood sample and $f(\alpha_{\text{cell}})$ is an empirical function describing an autocatalytic oxidative devolatilization. The notations of Figure S7 are explained in the table of parameters (**Table S1**) in the same page.

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Figure S7. $f(\alpha_{cell})$ functions 21

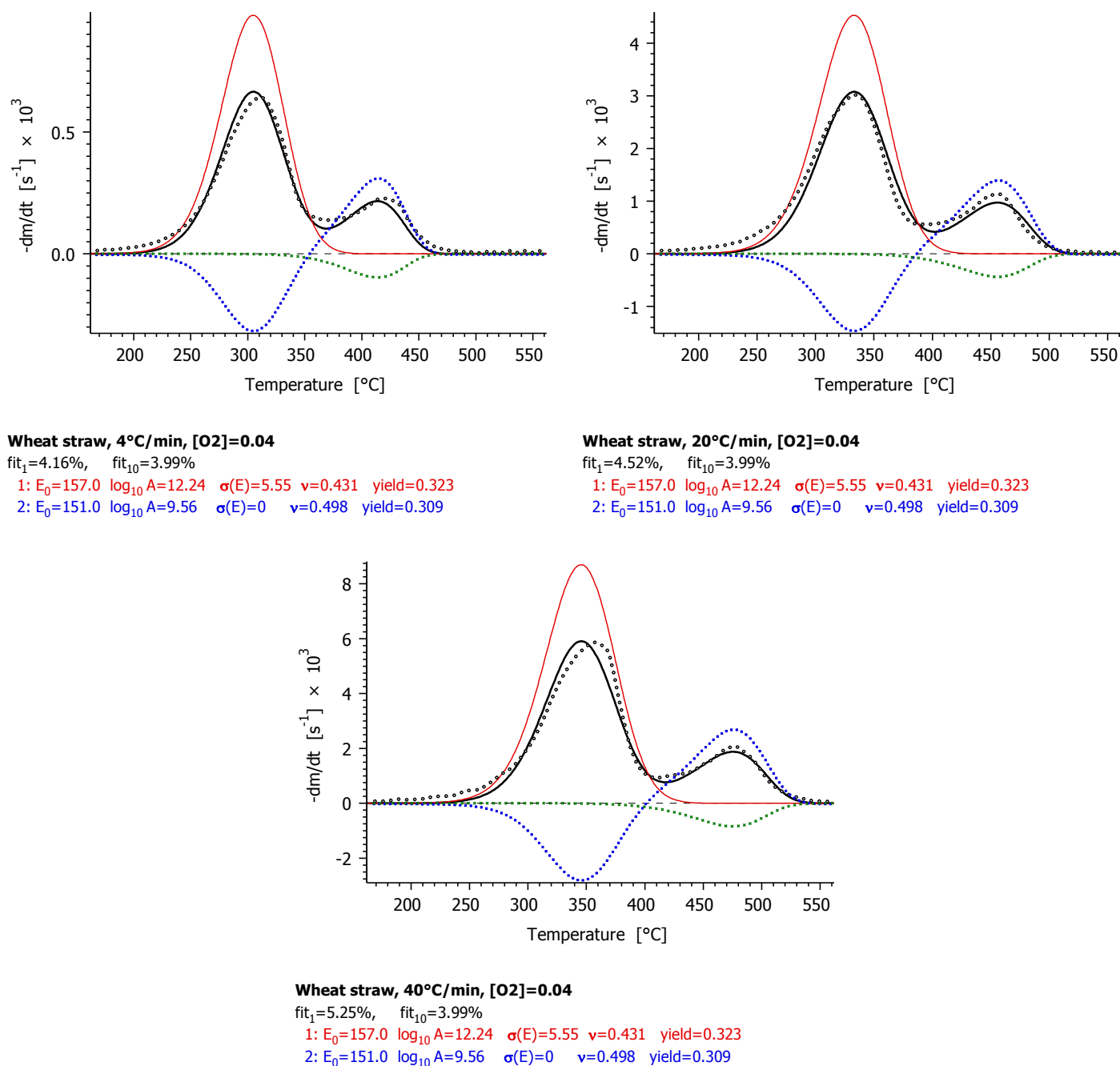
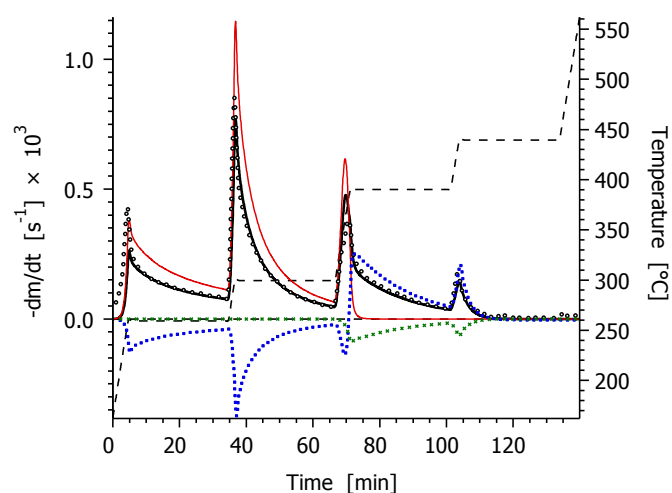
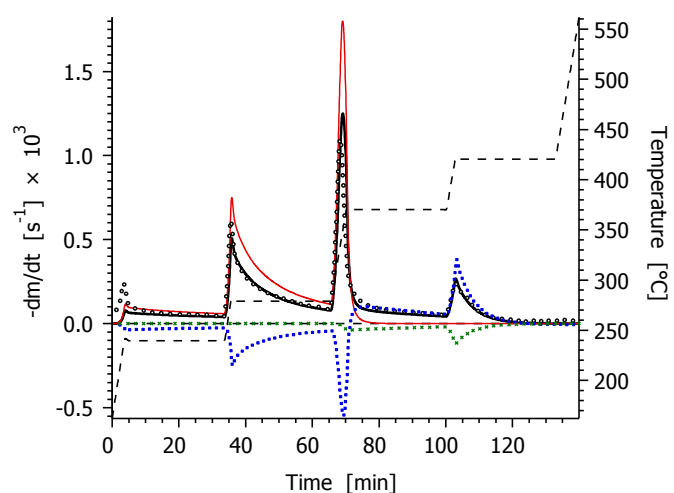


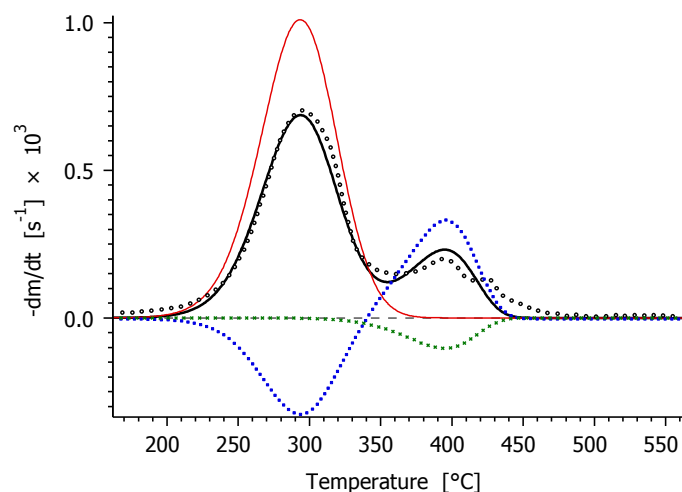
Figure S1. Evaluation of the wheat straw experiments by a model of successive devolatilization and char burn-off reactions


Wheat straw, stepwise 1, [O₂]=0.04
 $\text{fit}_1=3.95\%$, $\text{fit}_{10}=3.99\%$

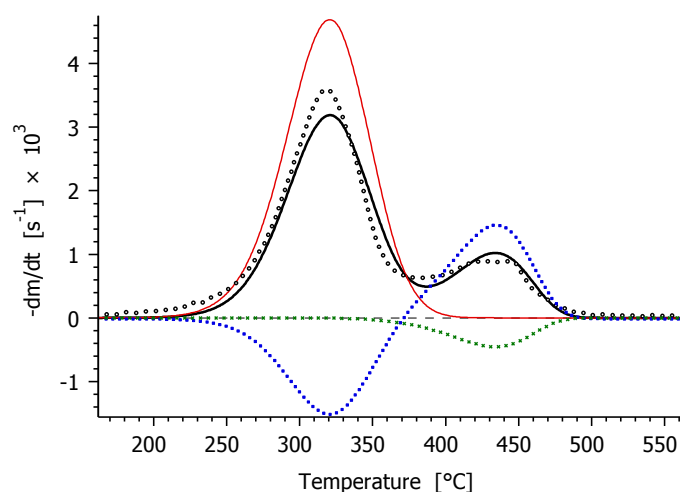
 1: $E_0=157.0$ $\log_{10} A=12.24$ $\sigma(E)=5.55$ $v=0.431$ $\text{yield}=0.323$

 2: $E_0=151.0$ $\log_{10} A=9.56$ $\sigma(E)=0$ $v=0.498$ $\text{yield}=0.309$

Wheat straw, stepwise 2, [O₂]=0.04
 $\text{fit}_1=4.01\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=157.0$ $\log_{10} A=12.24$ $\sigma(E)=5.55$ $v=0.431$ $\text{yield}=0.323$

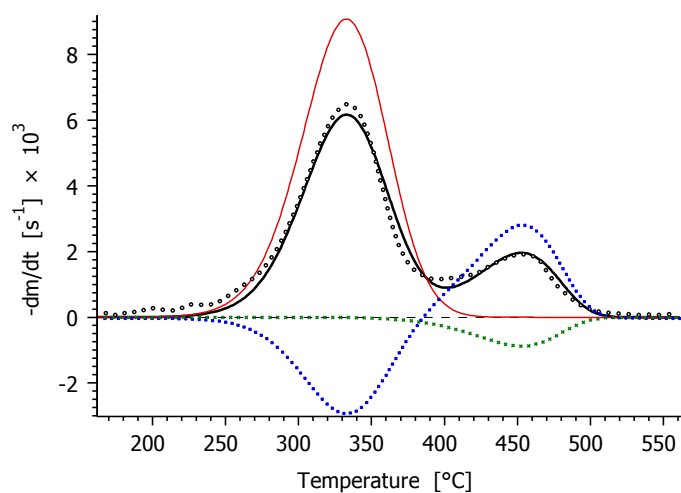
 2: $E_0=151.0$ $\log_{10} A=9.56$ $\sigma(E)=0$ $v=0.498$ $\text{yield}=0.309$

Wheat straw, 4°C/min, [O₂]=0.2
 $\text{fit}_1=4.19\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=157.0$ $\log_{10} A=12.24$ $\sigma(E)=5.55$ $v=0.431$ $\text{yield}=0.323$

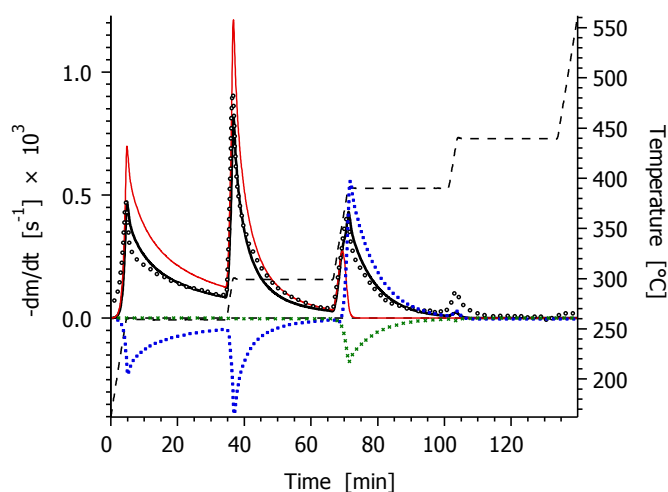
 2: $E_0=151.0$ $\log_{10} A=9.56$ $\sigma(E)=0$ $v=0.498$ $\text{yield}=0.309$

Wheat straw, 20°C/min, [O₂]=0.2
 $\text{fit}_1=3.98\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=157.0$ $\log_{10} A=12.24$ $\sigma(E)=5.55$ $v=0.431$ $\text{yield}=0.323$

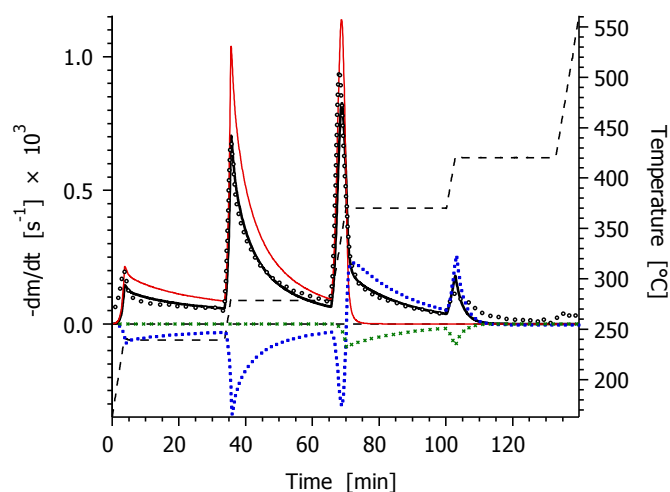
 2: $E_0=151.0$ $\log_{10} A=9.56$ $\sigma(E)=0$ $v=0.498$ $\text{yield}=0.309$
Figure S1. (Continued)


Wheat straw, 40°C/min, [O₂]=0.2
 $\text{fit}_1 = 3.02\%$, $\text{fit}_{10} = 3.99\%$

 1: $E_0 = 157.0$ $\log_{10} A = 12.24$ $\sigma(E) = 5.55$ $v = 0.431$ $\text{yield} = 0.323$

 2: $E_0 = 151.0$ $\log_{10} A = 9.56$ $\sigma(E) = 0$ $v = 0.498$ $\text{yield} = 0.309$

Wheat straw, stepwise 1, [O₂]=0.2
 $\text{fit}_1 = 3.14\%$, $\text{fit}_{10} = 3.99\%$

 1: $E_0 = 157.0$ $\log_{10} A = 12.24$ $\sigma(E) = 5.55$ $v = 0.431$ $\text{yield} = 0.323$

 2: $E_0 = 151.0$ $\log_{10} A = 9.56$ $\sigma(E) = 0$ $v = 0.498$ $\text{yield} = 0.309$

Wheat straw, stepwise 2, [O₂]=0.2
 $\text{fit}_1 = 3.15\%$, $\text{fit}_{10} = 3.99\%$

 1: $E_0 = 157.0$ $\log_{10} A = 12.24$ $\sigma(E) = 5.55$ $v = 0.431$ $\text{yield} = 0.323$

 2: $E_0 = 151.0$ $\log_{10} A = 9.56$ $\sigma(E) = 0$ $v = 0.498$ $\text{yield} = 0.309$
Figure S1. (Continued)

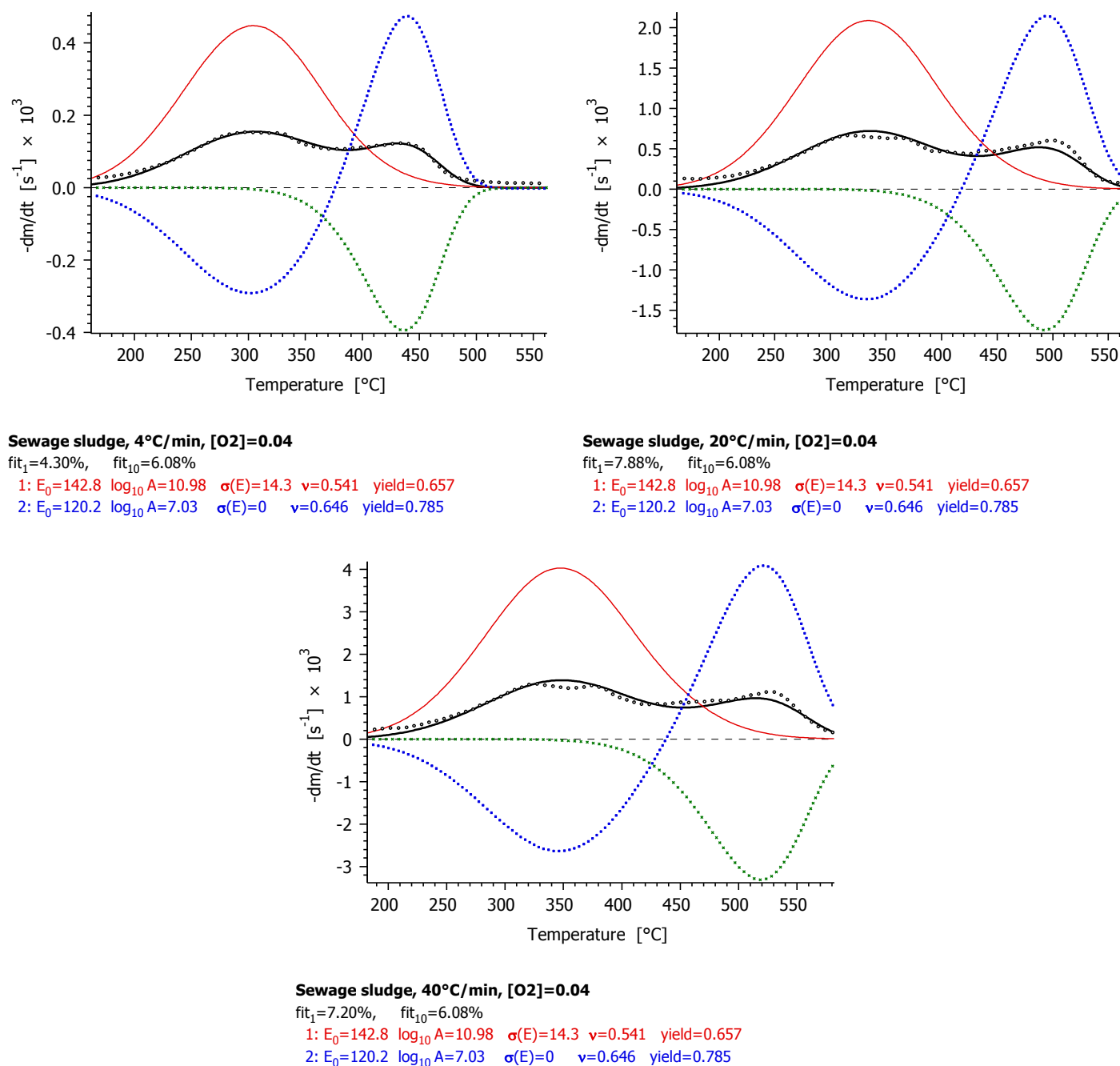
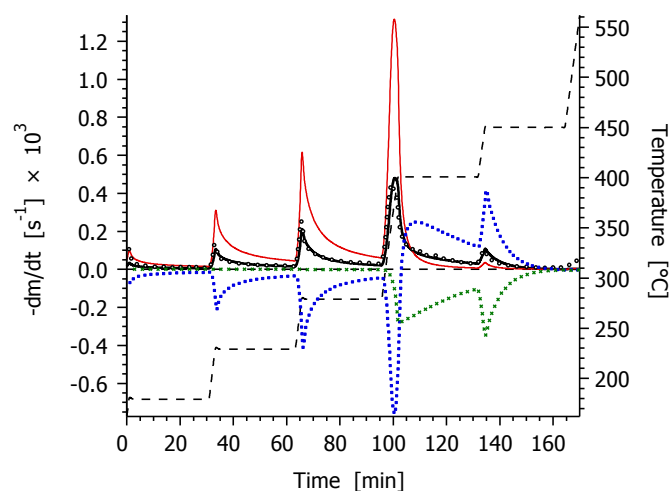
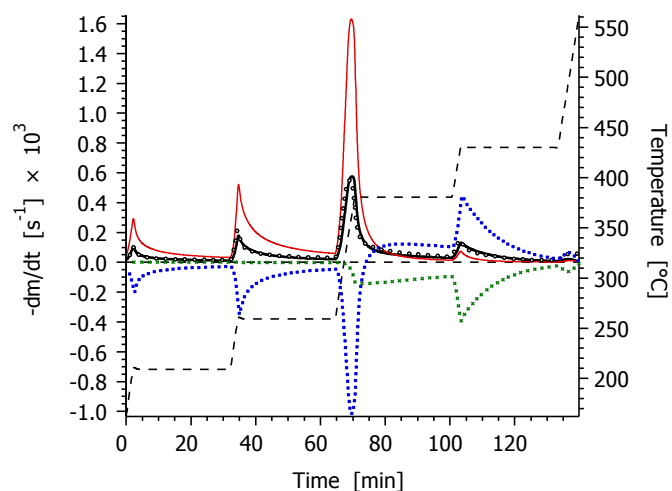


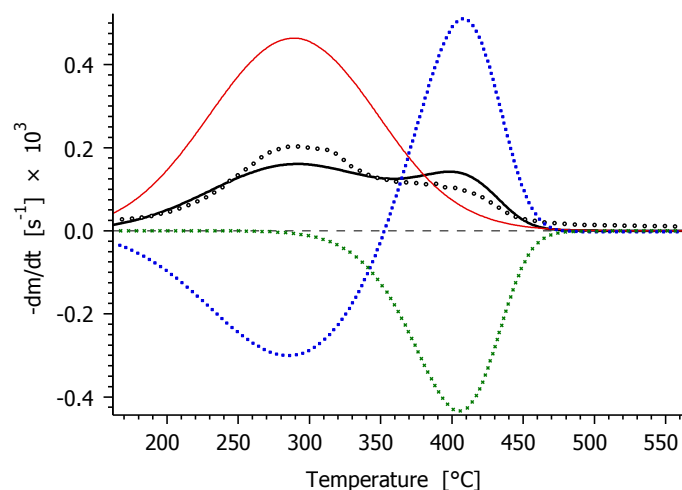
Figure S2. Evaluation of the sewage sludge experiments by a model of successive devolatilization and char burn-off reactions


Sewage sludge, stepwise 1, [O₂]=0.04
 $\text{fit}_1=3.50\%$, $\text{fit}_{10}=6.08\%$

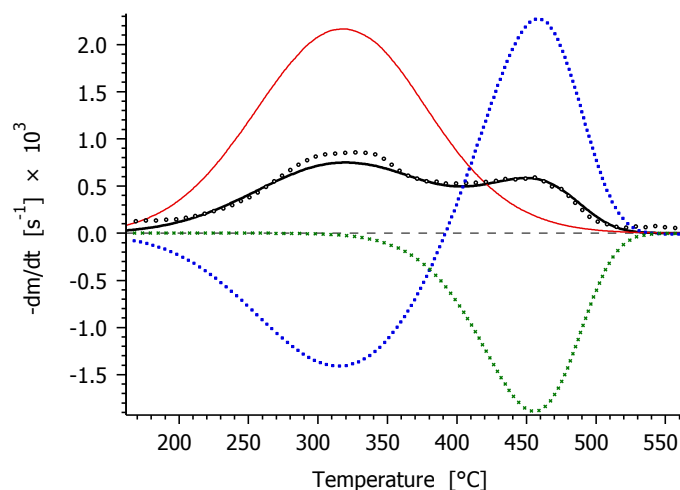
1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$


Sewage sludge, stepwise 2, [O₂]=0.04
 $\text{fit}_1=2.77\%$, $\text{fit}_{10}=6.08\%$

1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$

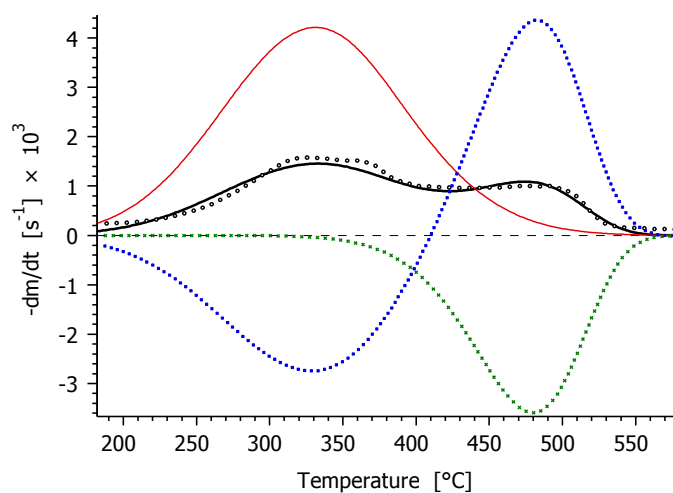

Sewage sludge, 4°C/min, [O₂]=0.2
 $\text{fit}_1=10.50\%$, $\text{fit}_{10}=6.08\%$

1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$

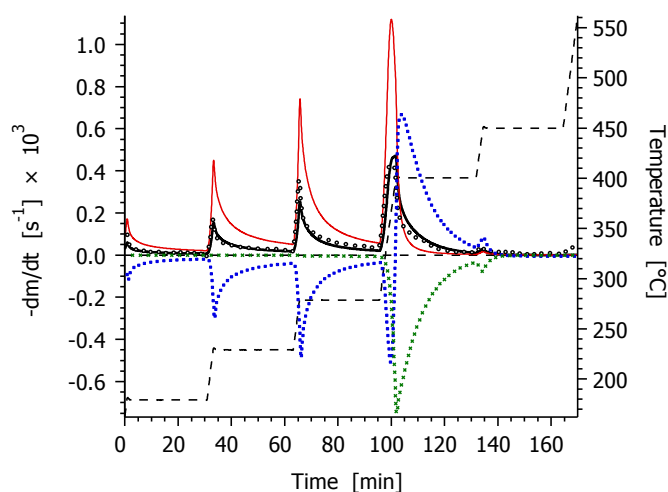

Sewage sludge, 20°C/min, [O₂]=0.2
 $\text{fit}_1=5.83\%$, $\text{fit}_{10}=6.08\%$

1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$

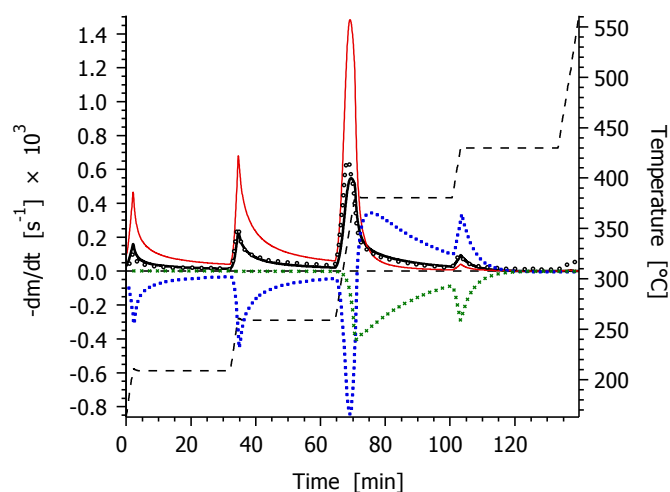
Figure S2. (Continued)


Sewage sludge, 40°C/min, [O₂]=0.2
 $\text{fit}_1=5.86\%$, $\text{fit}_{10}=6.08\%$

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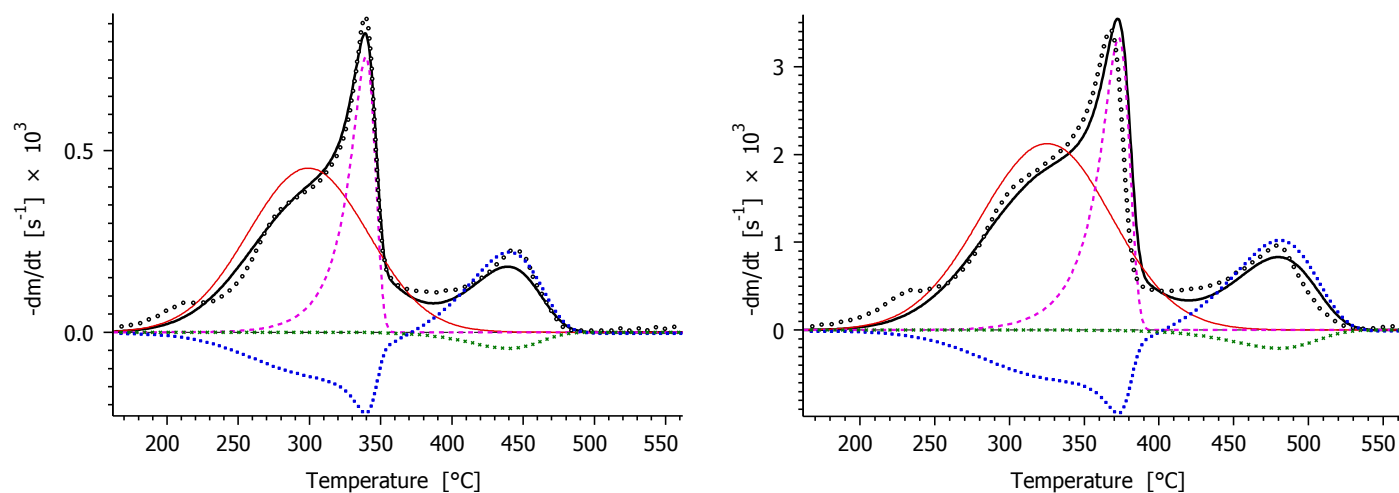
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$

Sewage sludge, stepwise 1, [O₂]=0.2
 $\text{fit}_1=4.95\%$, $\text{fit}_{10}=6.08\%$

 1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$

 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$

Sewage sludge, stepwise 2, [O₂]=0.2
 $\text{fit}_1=3.68\%$, $\text{fit}_{10}=6.08\%$

 1: $E_0=142.8$ $\log_{10} A=10.98$ $\sigma(E)=14.3$ $v=0.541$ $\text{yield}=0.657$

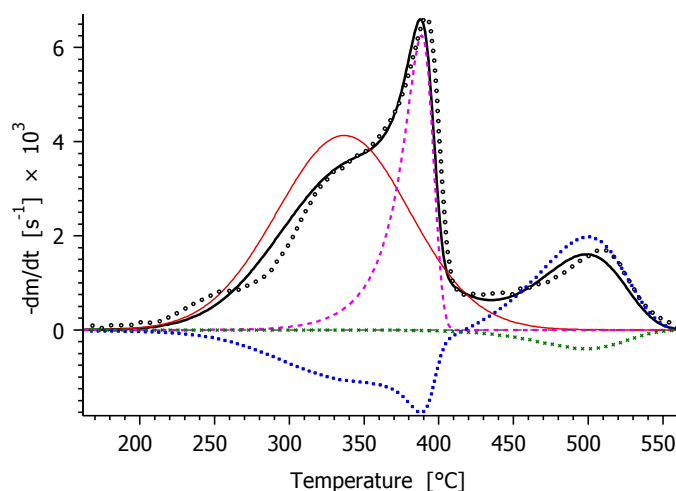
 2: $E_0=120.2$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ $\text{yield}=0.785$
Figure S2. (Continued)

**Willow, 4°C/min, [O₂]=0.04**fit₁=2.58%, fit₁₀=4.21%

1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

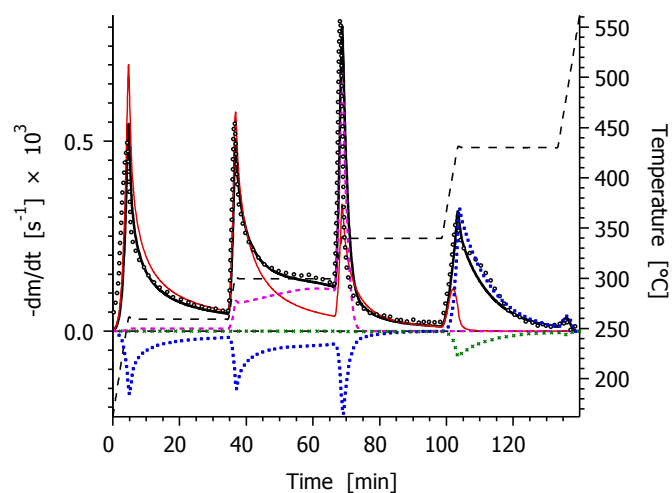
Willow, 20°C/min, [O₂]=0.04fit₁=6.15%, fit₁₀=4.21%

1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

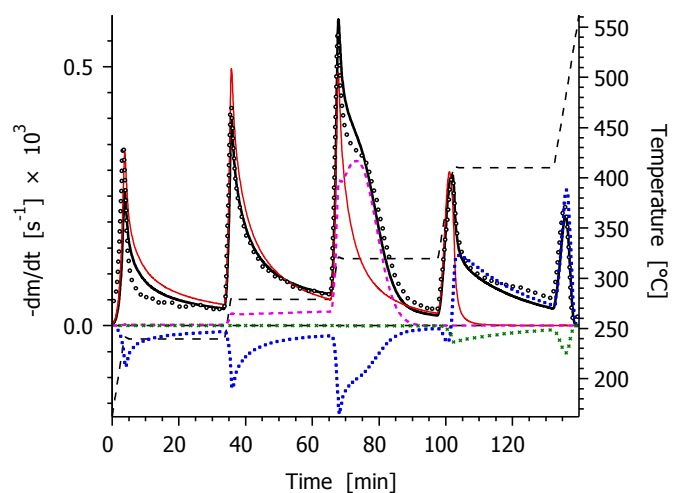
**Willow, 40°C/min, [O₂]=0.04**fit₁=5.65%, fit₁₀=4.21%

1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

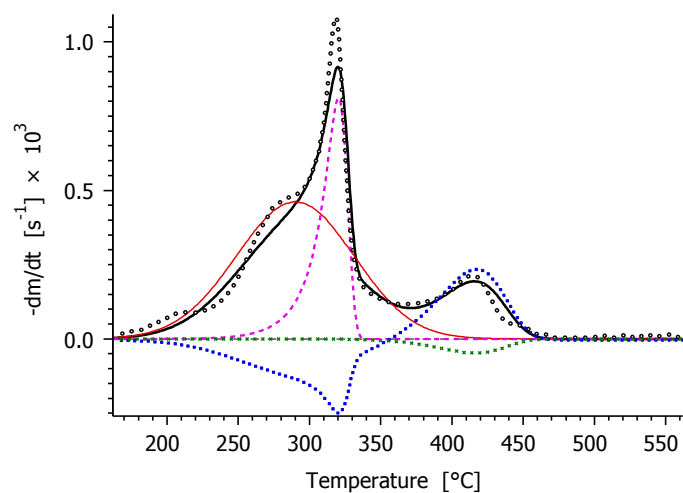
Figure S3. Evaluation of the willow experiments assuming two devolatilization reactions and a successive devolatilization and char burn-off

**Willow, stepwise 1, [O2]=0.04**fit₁=4.64%, fit₁₀=4.21%

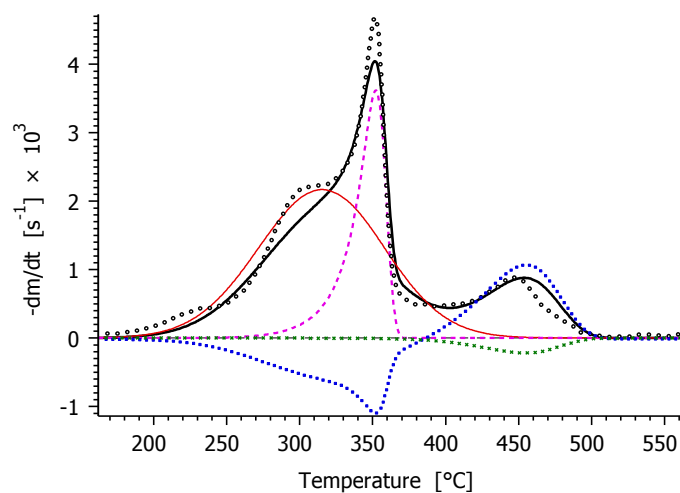
- 1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

**Willow, stepwise 2, [O2]=0.04**fit₁=4.03%, fit₁₀=4.21%

- 1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

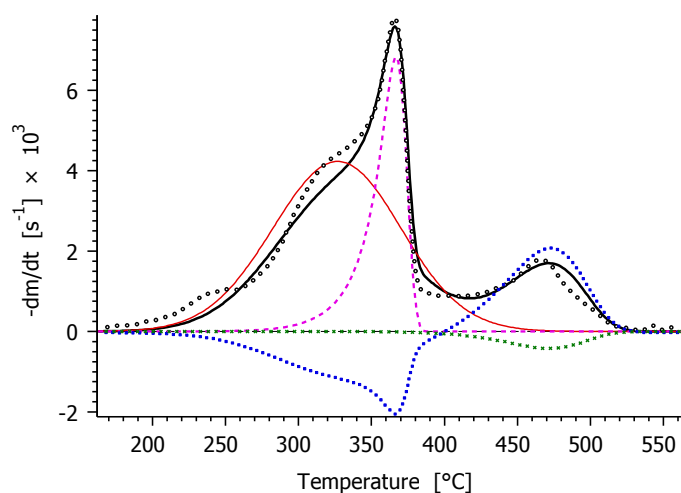
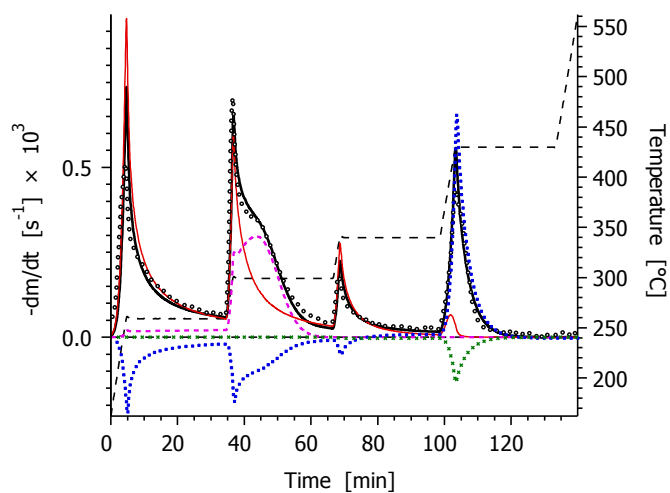
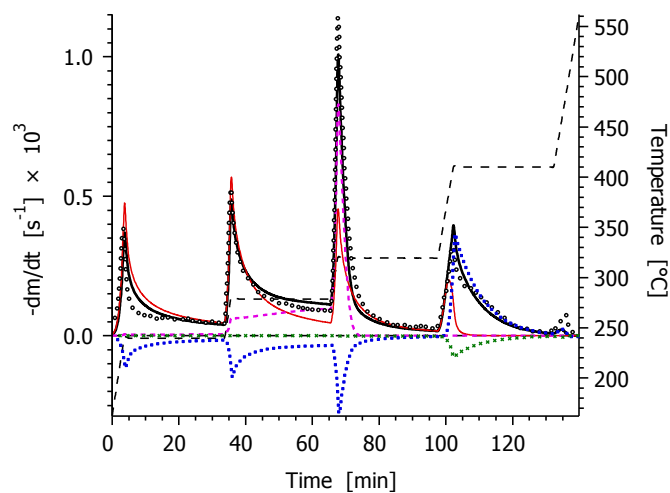
**Willow, 4°C/min, [O2]=0.2**fit₁=2.88%, fit₁₀=4.21%

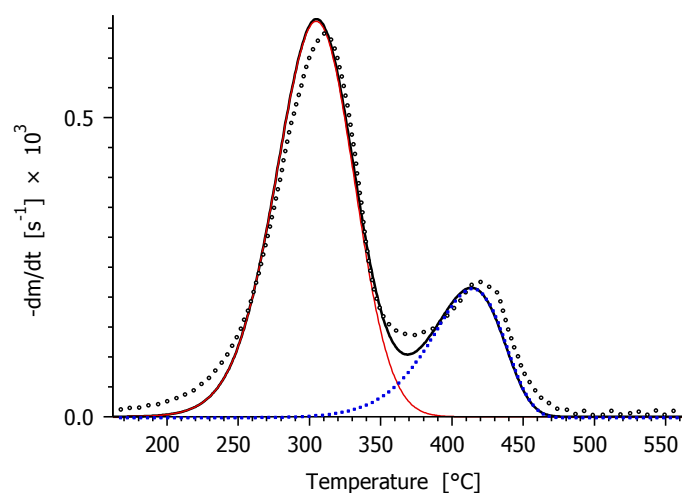
- 1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

**Willow, 20°C/min, [O2]=0.2**fit₁=3.49%, fit₁₀=4.21%

- 1: $E_0=165.9$ $\log_{10} A=13.05$ $\sigma(E)=11.2$ $v=0.366$ $\text{yield}=0.231$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$ $\text{yield}=0.208$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.624$ $\text{yield}=0.200$

Figure S3. (Continued)

**Willow, 40°C/min, [O₂]=0.2**fit₁=3.11%, fit₁₀=4.21%1: $E_0=165.9$ $\log_{10} A=13.05$ $\alpha(E)=11.2$ $v=0.366$ $\text{yield}=0.231$ 2: $E_0=145.0$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.611$ $\text{yield}=0.208$ 3: $E_0=168.9$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.624$ $\text{yield}=0.200$ **Willow, stepwise 1, [O₂]=0.2**fit₁=4.26%, fit₁₀=4.21%1: $E_0=165.9$ $\log_{10} A=13.05$ $\alpha(E)=11.2$ $v=0.366$ $\text{yield}=0.231$ 2: $E_0=145.0$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.611$ $\text{yield}=0.208$ 3: $E_0=168.9$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.624$ $\text{yield}=0.200$ **Willow, stepwise 2, [O₂]=0.2**fit₁=3.81%, fit₁₀=4.21%1: $E_0=165.9$ $\log_{10} A=13.05$ $\alpha(E)=11.2$ $v=0.366$ $\text{yield}=0.231$ 2: $E_0=145.0$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.611$ $\text{yield}=0.208$ 3: $E_0=168.9$ $\log_{10} A=10.66$ $\alpha(E)=0$ $v=0.624$ $\text{yield}=0.200$ **Figure S3.** (Continued)

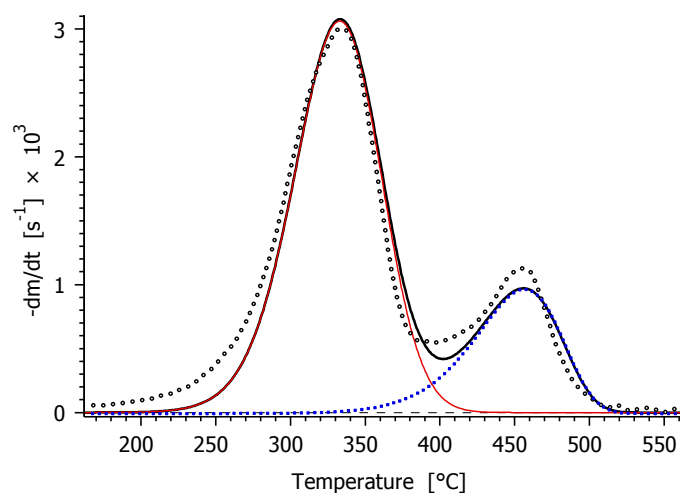


Wheat straw, 4°C/min, [O₂]=0.04

fit₁=4.16%, fit₁₀=3.99%

1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$

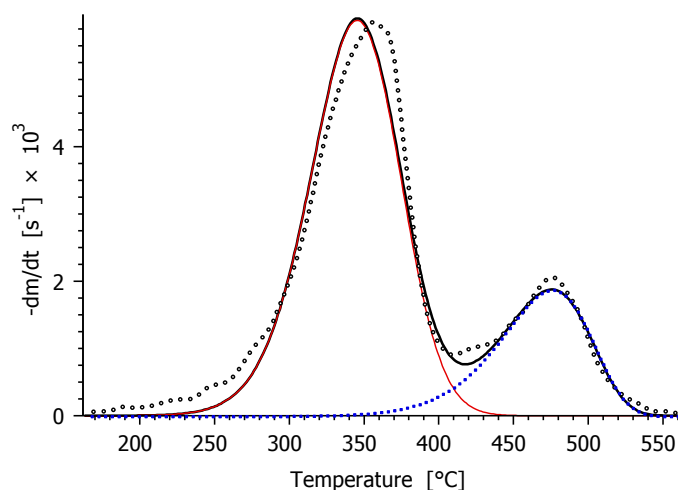


Wheat straw, 20°C/min, [O₂]=0.04

fit₁=4.53%, fit₁₀=3.99%

1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$



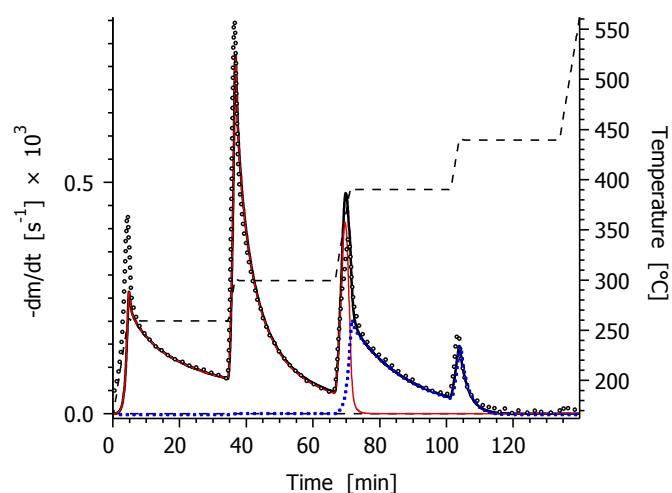
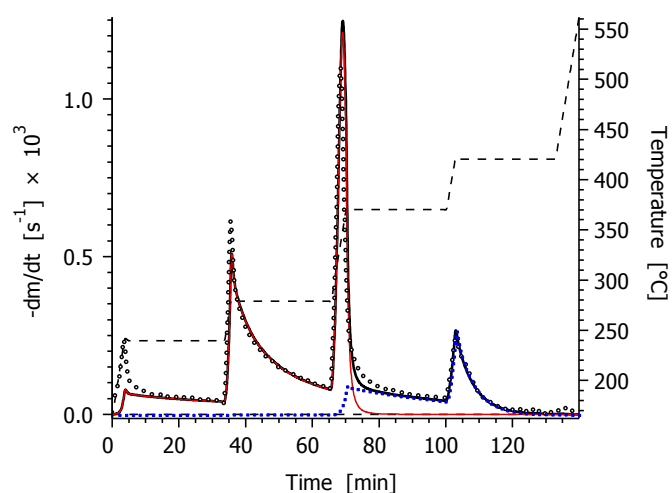
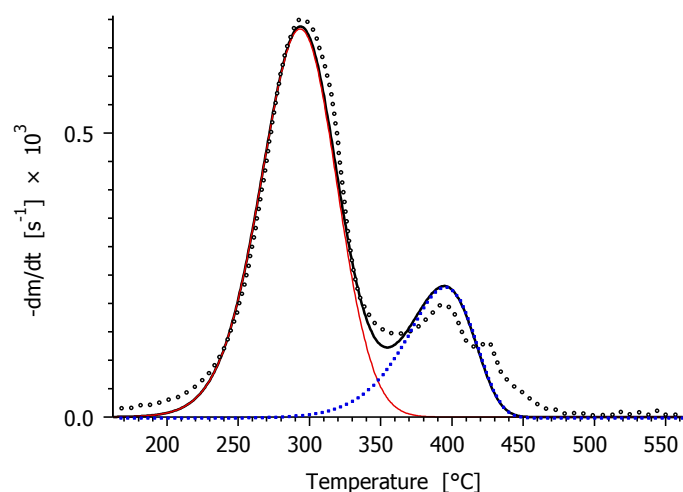
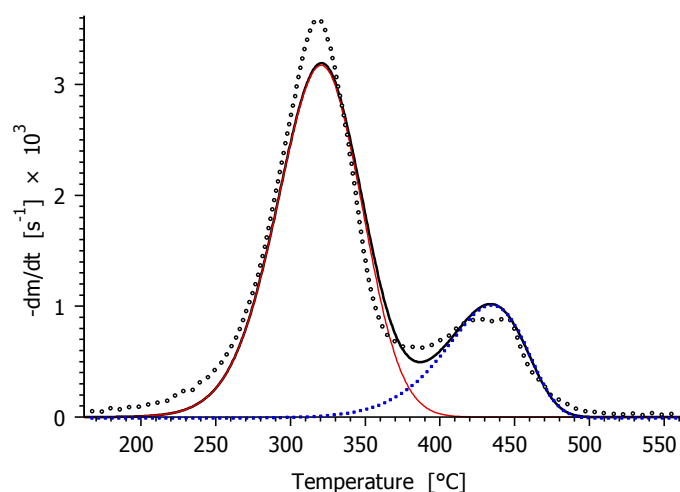
Wheat straw, 40°C/min, [O₂]=0.04

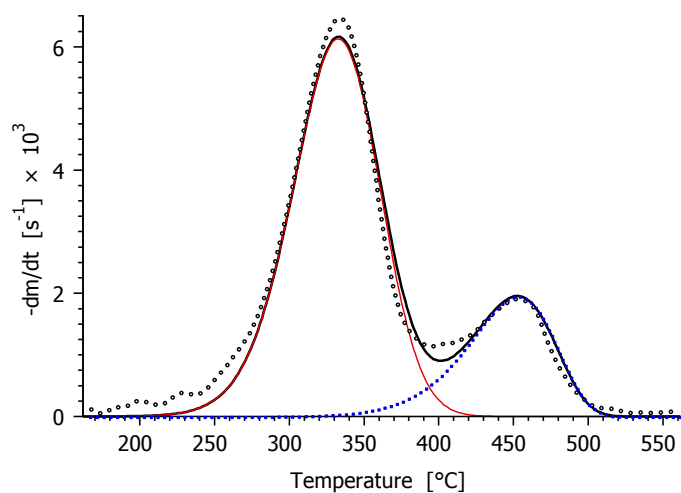
fit₁=5.25%, fit₁₀=3.99%

1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

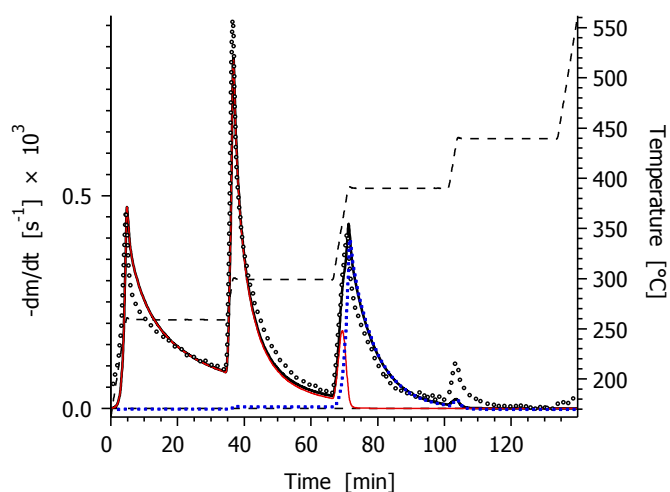
2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$

Figure S4. Evaluation of the wheat straw experiments by an approximate model of two parallel reactions

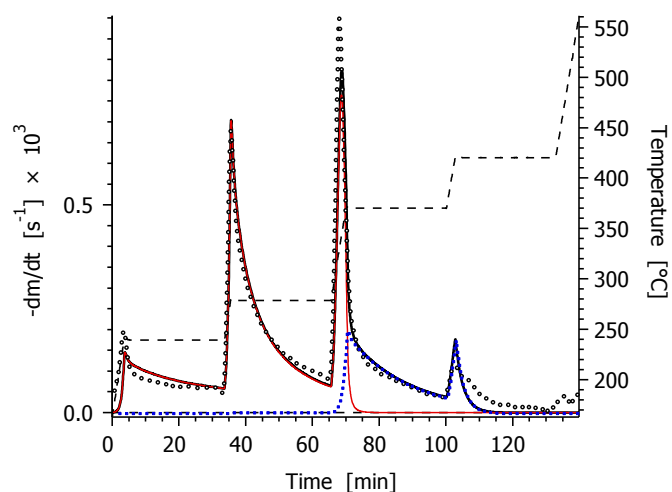
**Wheat straw, stepwise 1, [O₂]=0.04**fit₁=3.94%, fit₁₀=3.99%1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$ 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$ **Wheat straw, stepwise 2, [O₂]=0.04**fit₁=4.00%, fit₁₀=3.99%1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$ 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$ **Wheat straw, 4°C/min, [O₂]=0.2**fit₁=4.19%, fit₁₀=3.99%1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$ 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$ **Wheat straw, 20°C/min, [O₂]=0.2**fit₁=3.97%, fit₁₀=3.99%1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$ 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$ **Figure S4.** (Continued)


Wheat straw, 40°C/min, [O₂]=0.2
 $\text{fit}_1=3.01\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$

Wheat straw, stepwise 1, [O₂]=0.2
 $\text{fit}_1=3.14\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$

Wheat straw, stepwise 2, [O₂]=0.2
 $\text{fit}_1=3.15\%$, $\text{fit}_{10}=3.99\%$

 1: $E_0=156.9$ $\log_{10} A=12.23$ $\sigma(E)=5.53$ $v=0.431$

 2: $E_0=150.5$ $\log_{10} A=9.53$ $\sigma(E)=0$ $v=0.502$
Figure S4. (Continued)

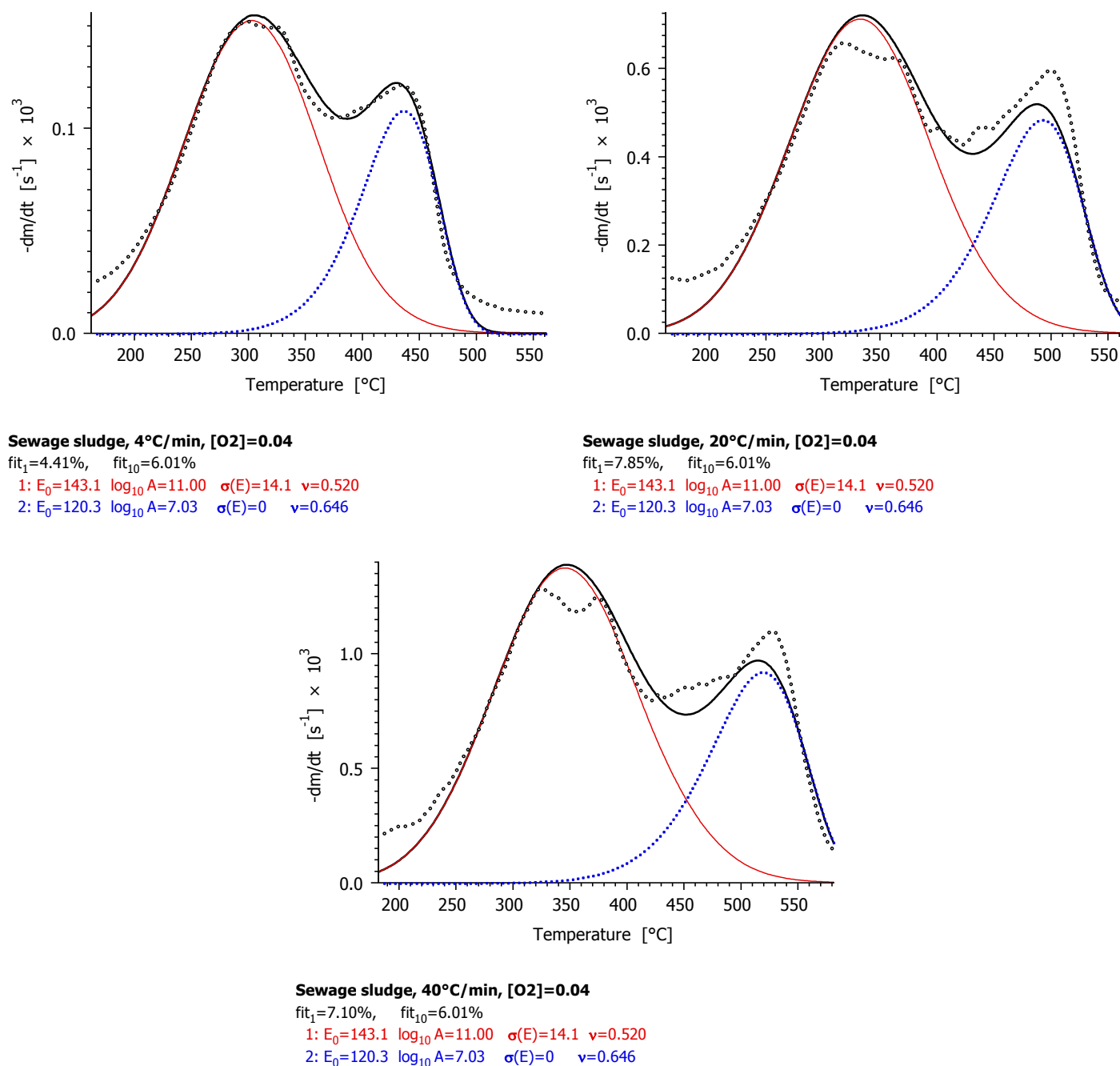
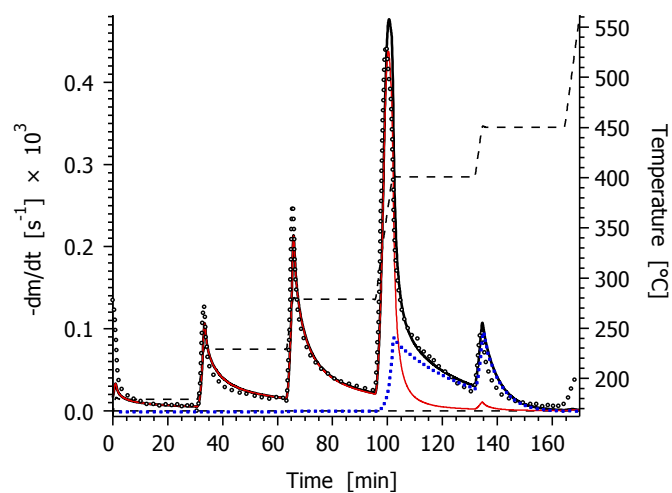
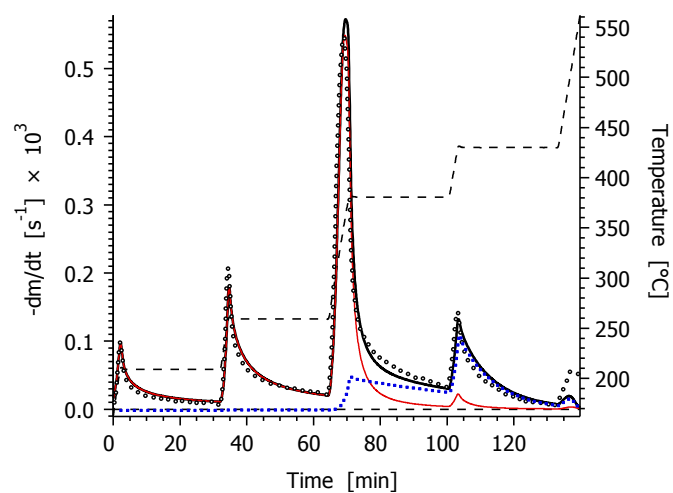
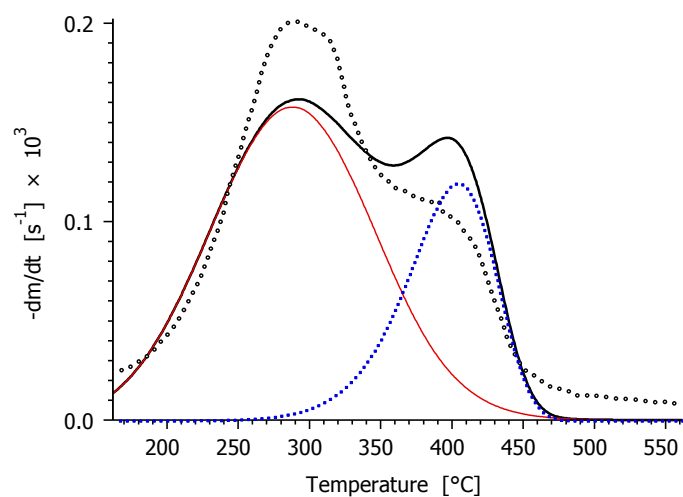
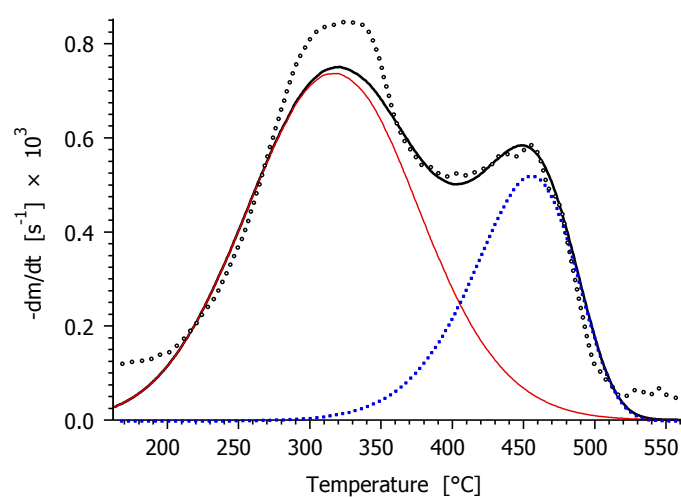
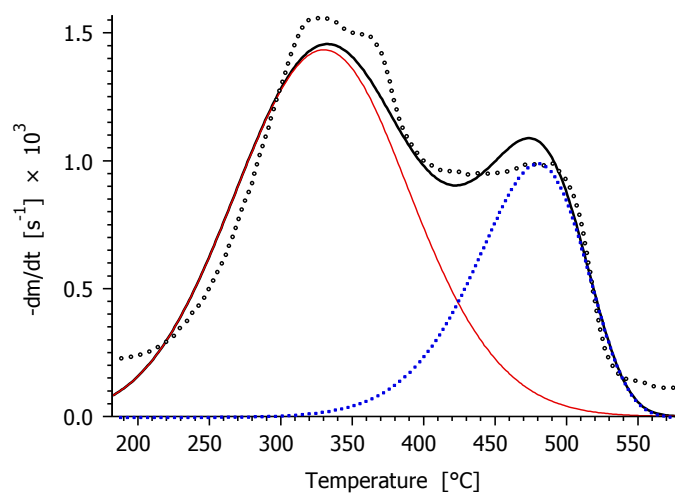


Figure S5. Evaluation of the sewage sludge experiments by an approximate model of two parallel reactions

**Sewage sludge, stepwise 1, [O₂]=0.04**fit₁=3.45%, fit₁₀=6.01%1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$ 2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ **Sewage sludge, stepwise 2, [O₂]=0.04**fit₁=2.69%, fit₁₀=6.01%1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$ 2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ **Sewage sludge, 4°C/min, [O₂]=0.2**fit₁=10.29%, fit₁₀=6.01%1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$ 2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ **Sewage sludge, 20°C/min, [O₂]=0.2**fit₁=5.76%, fit₁₀=6.01%1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$ 2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$ **Figure S5.** (Continued)

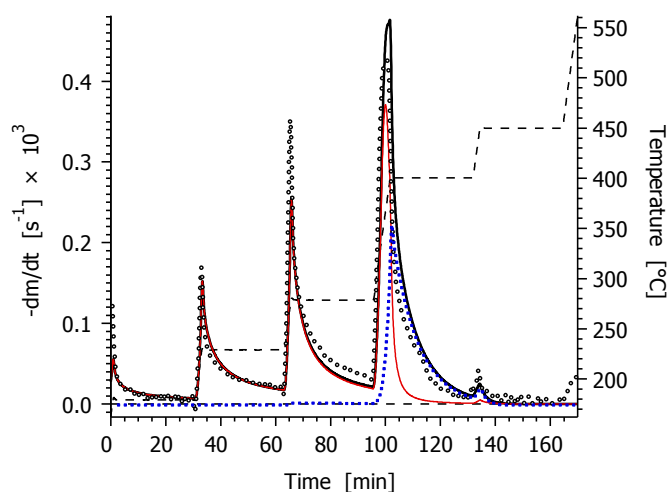


Sewage sludge, 40°C/min, [O₂]=0.2

fit₁=5.79%, fit₁₀=6.01%

1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$

2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$

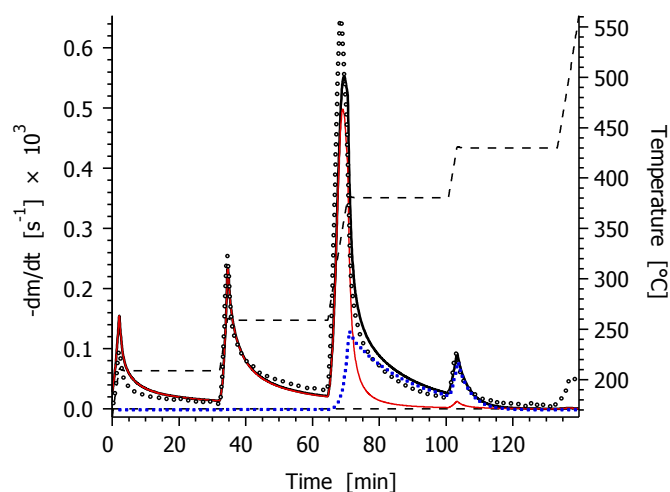


Sewage sludge, stepwise 1, [O₂]=0.2

fit₁=4.99%, fit₁₀=6.01%

1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$

2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$



Sewage sludge, stepwise 2, [O₂]=0.2

fit₁=3.63%, fit₁₀=6.01%

1: $E_0=143.1$ $\log_{10} A=11.00$ $\sigma(E)=14.1$ $v=0.520$

2: $E_0=120.3$ $\log_{10} A=7.03$ $\sigma(E)=0$ $v=0.646$

Figure S5. (Continued)

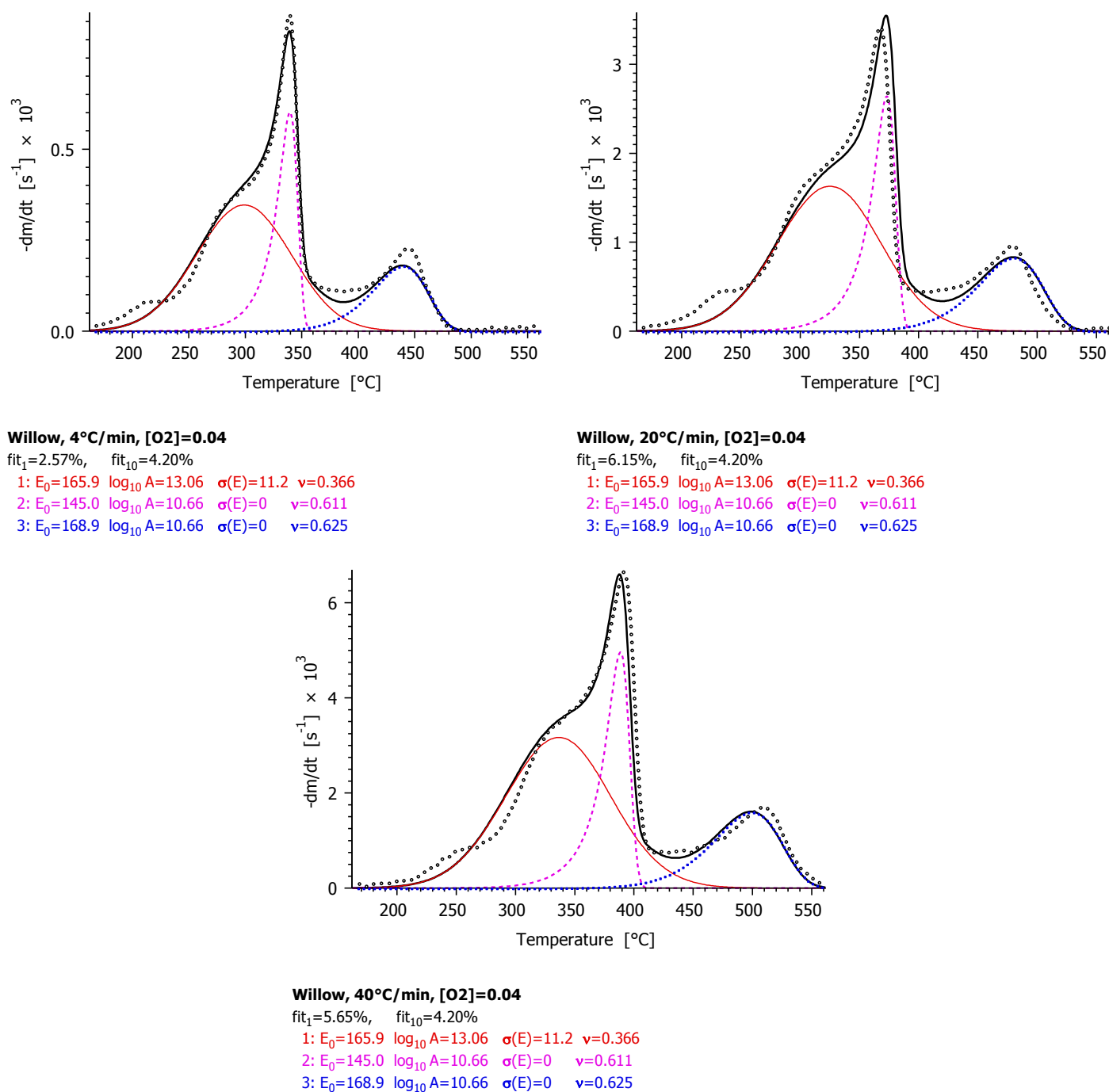
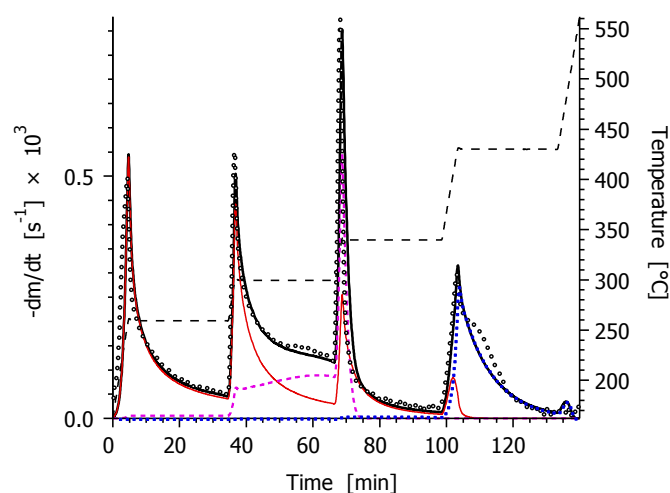
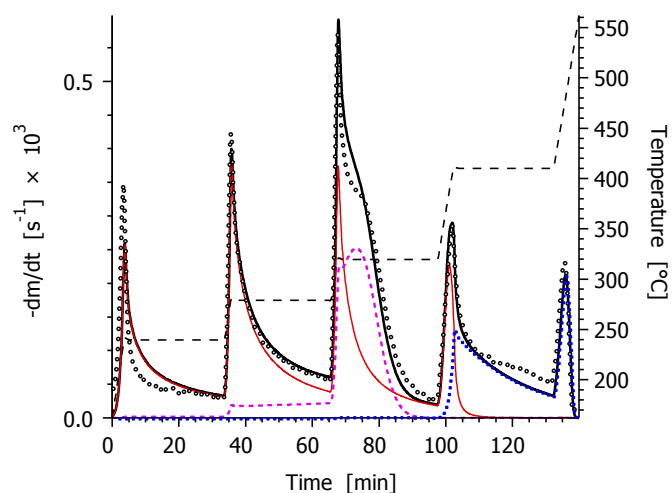


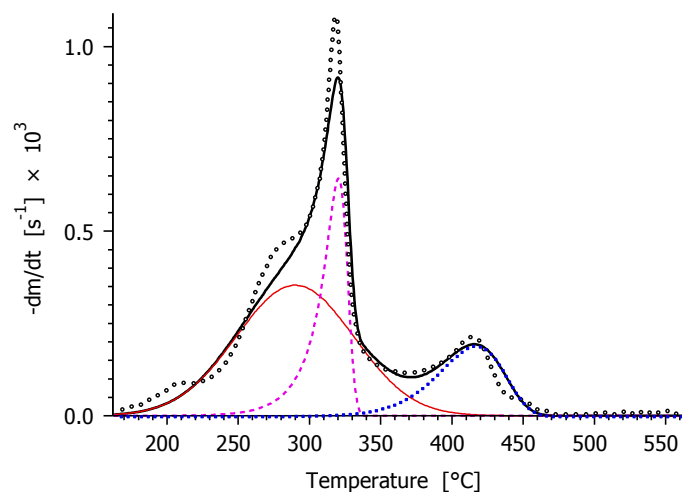
Figure S6. Evaluation of the willow experiments by an approximate model of three parallel reactions

**Willow, stepwise 1, [O₂]=0.04**fit₁=4.63%, fit₁₀=4.20%

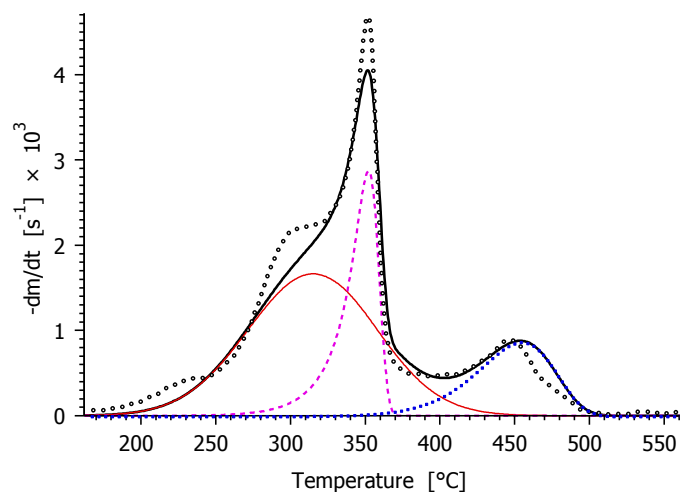
- 1: $E_0=165.9$ $\log_{10} A=13.06$ $\sigma(E)=11.2$ $v=0.366$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.625$

**Willow, stepwise 2, [O₂]=0.04**fit₁=4.03%, fit₁₀=4.20%

- 1: $E_0=165.9$ $\log_{10} A=13.06$ $\sigma(E)=11.2$ $v=0.366$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.625$

**Willow, 4°C/min, [O₂]=0.2**fit₁=2.87%, fit₁₀=4.20%

- 1: $E_0=165.9$ $\log_{10} A=13.06$ $\sigma(E)=11.2$ $v=0.366$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.625$

**Willow, 20°C/min, [O₂]=0.2**fit₁=3.49%, fit₁₀=4.20%

- 1: $E_0=165.9$ $\log_{10} A=13.06$ $\sigma(E)=11.2$ $v=0.366$
 2: $E_0=145.0$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.611$
 3: $E_0=168.9$ $\log_{10} A=10.66$ $\sigma(E)=0$ $v=0.625$

Figure S6. (Continued)

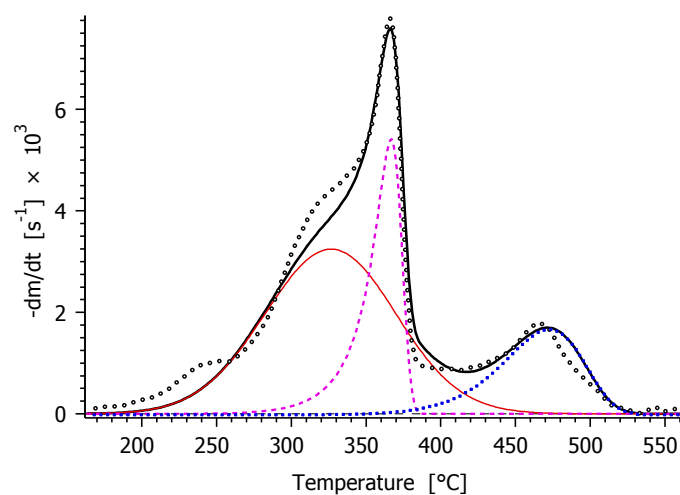
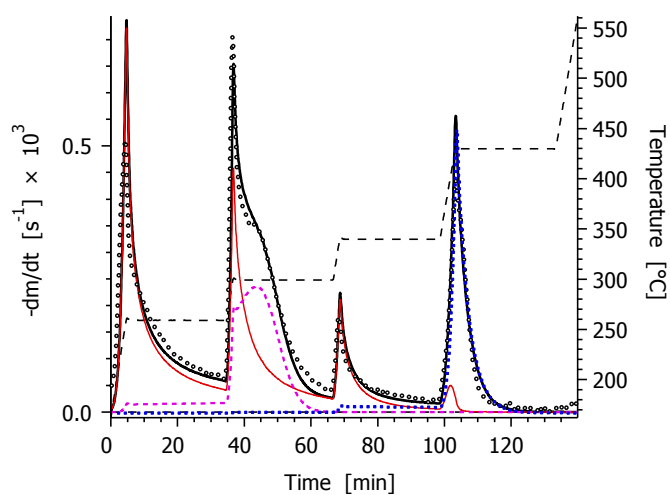
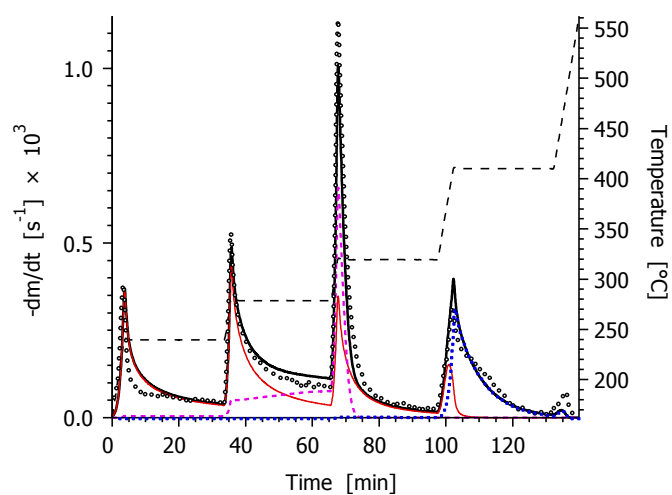
**Willow, 40°C/min, [O₂]=0.2**fit₁=3.10%, fit₁₀=4.20%1: E₀=165.9 log₁₀ A=13.06 σ(E)=11.2 v=0.3662: E₀=145.0 log₁₀ A=10.66 σ(E)=0 v=0.6113: E₀=168.9 log₁₀ A=10.66 σ(E)=0 v=0.625**Willow, stepwise 1, [O₂]=0.2**fit₁=4.26%, fit₁₀=4.20%1: E₀=165.9 log₁₀ A=13.06 σ(E)=11.2 v=0.3662: E₀=145.0 log₁₀ A=10.66 σ(E)=0 v=0.6113: E₀=168.9 log₁₀ A=10.66 σ(E)=0 v=0.625**Willow, stepwise 2, [O₂]=0.2**fit₁=3.81%, fit₁₀=4.20%1: E₀=165.9 log₁₀ A=13.06 σ(E)=11.2 v=0.3662: E₀=145.0 log₁₀ A=10.66 σ(E)=0 v=0.6113: E₀=168.9 log₁₀ A=10.66 σ(E)=0 v=0.625**Figure S6.** (Continued)

Table S1. Parameters of the $f(\alpha_{\text{cell}})$ functions^a

Devolatilization of the non-cellulosic part	DAEM	DAEM	DAEM	DAEM	DAEM	n-order
Char burn-off	successive 1 st order ^a	successive n order ^a	parallel 1 st order ^b	parallel n order	parallel DAEM ^b	successive 1 st order ^a
Line style and color of the corresponding curve in Figure S7	— black	— red	— blue	— green	— blue	- - - - dark magenta
n	0.87	0.87	0.88	0.88	0.88	0.86
a	2.89	2.98	3.21	3.24	3.21	4.86
z	1.02	1.06	1.16	1.18	1.16	2.55

^aThe parameters of the $f(\alpha_{\text{cell}})$ functions do not have physical meaning of their own. Their physical meaning lies in the shape of the corresponding $f(\alpha_{\text{cell}})$ curves, which are shown in Figure S7, below. The maximum curves shown there correspond to self-accelerating (autocatalytic) kinetics. The curves practically coincide with each other; only the dashed dark magenta curve (belonging to the last column in the table) differs from the others.

^bThe two evaluations denoted by blue color gave identical results because the DAEM for char burn-off converged to a simple first order reaction ($\sigma_{\text{char}}=0$).

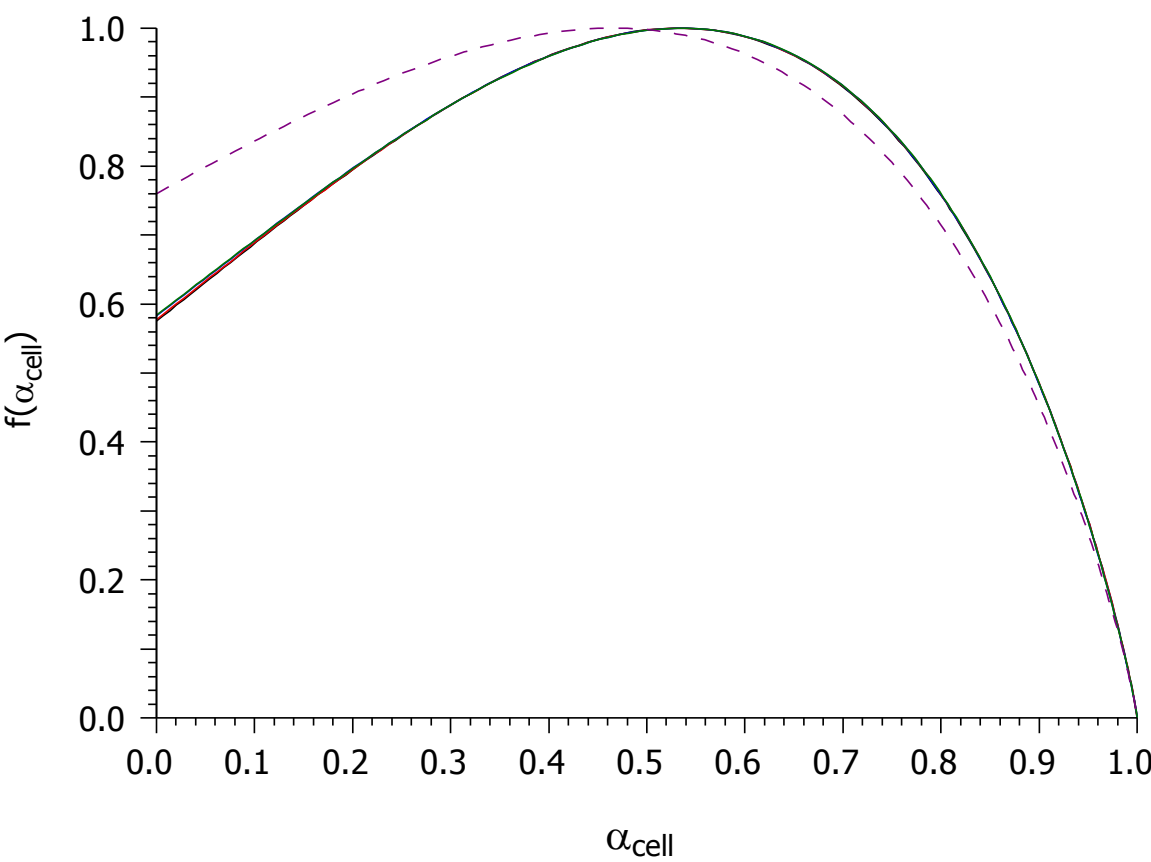


Figure S7. $f(\alpha_{\text{cell}})$ functions. (See the explanation in the footnotes of Table S1.)