Maximal gene number maintainable by stochastic correction – The second error threshold

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HIGHLIGHTS

- The second error threshold is set by intravesicular competition and assortment load.
- Multilevel selection can support as much as a 100 genes.
- This system can mitigate a limited amount of competition asymmetry.

ABSTRACT

There is still no general solution to Eigen's Paradox, the chicken-or-egg problem of the origin of life: neither accurate copying, nor long genomes could have evolved without one another being established beforehand. But an array of small, individually replicating genes might offer a workaround, provided that multilevel selection assists the survival of the ensemble. There are two key difficulties that such a system has to overcome: the non-synchronous replication of genes, and their random assortment into daughter cells (the units of higher-level selection) upon fission. Here we find, using the Stochastic Corrector Model framework, that a large number ($\tau >= 90$) of genes can coexist. Furthermore, the system can tolerate about 10% replication rate asymmetry (competition) among the genes. On this basis, we put forward a plausible (and testable!) scenario for how novel genes could have been incorporated into early living systems: a route to complex metabolism.

1. INTRODUCTION

It has been forty years since Manfred Eigen proposed the theory that mutations in molecular replication, a phenomenon considered conducive to the adaptation and speciation of the extant biota, could have posed a fundamental obstacle to the spontaneous formation of life (Eigen, 1971). The idea can be presented simply: early living systems lacking proof-reading processes had to tolerate a high rate of mutation; such mutation pressure precludes sustaining information in long chromosomes; but shorter genomes are unable to store proof-reading enzymes. For example, in the RNA world scenario “one cannot have accurate replication without a length of RNA, say, 2000 or more base pairs, and one cannot have that much RNA without accurate replication” (Maynard Smith, 1979). This is Eigen’s Paradox which still troubles origin of

life research: maintenance of information is a central topic of this field (Kun et al., 2015).

The notion of the error threshold was put forward with DNA genomes and peptide enzymes in mind. The 2000 base long RNA in Maynard Smith's example would code for an enzyme of length 600+, a small protein. A quick look at UNIPROT yields DNA-dependent DNA polymerases (E.C. 2.7.7.7) that are smaller than this, albeit mostly DNA polymerase IV, which is quite error prone.

On the other hand, reliable information replication evolved during the RNA world (Joyce, 2002; Kun et al., 2015; Yarus, 2011). The RNA world is the era in the history of Earth during which information was stored in RNA and catalysis was mostly done by RNA enzymes (ribozymes). At the moment, there is no known general RNA-based RNA polymerase ribozyme. There is a ribozyme which can catalyse the template based polymerisation of up to 98 nucleotides (Wochner et al., 2011), and given a very specific template a ribozyme can copy longer strands as well (Attwater et al., 2013) on par with its size of roughly 200 nucleotides. Still 200 nucleotides is a long sequence to emerge through non-enzymatic processes, when we take prebiotic replication fidelity into account (<99%, (Orgel, 1992)).

The error threshold, in the simplified treatment of Maynard Smith (1983), is: $L < \ln s / \mu$, meaning that the maximum sustainable genome size (L) is less than the quotient of the natural logarithm of the selective superiority (s) of the sequence to be copied ('master') and the error rate (μ). Selective superiority is the ratio of the average Malthusian growth rates of selected sequences (here, only the master) versus the rest (here, its mutants). Let us say that the error rate is $\mu = 0.01$ (Orgel, 1992). Based on the above inequality, this only allows the sustainment of sequences shorter than $L < 100$ monomers (with the standard assumption that $\ln s \approx 1$). Thus the 200 bases long putative replicase ribozyme (Wochner et al., 2011) seems to be too long.

Recent advances paint a brighter picture. An order of magnitude longer functional ribozymes can be maintained (with the error rate being equal) if the structure of the ribozymes, and the neutral mutations it allows, are taken into account (Kun et al., 2005; Szilágyi et al., 2014; Takeuchi et al., 2005). Second, it seems that intragenomic recombination may have shifted the threshold by about 30% (Santos et al., 2004). Third, the processivity of replication (i.e. the constraint that during template-based replication, nucleotides have to be inserted one by one into the growing copy) may have somewhat filtered against errors, provided erroneous insertions had slowed down replication (Huang et al., 1992; Mendelman et al., 1990; Perrino and Loeb, 1989): erroneous copies would have thus suffered from an inherent fitness disadvantage (Leu et al., 2012; Rajamani et al., 2010). It may also have alleviated the error threshold by about another 30%.

While such a relaxed error threshold seems less problematic, the replication of whole genomes that could run a primitive metabolism is still out of reach. Ribocells (cells whose metabolism is run by RNA enzymes) require at least one ribozyme of each of the essential enzymatic functionalities to be considered viable: they can produce the biomass component necessary for growth and reproduction. Cells lacking even one of the functions cannot reproduce. Thus all information needs to be replicated, which can be done if all ribozymes replicate individually. Individual known ribozymes are short enough to be faithfully copied (Szilágyi et al., 2014). However, if individual genes are replicated, they have individual growth rates inside the cell. Sequences having the highest growth rates will dominate the ribozyme population, and other genes will be lost (cf. the Spiegelman experiment (Kacian et al., 1972)). Thus while the error catastrophe can be overcome by replicating the whole set of genes required for the cell as individual replicators, it creates

another problem, that of non-synchronous replication. How much information can be integrated via the compartmentalisation of individually replicating ribozymes? Is such a system complex enough to overcome the error catastrophe?

The Stochastic Corrector Model (SCM) is a group selection / package model framework; it was developed to investigate the above compartmentalised system, which has the potential to solve the problem of information integration. Szathmáry and Demeter (1987) have shown that given a low number of replicators inside a cell having a far from optimal copy number distribution (the goal distribution can be arbitrary), stochastic separation of the genes into the daughter cells can ameliorate the copy number distribution of the parent cells. Previous works on the SCM have focused on cells with only two (Grey et al., 1995; Zintzaras et al., 2010) or three genes (Zintzaras et al., 2002). A few enzymes can coexist without a problem even without full compartmentalisation, i.e. on surfaces (Boerlijst, 2000; Czárán and Szathmáry, 2000; Hogeweg and Takeuchi, 2003; Könnyű and Czárán, 2013; Takeuchi and Hogeweg, 2009). And in vesicle models the coexistence of a few enzymes was demonstrated (Hogeweg and Takeuchi, 2003; Takeuchi and Hogeweg, 2009). An intellectual forebear to the SCM framework, the package model introduced by Niesert *et al.* (1981) shows that more than three genes can coexist. They assumed that cell division rate does not depend on its composition as long as at least one copy of each gene is present. A follow up study by Silvestre and Fontanari (Silvestre and Fontanari, 2008) shows the prerequisites for the coexistence of up to 10 genes. But the maximal number of coexisting genes was not investigated except by Fontanari *et al.* (2006), who have shown that arbitrary number of genes can coexist, if their replication rates are the same and the population size is infinitely large. These assumptions, however, are unrealistic—and as we will show–both of them critically affect gene coexistence.

Here we investigate how many independently replicating genes can coexist in a cell, despite the potential for information loss due to random assortment to daughter cells and non-synchronous replication. Information loss due to mutations in individual ribozymes is not investigated here. We already know that the error threshold limits the amount of information that can be maintained, and including it now would hamper our ability to assess how many genes can coexist despite different replication rates and random assortment into daughter cells. We show that these also limit the sustainable length of information. To distinguish these two sources of limitation, we term Eigen's limitation 'first error threshold' and the limitation investigated here 'second error threshold'.

2. METHODS

We follow the dynamics of a population (N) of ribocells. The biomass of the cells is produced by an abstract metabolism requiring τ different enzymatic functions. Ribozymes (catalysts) replicate individually and there could be more than one ribozyme of each type in the cell. The internal composition of the cell, i.e. the number of ribozymes and their distribution among the metabolic functions, determines the metabolic activity (R_i), which in turn affects the growth and replication of the cell. Accordingly, a cell i containing $\nu_i \in [1, \nu_{\max}]$ independently replicating ribozymes distributed among the τ different genes each having $\nu_{i,j}$ copies ($\nu_i = \sum_{j=1}^{\tau} \nu_{i,j}$) has a metabolic activity

$$R_i = \frac{\nu_i}{\nu_{\max}} \cdot \left(c \prod_{j=1}^{\tau} \frac{\nu_{i,j}}{\nu_i} \right)^{\varepsilon} . \qquad (1)$$

The main components of equation (1) are the effect of the cell size, and the effect of its composition. The greater the size of the cell, i.e. the number of ribozymes it harbours, the faster its metabolic activity will be (cf. the influx of materials through the surface). But the composition, the copy number of the different

genes, matters as well. Each reaction (catalysed by its gene) is presumed to be essential in the metabolic pathway (producing intermediers (e.g. monomers) for the replication of the ribozymes). If a cell loses any such genes, it becomes unviable (perishes) as its metabolic activity goes to zero. The optimal composition, maximising the second part of the equation (1) is the uniform distribution of copy numbers: where every different gene (ribozyme) is present with an identical number of copies (cf. the inequality of arithmetic and geometric means). A constant $c = \tau^{\tau}$ ensures that a cell of size $\nu_{\max}$ always has a maximal metabolic activity of $R_i = 1$. An arbitrary exponent (ε) weights the two components (size and composition). In preliminary studies employing $0.3 < \varepsilon < 3$, we found that giving higher weight to the composition is beneficial for the sustainability of the genome. We used $\varepsilon = 0.3$ for all results presented below.

The population dynamics is the following: a cell is chosen randomly, in proportion to its metabolic activity (R_i); this cell gains one new ribozyme. Next, a ribozyme (j) is chosen randomly from the ribozymes in the selected cell, proportionately to its replicase affinity (a_j); this ribozyme is copied. The new ribozyme belongs to the same type and has the same replicase affinity as its parent. Thus the replication rate of a molecule ($r_{i,j}$) is determined by the metabolic activity of the ribocell and the intracellular affinity differences

$$r_{i,j} = \frac{R_i}{\sum_{k=1}^{N} R_k} \cdot \frac{a_j}{\sum_{l=1}^{\nu_i} a_l}. \qquad (2)$$

If the number of ribozymes inside a cell reaches a maximal number ($\nu_{\max}$), then the cell splits into two. The ribozymes get into one of the daughter cells independently and randomly. The two new cells take the place of the parent cell and another one, which will perish, chosen randomly (with uniform probability): the population dynamics is a Moran process. Thus we assume constant population size, and fitness independent death-rate.

Pilot studies have shown that 50 "generations", i.e. $g = 50N$ cell divisions, are enough for the system to reach equilibrium. Extinction of the population (zero metabolic activity for every cell) is also an equilibrium state of this system. In all cases where extinction did not occur, we ran our simulations for $g = 100N$.

The initial cells start with $\nu_{\max}/2$ ribozymes, uniformly distributed among each function. When we refer to ribocell size, we mean this initial (and mean after-reproduction) ribozyme count.

For computational purposes, a metabolic activity of $R < 10^{-6}$ was taken to be zero.

3. RESULTS

Genes can coexist in the SCM, and the parameter range in which coexistence is possible increases with population size (N) (Fig. 1) and gene redundancy within the cell (Fig. 2), furthermore, the more equal the replication rates of the individually replicating genes, the more genes can coexist (Fig. 3).

Let's start by assuming that each functionally different ribozyme (different genes) has the same affinity to the replicase, thus there is no competition asymmetry in the system. A larger population size allows more genes (functionally different ribozymes) to coexist (Fig. 1). This is not surprising, given the fact that an infinite population size guarantees coexistence (Fontanari et al., 2006). However, it is also important to know how infinity is approached. It seems that for most of the parameter space, an increase in population size has a meagre effect on cell viability. Thus, while it is possible to increase population size to achieve the coexistence of any number of genes, the additional population size required for it can be unrealistically large; e.g. an increase of nearly two orders of magnitude in the population size (from 100 to 10,000) does not raise the fraction of viable cells when

$\tau > 45$. Because of computational limits, we did most of our simulations with $N = 1000$.

Tiny systems are prone to environmental and population stochasticity. Drift dominates when the population size is less than a hundred. Droplet based systems—the best currently available experimental setup to study protocells—as implemented e.g. in microfluidic devices (Agresti et al., 2005; Kelly et al., 2007; Taly et al., 2007), can easily accommodate a million droplet in a very small space and requiring little amount of material. Population size on the magnitude of a million should not be unrealistic for a primordial system with 100+ genes. We have shown that coexistence is possible for as few as 1,000 cells (and for potentially fewer, Fig.1). Thus our estimates of maximal genome size are conservative, as increasing population size would allow for a slightly greater coexistence of replicators.

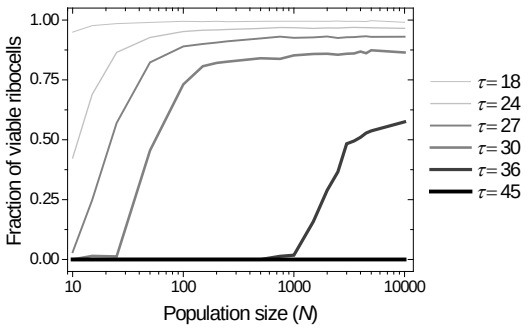

Figure 1. Fraction of viable cells increases with population size. Darker and wider lines represent systems with more required functions (τ). In all cases there are $\nu_{max} = 2160$ ribozymes in the cells. All cells are viable if $\tau < 18$, and none is viable if $\tau > 45$. Note the logarithmic scale of the X axis.

Any number of genes can coexist, given a sufficient redundancy (copy number of ribozymes of each type), and thus a required maximum ribocell size. The transition between ribocell sizes precluding coexistence and ensuring a viable population is threshold-like (Fig. 2). Increasing the maximum number of ribozymes inside the cells (and with it, the achievable redundancy for each gene) increases the fraction of viable ribocells. The shape of increase is sigmoid with a steep ascent. The midpoint of this ascent is the second error threshold, i.e. the redundancy below which a given number of genes cannot robustly coexist. Thus at any given ribozyme abundance, there is a maximum to how many genes can coexist. Reaching higher maintainable ribozyme diversities require an increase in the number of ribozymes a cell can harbour. As a good rule of thumb, the maintainable genetic diversity (number of genes) is approximately equal to the square root of the maximum number of ribozymes. Thus the size of the ribocells need to increase less than linearly proportional when the number of genes increases. At $N = 1000$ about 100 different ribozymes can coexist if a cell houses on average 10,000 ribozymes per cell. Once a population passes the error threshold and becomes viable, further increase in gene redundancy has negligible effect.

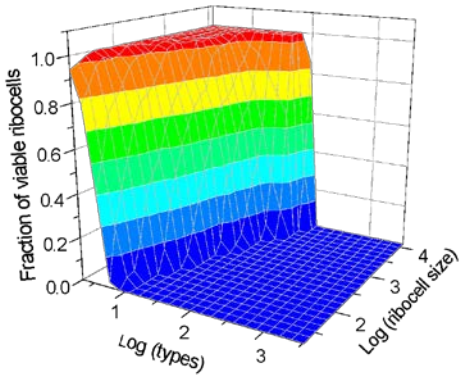

Figure 2. Maximum gene diversity. The fraction of viable ribocells is displayed as function of the number of types (τ) and the number of ribozymes per ribocell (ribocell size, $\nu = \nu_{max}/2$). Please note that it is the logarithm of the number of types and ribocell size that is on the X and Y axes, respectively. $N = 1000$.

Now we can forgo our initial assumption that every ribozyme has the same affinity to the replicase. Three different scenarios are compared with the previous results: (1) all affinities are the same, except for one ribozyme, which has a higher affinity; (2) all affinities are the same, except for one, which is lower; and (3) half of the genes have a higher, the others have a lower affinity (in case the number of

genes is odd, there is an extra higher-affinity gene). Competition asymmetry can cause the (competitive) exclusion of some of the genes, and consequently the loss of viability of the cells. When affinities differ as much as 10%, then, in the case of a single competitively superior gene, coexistence is already lost at $\tau = 12$ (Fig.3a). In the case when there is a single competitively inferior gene, a considerable number of genes can coexist despite 10% difference in their affinity to the replicase. The stochastic corrector can tolerate all of these scenarios when the difference in the affinities is even lower, i.e. 1% (Fig.3b) or 0.1% (Fig.3c).

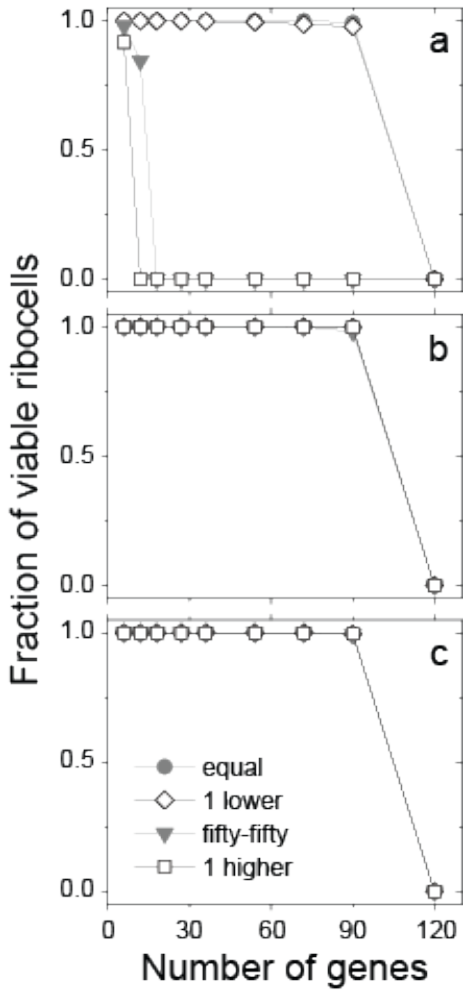

Figure 3. Mean fraction of viable cells harbouring genes with non-equal affinities to the replicase. "Equal" (solid square) $a_{1..\tau} = 1$; "One lower" (open rhombus) $a_{1..(\tau-1)} = 1$ and $a_\tau = \alpha$); "1:1" (solid circle) $a_{1..(\tau/2)} = 1$ and $a_{(\tau/2)+1..\tau} = \alpha$; and "one higher" (open downward triangle) $a_1 = 1$ and $a_{2..\tau} = \alpha$. (a) $\alpha = 0.9$, (b) $\alpha = 0.99$, (c) $\alpha = 0.999$. Symbols represent means from 10 iterations. $\nu_{\max} = 25920$

Once again, we can examine the effect of redundancy on the sustainable genome size. When affinities are unequal, it is no longer true that a greater redundancy helps sustain a larger genome (Fig. 4). For two genes ($\tau = 2$) of unequal replicase affinities ($\alpha = 0.9$), a ribocell size of more than a 100 molecules leads to a less uniform composition (and a lower mean metabolic activity in the population) than a smaller ribocell size. Thus there is an optimal ribocell size ($\nu \approx 80$) where despite differences in replicase affinities a mostly uniform composition is sustained. For 100 genes ($\tau = 100$) and a one-lower affinity distribution ($\alpha = 0.9$), we could not find this optimum. However, we show that below this supposed optimum, the mean metabolic activity of the population increases quicker with ribocell size (redundancy) when the affinities are equal. In both the equal and unequal cases, the minimal redundancy sufficient for coexistence is the same (100 copies of each gene), and is in agreement with Fig. 2.

4. DISCUSSION

Non-synchronous replication and random assortment leads to a threshold-like decrease in the viability of ribocells as the number of type increases. Thus there is a limit to the enzymatic diversity that can be maintained in an ancient cell. We term this limit the second error threshold. Despite the existence of the second error threshold, a sizable number of genes can coexist. Here we have shown that as many as 100 different genes (types) can coexist if internal copy number is moderately high and affinities do not differ by more than 1%.

4.1 ASSUMPTIONS OF THE MODEL

The computational analysis presented in this paper focuses on the phenomena we call the second error threshold. For this reason, we have excluded mutations from our current model. We understand that excluding possible mutations in

the enzymatic activities can affect our results. Increasing mutational rate can push the population over the error threshold (Kun et al., 2015; Takeuchi and Hogeweg, 2012). Here we show that assortment load also leads to a threshold-like change in the viability of the population, independently of the first error threshold. Mutations can also produce parasites, sequences that do not contribute to biomass production, but which contribute to cell size. Thus cells might divide harbouring few enzymes and many parasites, leading to deficient daughter cells with a higher probability. On the other hand, such cells have a severe selective disadvantage, and they would divide at a slower rate compared to cell having few parasites. The possibility of efficient information integration in the presence of parasites was demonstrated in the Stochastic Corrector Model framework (e.g. (Zintzaras et al., 2002)), albeit for only 3 genes. The interplay of the two error thresholds will be revisited in a future study.

We assume that the limiting factor in the metabolism of the cells is the number of enzymes present. Food scarcity is irrelevant, as it does not differentiate between the ribocells, thus would not affect selection.

The employed fitness function assumes that a uniform distribution of every different ribozyme results in the highest ribocell replication rate (metabolic activity). Metabolic activity, and thus ribocell fitness, drops considerably if the distribution deviates from the uniform distribution. But as long as at least one ribozyme from each type is present, the ribocell remains viable. It can be understood as either a linear (serial) set of all-essential reactions (for example, a chain of reactions that transform food molecule to monomers), or parallel pathways with equally important end-products (for example, the parallel production of all NTPs). This assumption of the essentiality of genes protects against information loss. For an additional layer of realism, a metabolic network can be employed, and the metabolic flux through the network can be used as a proxy for fitness (as in (Szilágyi et al., 2012)).

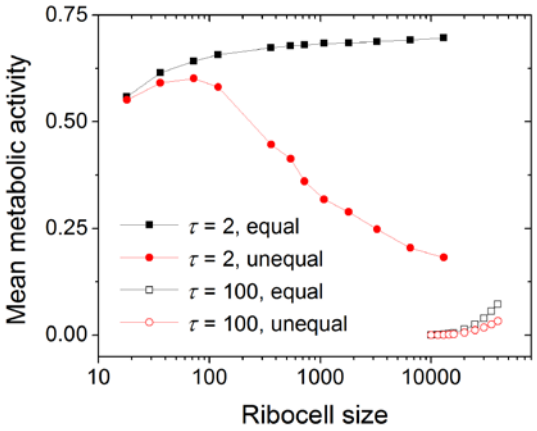

Figure 4. The effect of redundancy on asynchronous replication. Cases of equal and unequal affinities show a divergent trend with the growth of ribocell size ($\nu = \nu_{\max}/2$). Solid symbols: $\tau = 2$; open symbols: $\tau = 100$; black line (square): equal affinities; red line (circle): unequal, one-lower affinity distribution, $\alpha = 0.9$. Note the logarithmic scale of the X axis. N =

However, the added complexity of flux calculation pose a technical difficulty (as the computational requirement is already quite high), and may necessitate other simplifying assumptions.

4.2. MINIMAL GENE NUMBER OF A RIBO-ORGANISM

Minimal genome sizes found in contemporary organism can be as low as 112 kbases: *Nasuia deltocephalinicola* (112 kbase) (Bennett and Moran, 2013), *Tremblaya princeps* (139 kbase) (McCutcheon and von Dohlen, 2011), *Hodgkinia cicadicola* (144 kbase) (McCutcheon et al., 2009), *Sulcia muelleri* (146 kbase) (Chang et al., 2015; McCutcheon and Moran, 2007; McCutcheon and Moran, 2010; Woyke et al., 2010; Wu et al., 2006), *Carsonella ruddii* (160 kbase) (Tamames et al., 2007), *Zinderia insecticola* (208 kbase) (McCutcheon and Moran, 2010). However, these symbionts of insects are barely alive in the sense that they lack genes for membrane and cell wall synthesis, lack transporters, most of carbon metabolism (McCutcheon and Moran, 2011) and some even lack some genes for DNA replication and translation. Other symbionts and intracellular

parasites have genomes of around 600 kbases (*Mysoplasma genitalium, Buchnera* sp. (Islas et al., 2004)) and these minimalistic cells contain around 500-600 genes. However, the smallest possible genome size could have been even less (Luisi et al., 2006; Szathmáry, 2005): around 200 genes (Gil et al., 2004) (Table 1). These estimates pertain to cells having a DNA genome and peptide enzymes. A minimal ribo-organism can do with less. Jeffares *et al.* (1998) suggested that the last ribo-organism had a genome of 10-15 kbases. This estimate includes ribozymes involved in translation and RNA replication, but it lacks enzymes for the control of cell division, and the estimate for intermediate metabolism is rather arbitrary. The *last* ribo-organism most probably had translation, but we are more interested in the *first* cells, and not in the ones just on the verge to switch to DNA genomes.

A ribocell requires enzymes for the replication of its genetic material, chaperones for its ribozymes, maybe some enzymes that alters ribozymes much like post-translational modification alters peptide enzymes. Cellular processes, such as transport, also need some RNA enzymes. Moreover, the NTPs (both as monomers for RNA synthesis and as energy molecules), coenzymes and lipids need to be produced. A good estimate for the minimal intermediate metabolism covering said functionalities is given by Moya and co-workers (Gabaldón et al., 2007), who suggested 50 enzymes to be the minimum. We have to note that this set also included enzymes for dNTP production, which a ribo-organism did not need. A conservative estimate of 88 ribozymes is afforded by this back-of-the-envelope calculation (Table 1). Most probably even fewer ribozymes would be enough, as this set of 88 contains multi-subunit enzymes as well (Gil et al., 2004). We have estimated 60 to be a minimum (Szilágyi et al., 2012), a more detailed analysis of the minimal set of genes required for a ribocell will be proposed later (Kun *et al.*, *in prep*).

It is clear that even with 0.99 replication fidelity, a chromosome packed with 60 genes cannot be maintained due to the first error threshold. Sixty or even a hundred individually replicating genes can be maintained in randomly assorting ribocells (given a large enough cell size (Fisg. 1,2 & 4) at equal or one-lower (Fig. 3) replicase affinities, and an affinity difference not higher than 10%). We thus conclude that the information required for a minimal ribocell can be propagated despite the existence of the second error threshold.

4.3 POSSIBLE EVOLUTIONARY ROUTE TO COMPLEX METABOLISM

Metabolisms having hundreds of enzymes and molecules do not appear at once. Most probably enzymes, and thus functions, were added one at a time (Szathmáry, 2007). A few enzyme can coexist on surfaces (Boerlijst, 2000; Czárán and Szathmáry, 2000; Hogeweg and Takeuchi, 2003; Könnyű and Czárán, 2013; Takeuchi and Hogeweg, 2009) as well as in vesicles (Hogeweg and Takeuchi, 2003; Szathmáry and Demeter, 1987; Takeuchi and Hogeweg, 2009; Zintzaras et al., 2002). How

Table 1. Estimate of a minimal gene set for a ribo-organism

Function	Number of gene in a DNA-peptide organism	Number of gene in a ribo-organism	Notes
Replication of the genetic information	16	16	
Translation	106	0	
Enzyme folding, modification and translocation	15	15	
Cellular processes	5	5	
Energetic and intermediary metabolism	56	52	no need for dNTP production
Total	198	88	

can we get from a few enzymes to nearly a hundred? The enhancement of metabolic capabilities afforded by more enzymes is surely selectively advantageous. On the other hand, if the new enzyme cannot establish or coexist with the "old" ones, then this evolutionary step cannot be taken. Based on our results we can propose a possible evolutionary route to increasing metabolic complexity, i.e. more genes.

Equal affinities to the replicator ensure that no replicator outcompete the others. Thus the process could have started by a few (even two) ribozymes with equal replication rates. Now let us assume that any novel enzyme has a lower affinity to the replicase than the already established ones, then this enzyme can establish in the system, even if its affinity to the replicase is lower by as much as 10% compared to the rest of the enzymes (cf. Fig. 3a). Difference in affinities could not be very high: 10% difference is too much for the maintenance of a mere 10 enzymes, which is still too few for a metabolism. However, new enzymes probably evolved from established ones, and thus probably had tag sequences compatible with the replicase. Such a system can evolve to equalise all affinities (Kun, unpublished results), in this case to increase the affinity of the new enzyme. The simultaneous addition of more enzymes may drive the system to extinction, but the addition of a single one seems to be feasible. During this process, the total information content of the cell also increases. While given the same replication fidelity, the number of genes can only increase by decreasing the length of individual enzymes (Silvestre and Fontanari, 2008), the increased metabolic efficiency could allow for better replicases. Gradual coevolution of the metabolism and replication fidelity is possible (Scheuring, 2000). Thus enzymes can be added one after the other with the requirement of only slight difference in affinities to the replicator.

The proposed evolutionary scenario of gradual increase in metabolic complexity can progress till the coexistence is no longer possible due to internal redundancy (Fig. 2), which can be alleviated by increasing the cell's size at division. Cell sizes do not need to increase to infinity or even very high: at a certain metabolic complexity, replication efficiency and fidelity could increase to a level at which a chromosome can be replicated. Then integration of the genetic information, a chromosome, can evolve (Maynard Smith and Szathmáry, 1993). The emergence of the chromosome, a major evolutionary transition (Maynard Smith and Szathmáry, 1995; Szathmáry, 2015; Szathmáry and Maynard Smith, 1995), is made possible by overcoming the first error threshold. An interim solution to the first error threshold is the individual replication of ribozymes, which introduces the second error threshold. The second error threshold is alleviated by controlling the distribution of chromosomes to the daughter cells.

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